

# BULLETIN

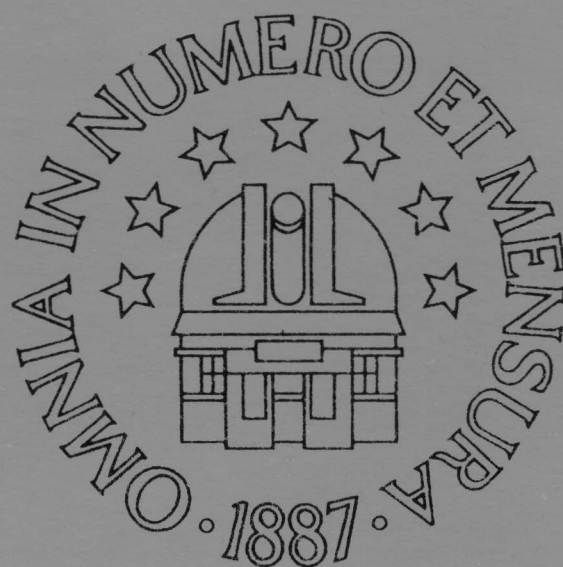
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## L'OBSERVATOIRE ASTRONOMIQUE DE BELGRADE

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# BULLETIN

DE

## L'OBSERVATOIRE ASTRONOMIQUE DE BELGRADE

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## A SEARCH AND CLASSIFICATION OF MULTIPLE SYSTEMS IN THE GENERAL FIELD

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**SUMMARY:** The subject of the present paper is a study of multiple stellar and galaxy systems aimed at a classification of their dynamical states and finding a statistical criterion for recognition of chance and non-chance groups of objects. The proposed statistical criterion is applied to some multiple systems of stars and galaxies. A corresponding algorithm is extended and finally the dynamical states of triple system ADS 9909 ( $\varphi$  Sco) are studied taking into account the uncertainty of the observational data.

## 1. INTRODUCTION

The study of surface and space distributions of stars and galaxies in the general Galactic and Metagalactic field shows a marked tendency to the clustering for these objects. It is joining of stars and galaxies in the multiples with a different number from the smallest systems (double and triple stars and galaxies) to the clusters of these objects with a large number.

The investigations of star multiplicity distributions in the solar neighbourhood (see e.g. Agekyan et al. 1962, Brosche 1964, Abt and Levi 1976, Dommanget 1977, Worley 1977, Poveda et al. 1982) have shown that a mean multiplicity ratio is equal approximately to 0.45 : 0.35 : 0.10 : 0.10 for the single, double, triple, and more multiple stars correspondingly. Dommanget (1977) made a statistical comparison between the multiple stars and the open star clusters and found that a significant distinction is observed in the characteristic distributions between the multiple systems with  $n \leq 10$ –20 and ones with  $n > 20$ . Therefore, one can consider the stellar systems with a number  $n \leq 10$ –20 as multiple stars, and ones with a larger  $n$  as star clusters.

The galaxies also have a strong tendency to the clustering, their multiplicity distribution is similar to the analogous one for the stars of our Galaxy. There have been also observed galaxies with multiple nuclei.

The study of multiple systems has interest for many problems in stellar and extragalactic astronomy because of widespreading of multiple stars and galaxies in the Galactic and Metagalactic fields and in the star and galaxy clusters, as well as some cosmogonic conclusion which one may draw from the investigation of statistics and dynamics of multiple systems (the age estimations for clusters, Galaxy and Metagalaxy including the multiples; a presentation of their qualitative evolution scenario etc.).

The general problems in the study of multiple systems of objects (stars, galaxies etc.) are the following ones:

1) a discovery of multiple systems in the general Galactic or Metagalactic field or in the star or galaxy clusters;

2) a separation of the discovered multiples to the chance (optical) groups of objects and the non-chance ones;

3) an edition of the systems with components connected physically;

4) a division of such multiple systems into the ones with components connected dynamically (i. e. with relatively strong dynamical connections) and the ones without such connections;

5) a division of the systems with connected components into the stable and unstable ones;

6) a numerical study of dynamical evolution for unstable systems: the estimations of their life-time; analysis of processes of formation, evolution, and motion for the subsystems of a smaller multiplicity; calculation of the trajectories of the component's relative motions etc.

One must solve the problems formulated above according to the indicated sequence. The necessary condition for solving these problems is the availability of the three-dimensional coordinates and velocities and relative masses for all components in a multiple system, i.e. the availability of data obtained by the combination of astrometrical and astrophysical observations of these objects. The problems enumerated require diverse accuracy levels in the data used for their solution, in addition to that the requirements to accuracy level grow as the number of problems increases. The complete solution of all problems enumerated above for multiple stars is possible only at the highest accuracy attainable at present for the observational data obtained from the ground observations as well as by the space observatories.

The problem to obtain the complex of observational data for star and galaxy systems is a complicated task in connection with some natural physical properties of their components. It requires significant efforts of specialists in different astronomical specializations. The majority of multiple stars and galaxies consists of the components of different brightnesses. Frequently the components have so significant diversity in the apparent magnitudes and in the spectral types (luminosity classes (for stars) or in the morphological types (for galaxies) that it strongly troubles obtaining homogeneous high-precise data for all components from the astrometrical observations as well as the astrophysical ones. Moreover, a large part of the observed multiple stars and galaxies have no known distances and for systems with the values  $r > 100$  pc it is impossible to solve correctly the problems formulated above at present. For the multiple galaxies, one may obtain the relative positions and radial velocities of components.

In connection with these difficulties, the problem to obtain the complex of astrometrical and astrophysical data for the multiple stars has not been practically formulated before. For the most part, the observations of components in multiple stars (until an assumed limited apparent magnitude) have been carried out by passing with the observations of double stars. Moreover, the programs of astrometrical and astrophysical observations include for the most part different objects: the photographic astrometrical observations are usually carried out for stars with  $m = 9^m - 11^m$ ; the astrophysical ones — for stars brighter than  $7^m - 8^m$ ; the program of meridian astrometrical observations includes only the primary components (brighter than  $4^m$ ) of a few multiple stars. For the multiple galaxies, there is also a significant deficit of observational data.

## 2. THE CONSTRUCTION OF HIERARCHICAL STRUCTURE FOR THE FIELD OF OBJECTS

The first problem in the study of multiple stars and galaxies is the discovery of such systems in the general Galactic or Metagalactic field or in the clusters of objects under consideration.

In the majority of works, some subjective methods have been used for a recognition of multiple systems (see e.g. Holmberg 1940, Karachentsev 1970, Turner and Gott 1977). Materne (1978) was the first to develop a strict algorithm to construct a hierarchical structure in the Metagalactic field on the base of the well-known mathematical method of cluster-analysis (see e.g. Aivisian et al.). Then Tully (1980), Huchra and Geller (1982), and Vennik (1984) used this method in order to compile the more complete and homogeneous lists of galaxy groups in the Metagalaxy.

This method consists of the following operations: 1) at first, one searches from a totality of  $N$  objects of the field two objects  $i$  and  $j$  ( $i, j = 1, 2, \dots, N$ ) with an extreme value of a selection parameter chosen (Materne (1978), Huchra and Geller (1982, 1983) have chosen it as a minimum three-dimensional distance  $R_{ij}$  between objects, Tully (1980) and Vennik (1984) have taken it as a maximum parameter of the gravitating force  $F_{ij} = M_{\max} R_{ij}^{-2}$ , where  $M_{\max} = \max(M_i, M_j)$ ,  $M_i$  and  $M_j$  are the masses of objects  $i$  and  $j$ ); 2) secondly, one considers such two objects as a single unit with a mass equal to the summary one of this binary and with an inertia centre at its baricentre; 3) furthermore, one uses this algorithm for  $N-1$  objects etc., until all the members within the considered totality are joined in a unified hierarchical structure according to a chain defined by the condition for the maximum of values  $R_{ij}^{-1}$  or  $F_{ij}$ .

In order to separate the members of multiple systems from the background objects, one must use some isolating criteria, however there is no objective criterion of such type at present. Therefore, some empirical dependences between the characteristics of multiple system components and background objects have been generally used. Such dependences reflect an isolation of the members of systems from the background objects in a phase space of coordinates and velocities. The diverse authors used the unlike selection parameters and various (sometimes strongly distinguishing from each other) decisive values of these parameters when they compiled the lists or catalogues of multiple stars and galaxies.

## 3. CLASSIFICATION OF MULTIPLE SYSTEMS

The multiple systems of objects (stars, galaxies, their groups or clusters etc.) with any number of compo-

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nents might be divided into three basic types from the dynamical point of view:

I - such multiple systems in which all or a few components are by chance within a region of the phase space covered by the system: these systems cannot be isolated from the background objects in the phase space; one may qualify suchlike systems as the *chance* groups of objects or *optical* systems;

II - such multiple systems which are no chance groups; they are isolated from the background objects in the phase space; their components have some common features; however, the gravitating forces between components are small or approximately equal to the regular forces of the environment; these systems, cannot be isolated from the background objects in the coordinate space; one may qualify suchlike systems as the *non-chance* groups of objects. One might divide these systems into two classes:

II a - systems completely isolated in the velocity space (e. g. the moving star clusters);

II b - systems only partially isolated in the ve-

locity space (e. g. in one or two of velocity components, like some of well-known Eggen's kinematical groups);

III - multiple systems which can be isolated from the background objects in the coordinate space; in these systems the irregular gravitating forces between their components essentially exceed the regular forces of the environment; one may qualify such systems as the multiples *with a physical connection* between their components.

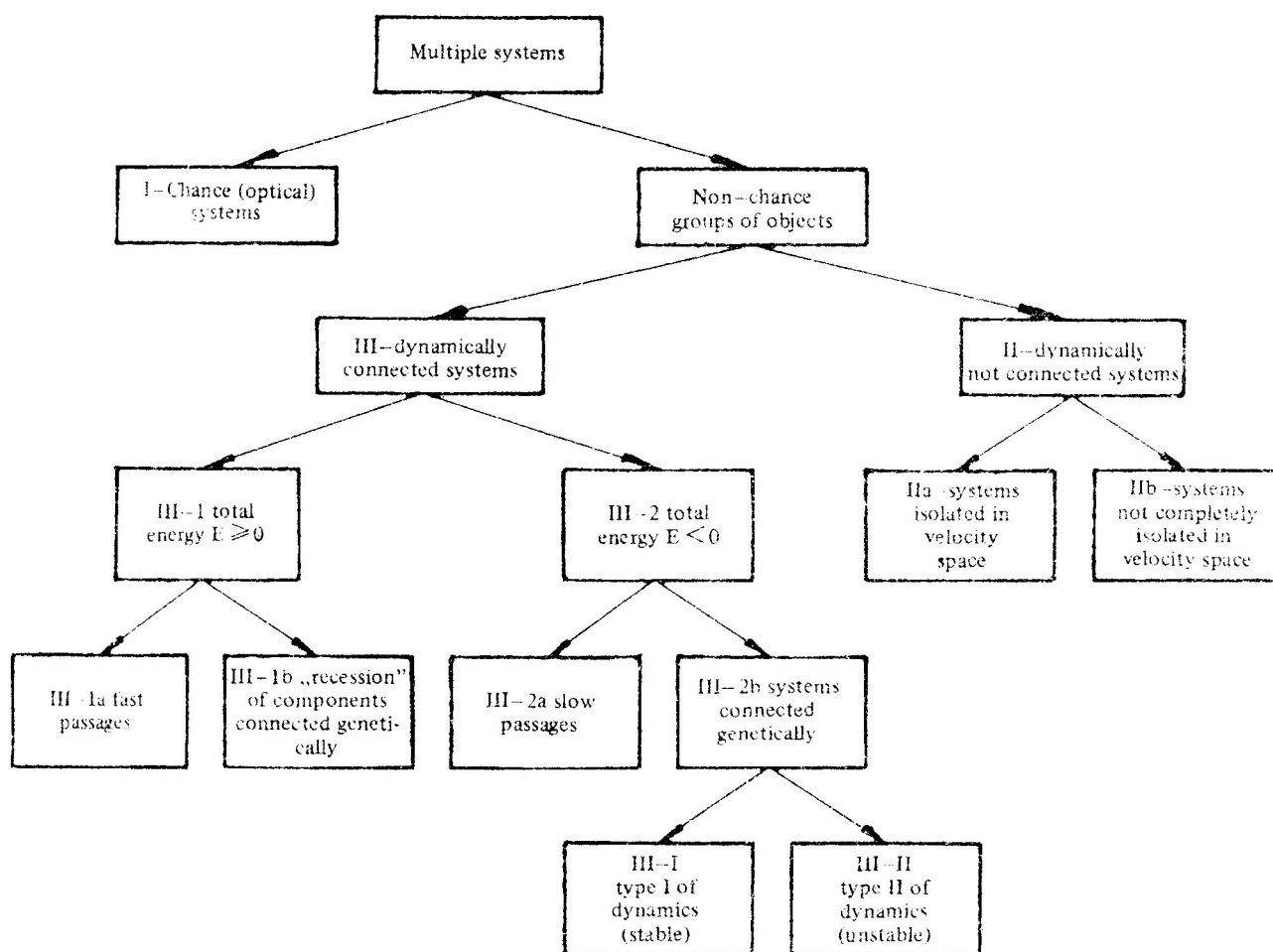
One might divide the systems of the latter type into two classes:

III - 1 - multiple systems in which *there is no dynamical connection* among all or a part of components so that the total energy is *non-negative*  $E \geq 0$ . One might also divide such systems into two subclasses:

III - 1a - the multiple systems in which *there is no genetic connection* among all or a part of components: all  $n$  single objects in a system *rapidly* pass by each other or a number  $s$  ( $s < n$ ) of single components and subsystems inside this system *rapidly* pass by each other,

Table 1

A classification of the states of multiple systems



III - 1b - the multiple systems in which *there is a genetic community* of components but also there is a „recession“ of components ( $E \geq 0$ ) - e.g. according to the well-known conception of V.A. Ambartsumian;

III - 2 - the multiples in which *there is a dynamical connection* of the components so that the total energy is *negative*  $E < 0$ ; one might also divide such systems into two subclasses:

III - 2a - the multiple systems in which *there is no genetic community* among a part of components: a number  $s$  ( $s < n$ ) of single components and subsystems with a smaller multiplicity than  $n$  inside a system pass slow ( $E < 0$ ) by each other;

III - 2b - the multiples in which *there is a genetic community among all components* (a co-formation); such systems may have one of two dynamical types:

III - I - *dynamically stable* multiples;

III - II - *dynamically unstable* ones.

The proposed classification of multiple systems (stars, galaxies etc.) might clearly be shown by a block-scheme (see Table 1).

#### 4. STATISTICAL CRITERIA FOR RECOGNITION OF CHANCE AND NON-CHANCE GROUPS OF OBJECTS.

Deutsch (1961) was the first to develop a statistical criterion in order to recognize the chance star groups in the galactic field; this criterion uses only the astrometric data for stars - the relative positions of components on the celestial sphere and their proper motions.

This criterion estimates the expectation EX of a number of chance realizations that  $n$  single stars will be found within a circle of radius  $\rho$  and area  $\sigma$  on the celestial sphere of total area  $\Sigma$ , on condition that the proper motions  $\mu$  of these stars are in agreement in limits of their uncertainties  $\delta\mu$

$$EX = C_N^n \left(\frac{\sigma}{\Sigma}\right)^{n-1} \left(\frac{\delta\mu}{\mu}\right)^{n-1}, \quad (1)$$

where  $C_N^n$  is a number of combinations from  $N$  by  $n$ ;  $N$  is the total number of stars; the star proper motions are represented as the vectors radiating from one point and reaching their ends to some region of area  $S$ ,  $s$  is an area of circle of radius  $\epsilon\sqrt{n}$  where  $\epsilon$  is a probable error of a single measurement of the star proper motion.

Deutsch's criterion is feasible only to the multiple stars. Moreover, it does not take into consideration a likeness or difference in the space characteristics of stars - their parallaxes and radial velocities.

In the present work, a statistical criterion is proposed in order to recognize the chance and non-chance star and galaxy groups with any multiplicity  $n$  which takes into consideration a likeness or difference of the individual configurational and kinematical data for

all components within a system

$$r, \mu, v_A; \quad \rho, r, \mu, v_i; \quad i=1, 2, \dots, n-1 \quad (2)$$

where  $A$  is the primary component of a system with multiplicity  $n$ ,  $i$  is the number of its  $i$ -th companion;  $\rho$  is the relative angular separation of the  $i$ -th object from the component  $A$ ;  $r$ ,  $\mu$ , and  $v$  are the distance on the line-of-sight, the modulus of a relative proper motion and the relative radial velocity accordingly. The effects of uncertainties in the values

$$\delta r, \delta\mu, \delta v_A; \quad \delta\rho, \delta r, \delta\mu, \delta v_i \quad (3)$$

are also taken into account.

The necessary condition in order to establish the chance or nonchance for a multiple system is shown to be an availability of the total complex of observed data (2) and (3) for all components, unless the relative orbits of all components are obtained. For every multiple system with a total complex of observed data, one could estimate:

1) the probability  $P$  that all  $n$  components have by chance been found in the region  $\sigma$  of phase space occupied by the multiple system,

2) the expectation EX of a number of the systems with parameters corresponding to the observed data (2) taking into account (3).

This probability  $P$  and expectation EX in the case of a sphere  $\Sigma$  with a radius  $R$  are estimated by the following formulae by assuming a random distribution of the objects within the sphere

$$P = C_{N-1}^{n-1} B^{n-1} (1-B)^{N-n} \quad (4)$$

$$EX = C_N^n B^{n-1} (1-B)^{N-n}$$

where  $B$  is the ratio of the volume of the region  $\sigma$  to the volume of the sphere  $\Sigma$  given as (Anosova 1990)

$$B = 1.55 \cdot 10^{-3} (\text{tg } \rho_{n/2})^2 \left(\frac{\text{tg } \Delta\mu/2}{\text{tg } \mu}\right)^2 \left(\frac{r_A}{R}\right)^5$$

$$\frac{|v_A|}{U} \dots \quad (5)$$

$$\left[1 - \left(\frac{r_n}{r_A}\right)^3\right] \left[1 - \left(\frac{r_n}{r_A}\right)^2 \frac{v_n}{v_A}\right]$$

where  $r_A > r_n$ ; the number  $n$  corresponds to a component that is the most distant one from the primary component  $A$  of the system; when  $r_A < r_n$  the indexes  $n$  and  $A$  in the quantities  $r$  and  $v$  are changed: the quantity  $U$  is the maximum possible total velocity of objects in the field under consideration,  $\mu$  is the proper motion of an object located at the distance  $R$  from observer which corresponds to the value  $U$ .

Comparing the expectations  $EX$  obtained with an observed number of multiple systems with data close to (2) in the uncertainty limits (3), one could conclude that the multiple system under consideration is a chance group of objects or a non-chance one by the following conditions:

I – the multiple system is certainly a non-chance group if the expectation is submitted to the inequality

$$EX \leq 1; \quad (6)$$

II – the multiple system is certainly a chance (optical) group if the equality takes place

$$EX \approx N/n, \quad (7)$$

where  $N/n$  is the maximum possible number of systems with multiplicity  $n$  in the general field of objects;

III – one cannot make any certain conclusion for the multiple system if the relation is realized

$$1 < EX < N/n \quad (8)$$

perhaps, the lack of confidence for such multiples is due to large errors (3) of the values (2).

The statistical criterion proposed might be used for solving of a number of problems: 1) a recognition of multiple systems – chance and non-chance groups of objects in stellar and extragalactic fields; 2) a sampling of the probable members in the moving star clusters and streams; 3) an elimination of the background objects in the star and galaxy groups and clusters; 4) a recognition inside the star and galaxy clusters of the subgroups of objects connected physically.

In the coordinate space, formula (5) becomes

$$B = 0.25 (\lg \rho_n / 2)^2 (r_A / R)^3 [1 - (r_n / r_A)^3] \quad (9)$$

where  $r_n < r_A$ . This formula with (4) is a statistical criterion isolating multiple systems in the coordinate space. It could be used in order to recognize multiple systems with components connected physically. By analogy, one can easily obtain a statistical criterion isolating multiples in the velocity space.

## 5. CRITICAL PARAMETER VALUES ISOLATING THE CERTAINLY PHYSICAL MULTIPLE STARS AND GALAXIES

One might use the criterion proposed above in order to recognize chance and non-chance groups of objects and physical multiples in order to obtain some objective critical values of parameters isolating the certainly physical systems from the probably background objects considering some different selection parameters – the relative angular separations  $\rho$  within pairs

of objects, the corresponding three-dimensional distances  $R$  or the parameter  $F$  of the gravitating force.

The condition (6) must be fulfilled for the certainly physical system with  $n$  components, and the condition (7) must be satisfied for the probably chance system with multiplicity  $n + 1$ , in this case the  $(n + 1)$ -th probably background object is the most nearby one to the system of multiplicity  $n$  in the coordinate space.

Transposing the expressions (4) and (9) in order to estimate the expectations  $EX_n$  and  $EX_{n+1}$  for the systems with multiplicities  $n$  and  $n+1$ , one can obtain the ratios of the parameters

$$\rho_{n+1} / \rho_n, R_{n+1} / R_n, F_{n+1} / F_n. \quad (10)$$

Substituting in the expressions obtained the quantities of the expectations (6) and (7), one obtains some objective extreme quantities (10) corresponding to a maximum possible isolation of a system with multiplicity  $n$  from the background objects of the field

$$\begin{aligned} (\rho_{n+1} / \rho_n)_{\max} &= \sqrt{N/n+1}, (R_{n+1} / R_n)_{\max} = \\ &= \sqrt{N/n+1}, \\ (F_{n+1} / F_n) &= (n+1/N) \frac{\max(M_{n+1}, \sum_{i=1}^n M_i)}{\max(M_n, \sum_{i=1}^{n-1} M_i)} \end{aligned} \quad (11)$$

Let us consider for example the triple stars in the solar neighbourhood within the radius  $R = 20$  pc (Gliese, 1969). For the certainly chance triple stars with components A, B, C in this case, one has the following limited estimations for the ratios of the selection parameters

$$\begin{aligned} (\rho_{n+1} / \rho_n)_{\max} &\cong 30, (R_{n+1} / R_n)_{\max} \cong 30, \\ (F_{n+1} / F_n)_{\max} &\cong 10^{-3}. \end{aligned} \quad (12)$$

The proposed statistical criterion recognizing the chance and nonchance multiple systems gives some possibility to estimate a critical quantity  $\Delta v_{cr}$  for the tolerant differences of the radial velocities of components in the certainly physical multiple galaxies for the different separation between their components on the celestial sphere and along the line of sight. The results of calculations carried out for the double Markarian galaxies from a paper of Dahari (1985) are shown in Table 2 in which the quantity  $\Delta v_{cr}$  is expressed in km/s,  $z$  is the redshift of the primary component within a binary,  $D$  is the linear distance between the components in kpc. The estimations obtained show that the quantity  $\Delta v_{cr}$  strongly varies depending on the values of  $z$  and  $D$ ; if their values, are small the quantity  $\Delta v_{cr}$  may reach the largest values of  $\Delta v_{cr} = 1000$  km/s. As the values  $z$  and  $D$  increase the quantity  $\Delta v_{cr}$  rapidly decreases and falls to the values compared with the uncertainties of modern observations of radial velocities of galaxies.

Table 2

The quantities  $\Delta v_{cl}$  (km/s) for multiple galaxies with components connected physically ( $EX \leq 1$ )

| $z$ d(kpc)        | 10   | 30  | 50 | 70  |
|-------------------|------|-----|----|-----|
| $10^{-2}$         | 1000 | 150 | 60 | 30  |
| $2 \cdot 10^{-2}$ | 200  | 20  | 10 | 5   |
| $3 \cdot 10^{-2}$ | 50   | 5   | 2  | 1   |
| $4 \cdot 10^{-2}$ | 25   | 1   | 1  | 0.5 |

## 6. APPLICATION OF THE STATISTICAL CRITERION TO MULTIPLE STARS AND GALAXIES

### a) some wide triple stars in the solar neighbourhood

In the Index catalogue of double and multiple stars (Jeffers et al. 1963), there are a few wide multiple systems which have large angular separations between their components. A distribution  $N(\rho)$  for the binaries and multiples from this Catalogue, where  $\rho$  is the maximum separation between two components, is presented

#### Distribution $N(\rho)$ of multiple stars in IDS

| $\rho$   | 0-2              | 2-5              | 3-5              | 5-10           | 10-30          | 30-100 | 100 |
|----------|------------------|------------------|------------------|----------------|----------------|--------|-----|
| N        | $5.4 \cdot 10^4$ | $1.6 \cdot 10^4$ | $2.6 \cdot 10^2$ | $7.2 \cdot 10$ | $2.5 \cdot 10$ | 2      | 2   |
| $N(n=3)$ | $3.9 \cdot 10^3$ | $1.7 \cdot 10^2$ | $3.3 \cdot 10$   | 9              | 2              | 1      | 1   |

Table 3

in Table 3. The data for triple stars are separately shown in the third column of this Table.

Among these triple stars, one selects seven systems located at the distances from the Sun shorter than 20 pc and having the total complex of observed data (2) and (3) for all components. The most distant components have the characteristics (2) similar to the ones of other components in five wide multiple stars presented. For two systems ADS 10058 and ADS 11853, the distances from the Sun and the radial velocities of the distant components are in disagreement with the corresponding values of other components.

Using the proposed statistical criterion, one estimates for the multiple stars under consideration the probability  $P$  that component C, that is the most distant one from the primary component A, by chance in its environment, and the expectation  $EX$  of a member of suchlike optical systems inside the sphere of radius  $R = \max(r_A, r_C)$  on the following parameters of the stellar field (see e.g. Wielen 1974): a radius of the neighbourhood  $R = 20$  pc, a mean local star number density  $\nu = 0.12$  stars in  $1 \text{ pc}^3$ , a velocity  $|v| = 20$  km/s, and a peculiar velocity standard  $\sigma_v = 20$  km/s. The results of calculations are in Table 4.

Table 4

#### The probabilities $P$ and expectations $EX$ of a number of optical stars (chance groups)

| ADS                   | 7114+<br>(9+10)UMa   | $\alpha$ Cen        | 20390<br>S3142      | 10058            | 11853               | 48                   | 6175<br>(Castor)     |
|-----------------------|----------------------|---------------------|---------------------|------------------|---------------------|----------------------|----------------------|
| $\rho'$               | $3.8 \cdot 10^2$     | $1.3 \cdot 10^2$    | $7.7 \cdot 10$      | 9.4              | 6.9                 | 5.5                  | 1.2                  |
| The probabilities $P$ |                      |                     |                     |                  |                     |                      |                      |
| 1)                    | $5.0 \cdot 10^{-3}$  | $7.6 \cdot 10^{-5}$ | $2.6 \cdot 10^{-5}$ | 0.30             | $2.6 \cdot 10^{-5}$ | $1.4 \cdot 10^{-7}$  | $7.2 \cdot 10^{-8}$  |
| 2)                    | $1.1 \cdot 10^{-4}$  | $5.3 \cdot 10^{-7}$ | $4.2 \cdot 10^{-7}$ | 0.60             | $2.5 \cdot 10^{-5}$ | $5.2 \cdot 10^{-5}$  | $1.2 \cdot 10^{-8}$  |
| 3)                    | $7.3 \cdot 10^{-5}$  | $2.8 \cdot 10^{-7}$ | $2.5 \cdot 10^{-7}$ | 0.60             | $3.0 \cdot 10^{-9}$ | $3.0 \cdot 10^{-9}$  | $5.9 \cdot 10^{-9}$  |
| 4)                    | $2.8 \cdot 10^{-5}$  | $7.0 \cdot 10^{-8}$ | $7.6 \cdot 10^{-8}$ | 0.30             | $2.6 \cdot 10^{-5}$ | $4.0 \cdot 10^{-10}$ | $8.0 \cdot 10^{-10}$ |
| $R_{pc}$              | 20                   | 20                  | 20                  | 200              | 50                  | 20                   | 20                   |
| The expectations $EX$ |                      |                     |                     |                  |                     |                      |                      |
| 1)                    | 8.5                  | $0 \cdot 10$        | $4.5 \cdot 10^{-2}$ | $5.3 \cdot 10^5$ | 0.68                | $2.4 \cdot 10^{-3}$  | $1.2 \cdot 10^{-4}$  |
| 2)                    | 0.18                 | $8.9 \cdot 10^{-4}$ | $7.2 \cdot 10^{-4}$ | $0.3 \cdot 10^6$ | 0.59                | $3.4 \cdot 10^{-4}$  | $1.9 \cdot 10^{-5}$  |
| 3)                    | 0.12                 | $3.5 \cdot 10^{-4}$ | $4.5 \cdot 10^{-4}$ | $0.3 \cdot 10^6$ | 0.58                | $2.0 \cdot 10^{-6}$  | $9.1 \cdot 10^{-6}$  |
| 4)                    | $0.47 \cdot 10^{-1}$ | $1.1 \cdot 10^{-4}$ | $1.3 \cdot 10^{-4}$ | $5.6 \cdot 10^5$ | 0.68                | $2.6 \cdot 10^{-7}$  | $1.3 \cdot 10^{-6}$  |

Explanations: 1) only  $\rho$  values used; 2) only  $\rho$  and  $\mu$  used; 3)  $\rho, \mu, r$  used; 4) used values of all quantities  $\rho, \mu, r, v$ .



It appears that the first five multiple stars are certainly physical systems; ADS 10058 is probably an optical one; the quadruple star ADS 11853 is a projection of two physical binaries.

#### b) the multiple galaxies in the metagalactic field

Let us calculate the values  $P$  and  $EX$  for the galaxy triplets from a list of Karachentseva et al. (1979). The following characteristics of the metagalactic field were used for the estimations of the quantities sought: a mean galaxy number density of  $\nu = 0.05$  galaxies in  $1 \text{ Mpc}^3$  (see Agekyan et al. 1962), the Hubble constant is  $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , the radius of the sphere is  $R = \max(r_A, r_C)$ .

The results of calculations are in Table 5, the triplets classified by the authors of the list as the probably physical systems on a critical quantity  $\Delta v_{cr} = 500 \text{ km/s}$  are marked by asterisks. In Table 6 (the second line), there is a distribution  $N(EX)$  of the galaxy triplets in the values  $EX$ . This Table shows that the galaxy triplets are clearly separated into two groups according to the quantities  $EX$ : 44 triplets have  $EX < 300$ , and 33 ones have  $EX > 1000$ , there are only 6 triple galaxies in the intermediate interval. If one considers  $EX = 300$

as a critical value of  $EX$  (an increasing of  $EX$  may be caused by an internal velocity dispersion as well as by the uncertainties in the values  $v$  of components) then for the most part (70 triplets out of 83 ones) the results by I.D. Karachentsev and V.E. Karachentseva on the selection of the physical galaxy triplets are confirmed. Only in three cases (N 33, 50, and 68 from the list by Karachentseva et al. 1979), the nearby triplets with close components have a difference  $\Delta v$  of the radial velocities more than  $500 \text{ km/s}$ , however the values  $EX$  for them are small and these triplets might be qualified as probable physical systems. Ten distant and wide systems (N 31, 34, 46, 48, 60, 73–77) with  $\Delta v < 500 \text{ km/s}$  have  $EX > 300$  and therefore they might be qualified as possible chance (optical) systems. Use of the criteria (6) and (7) enables to recognize 11 certainly physical systems (N 1, 22, 24, 25, 28, 33, 36, 39, 41, 44, 54) with  $EX < 1$  and 33 probably optical systems with  $EX > 10^3$  (their numbers are underlined in Table 6) among the triple galaxies under consideration. In Table 7 there are the distributions of the ratios of three-dimensional distances for the galaxy triplets with the quantities  $EX$  inside the intervals indicated. In the last line of this Table a number of triplets with corresponding values  $EX$  is given, in Table 7a there are the

Table 5

#### Triplets of galaxies

| $N^0$ | $EX$                 | $N^0$ | $EX$                | $N^0$ | $EX$                | $N^0$ | $EX$                | $N^0$ | $EX$             | $N^0$ | $EX$             |
|-------|----------------------|-------|---------------------|-------|---------------------|-------|---------------------|-------|------------------|-------|------------------|
| 1*    | $3.4 \cdot 10^{-13}$ | 15*   | $2.7 \cdot 10^2$    | 29    | $8.2 \cdot 10^2$    | 43*   | $6.8 \cdot 10$      | 57    | $7.1 \cdot 10^3$ | 71*   | $2.1 \cdot 10^2$ |
| 2*    | $2.2 \cdot 10^2$     | 16*   | $2.9 \cdot 10^2$    | 30    | $1.5 \cdot 10^5$    | 44*   | $4.3 \cdot 10^{-3}$ | 58    | $2.9 \cdot 10^4$ | 72*   | $2.4 \cdot 10^2$ |
| 3*    | $3.0 \cdot 10$       | 17    | $8.8 \cdot 10^3$    | 31*   | $6.9 \cdot 10^2$    | 45*   | $2.2 \cdot 10$      | 59*   | $2.1 \cdot 10^2$ | 73*   | $3.5 \cdot 10^3$ |
| 4*    | $8.5 \cdot 10$       | 18    | $5.9 \cdot 10^4$    | 32    | $5.2 \cdot 10^3$    | 46*   | $1.3 \cdot 10^3$    | 60*   | $0.8 \cdot 10^4$ | 74*   | $7.1 \cdot 10^3$ |
| 5     | $1.1 \cdot 10^4$     | 19    | $9.1 \cdot 10^4$    | 33    | $2.4 \cdot 10^{-1}$ | 47*   | $1.4 \cdot 10^2$    | 61*   | $5.8 \cdot 10$   | 75*   | $5.5 \cdot 10^2$ |
| 6     | $2.9 \cdot 10^5$     | 20    | $4.7 \cdot 10^3$    | 34*   | $4.1 \cdot 10^3$    | 48*   | $3.3 \cdot 10^2$    | 62*   | 9.0              | 76*   | $1.6 \cdot 10^3$ |
| 7     | $7.2 \cdot 10^4$     | 21*   | 8.9                 | 35    | $1.9 \cdot 10^4$    | 49*   | $2.3 \cdot 10^2$    | 63    | $3.7 \cdot 10^3$ | 77*   | $2.8 \cdot 10^3$ |
| 8     | $2.3 \cdot 10^3$     | 22*   | $5.5 \cdot 10^{-1}$ | 36*   | $9.3 \cdot 10^{-2}$ | 50    | $2.0 \cdot 10$      | 64*   | $7.9 \cdot 10$   | 78*   | $6.7 \cdot 10$   |
| 9     | $2.2 \cdot 10^4$     | 23*   | $1.7 \cdot 10^{-5}$ | 37    | $0.5 \cdot 10^{-7}$ | 51*   | $1.2 \cdot 10^2$    | 65    | $2.8 \cdot 10^5$ | 79*   | $1.4 \cdot 10^2$ |
| 10    | $1.8 \cdot 10^3$     | 24    | $9.0 \cdot 10^4$    | 38*   | $1.0 \cdot 10^2$    | 52*   | $1.4 \cdot 10$      | 66    | $1.8 \cdot 10^3$ | 80*   | 2.2              |
| 11*   | $6.0 \cdot 10$       | 25*   | $8.8 \cdot 10^{-1}$ | 39*   | $2.2 \cdot 10^{-1}$ | 53    | $1.6 \cdot 10^4$    | 67*   | $1.6 \cdot 10^2$ | 81*   | $9.3 \cdot 10$   |
| 12*   | $9.5 \cdot 10$       | 26*   | $6.3 \cdot 10$      | 40    | $9.1 \cdot 10^4$    | 54*   | $4.8 \cdot 10^{-1}$ | 68    | $2.3 \cdot 10^2$ | 82*   | $1.7 \cdot 10$   |
| 13    | $5.8 \cdot 10^5$     | 27    | $5.7 \cdot 10^4$    | 41*   | $3.8 \cdot 10^{-3}$ | 55*   | 1.7                 | 69    | —                | 83    | $8.6 \cdot 10^2$ |
| 14*   | $3.0 \cdot 10$       | 28*   | $2.1 \cdot 10^{-2}$ | 42*   | 3.6                 | 56    | $1.6 \cdot 10^5$    | 70*   | $3.5 \cdot 10$   | 84    | $1.6 \cdot 10^5$ |

Table 6

#### A distribution of expectations $EX$ for the multiple galaxies from the lists of Karachentseva et al. and Dahari

| $EX$    | $\leq 1$ | 1–10 | 10–100 | 100–300 | 300–500 | 500–1000 | $> 1000$ |
|---------|----------|------|--------|---------|---------|----------|----------|
| $n = 3$ | 10       | 5    | 16     | 13      | 3       | 3        | 33       |
| $n = 2$ | 17       | 11   | 7      | 6       | 3       | 3        | 2        |



mean values and rms deviations for the parameters EX,  $R_C/R_B$ , and  $\rho_C/\rho_B$ . The data show (Table 7) that a strong prevalence of small ratios  $R_C/R_B$  (an isolation of the distant component from the close pair is not large) takes place for the probably physical galaxy systems with  $EX < 300$ . At the same time, the distribution of values  $R_C/R_B$  for the probably optical systems is practically random within the interval (1, 100). Table 7a shows also the absence of correlation between the quantities (EX,  $\rho_C/\rho_B$ ) and ( $R_C/R_B$ ,  $\rho_C/\rho_B$ ). According to this Table, the certainly physical systems have  $R_C/R_B \leq 5$ , the probably physical ones have  $5 < R_C/R_B \leq 15$ , the possible chance ones have  $15 < R_C/R_B \leq$

30, and the certainly optical (chance) systems have  $R_C/R_B > 30$ .

Now, let us apply the statistical criterion of recognizing optical and physical multiple systems to the close double galaxies from the list of Dahari (1985) in which the primary components are Seyfert galaxies. The results of calculation of P and EX for these objects are in Table 8, the distribution N (EX) for them is given in the third line of Table 6. These data show that the condition  $EX \leq 1$  is satisfied for 17 nearby and close double galaxies and they may be qualified as certain physical systems; the inequality  $1 < EX \leq 300$  takes place for 24 binaries and they might be qualified as

Table 7

The distributions of the hierarchy coefficients of galaxy triplets

| $R_C/R_B \backslash EX$ | $\leq 1$ | 1-100 | 100-300 | 300-1000 | $10^3-10^5$ |
|-------------------------|----------|-------|---------|----------|-------------|
| 1 - 5                   | 4        | 12    | 6       | 2        | 7           |
| 5 - 10                  | 6        | 7     | 2       | 2        | 6           |
| 10 - 20                 | 1        | 2     | 3       | 0        | 4           |
| 20 - 50                 | 0        | 1     | 1       | 2        | 5           |
| 50 - 100                | 0        | 0     | 0       | 0        | 6           |
| > 100                   | 0        | 0     | 1       | 0        | 5           |
| N                       | 17       | 22    | 13      | 6        | 32          |

Table 7a

The means of hierarchy coefficients for the galaxy triplets

|                   |               |               |               |               |                          |
|-------------------|---------------|---------------|---------------|---------------|--------------------------|
| EX                | $0.1 \pm 0.2$ | $47 \pm 36$   | $210 \pm 54$  | $540 \pm 200$ | $(30 \pm 14) \cdot 10^3$ |
| $(R_C/R_B)$       | $4.3 \pm 2.3$ | $8.0 \pm 7.3$ | $16 \pm 25$   | $18 \pm 21$   | $45 \pm 65$              |
| $(\rho_C/\rho_B)$ | $3.0 \pm 1.8$ | $2.9 \pm 1.8$ | $3.0 \pm 2.2$ | $2.9 \pm 1.2$ | $3.5 \pm 4.1$            |
| N                 | 11            | 22            | 13            | 6             | 32                       |

Table 8

Seyfert double galaxies

| $N^0$ | EX                  | $N^0$ | EX                  | $N^0$ | EX                  | $N^0$ | EX                  | $N^0$ | EX                  |
|-------|---------------------|-------|---------------------|-------|---------------------|-------|---------------------|-------|---------------------|
| 10    | $6.0 \cdot 10^2$    | 463   | 1.3                 | 915   | $1.3 \cdot 10^2$    | 3227  | $7.0 \cdot 10^{-3}$ | 5506  | $1.0 \cdot 10$      |
| 40    | $2.5 \cdot 10^{-4}$ | 474   | $7.4 \cdot 10^3$    | 926   | $8.1 \cdot 10^2$    | 3516  | $2.0 \cdot 10^2$    | 5929  | $1.2 \cdot 10^{-2}$ |
| 141   | $1.1 \cdot 10^2$    | 506   | $1.2 \cdot 10$      | 975   | 6.1                 | 3998  | $3.5 \cdot 10^{-2}$ | 5953  | $7.6 \cdot 10^{-1}$ |
| 176   | 4.0                 | 530   | $2.9 \cdot 10^3$    | 1040  | $2.4 \cdot 10^{-1}$ | 4117  | $3.6 \cdot 10^{-2}$ | 6251  | $3.9 \cdot 10^2$    |
| 266   | $7.2 \cdot 10^{-2}$ | 533   | $1.3 \cdot 10$      | 1073  | $4.1 \cdot 10^2$    | 4151  | $1.3 \cdot 10^2$    | 7212  | $4.4 \cdot 10^6$    |
| 268   | $9.6 \cdot 10^2$    | 595   | $1.3 \cdot 10^2$    | 1218  | 5.9                 | 4258  | $5.1 \cdot 10^{-3}$ | 7319  | 1.8                 |
| 279   | $5.2 \cdot 10$      | 612   | 9.5                 | 1239  | 3.1                 | 4593  | 1.6                 | 7469  | 1.9                 |
| 349   | $9.7 \cdot 10^{-1}$ | 716   | $2.7 \cdot 10$      | 1144  | 7.4                 | 4922  | $3.9 \cdot 10^{-2}$ | 4329  | $1.3 \cdot 10$      |
| 374   | $4.4 \cdot 10^2$    | 739   | $1.0 \cdot 10^{-1}$ | 2992  | $5.3 \cdot 10^{-1}$ | 5273  | $2.2 \cdot 10$      | 700   | 2.5                 |
| 423   | 1.2                 | 744   | $2.0 \cdot 10$      | 3031  | $5.1 \cdot 10$      | 5427  | $6.2 \cdot 10$      |       |                     |

probable physical systems; six doubles (MrK 10, 268, 374, 926, 1073, and 6251) might be qualified as probable optical systems and two double galaxies (MrK 474 and 550) with  $EX > 10^3$  are certainly optical systems.

## 7. ALGORITHM FOR RECOGNITION, ESTABLISHMENT OF A NUMBER AND MULTIPLICITY FOR SYSTEMS, AND THEIR CLASSIFICATION IN THE GENERAL FIELD

After constructing a hierarchical structure for a field of objects, using the statistical criterion one can recognize the groups of objects in the field, establish the number and multiplicity of them, and make their classification — in order to separate the chance and physical systems among them.

A proposed algorithm consists of the following operations:

1) one takes any object  $A_j$  from the general totality of  $N$  objects in the field;

2) for this object  $A_j$ , one constructs a sequence of  $N - 1$  objects arranged according to decreasing of the selection parameter used in the construction of the hierarchical structure of the field;

3) for this sequence of  $N - 1$  objects, one obtains a sequence of the expectations  $EX_1, EX_2, \dots, EX_{N-1}$  according to the formulae (4) and (5) justified for the phase space;

every time, one considers as a primary object of a multiple system the inertia centre of a subsystem consisting of  $i - 1$  objects for which the calculations have already been executed, and the observational data (2) and (3) for this subsystem are obtained as the means for  $i - 1$  and  $A_j$  objects;

4) one verifies the inequality (6)  $EX \leq 1$  for every element of the sequence  $EX_i$  ( $i = 1, 2, \dots, N - 1$ ). Note that the sequence  $EX_i$  determined for  $N - 1$  objects considered in the phase space is no monotonously increasing sequence in spite of decreasing of the selection parameter with rise of the number  $i$ ;

5) a number  $K$  of elements from the totality  $EX_i$  satisfying the condition (6) then determines the multiplicity of this system  $n = K + 1$ ; if neither of the elements  $EX_i$  satisfies the condition (6) then the object  $A_j$  is qualified as a single object of the field; if the criterion of isolation in the phase space is not satisfied for any object  $i$  then the observed data for this object  $i$  are excluded from the calculation of  $EX_{i+1}$ , i.e. the position of object  $i + 1$  in the phase space is considered in regard to the inertia centre of  $i - 1$  objects etc.;

6) an examination of elements  $A_j$  from the general totality of  $N$  objects excluding from it the objects included in the multiple systems found earlier allows to define a number  $n^*$  and a composition of the non-chance groups of objects with a various multiplicity in the general field;

7) by repeating the operations 1) and 2) and by using the statistical criterion of isolating in the coordinate space — one determines for every object  $A_j$  ( $j = 1, 2, \dots, N$ ) a sequence of the expectations  $EX_{ij}^*$  for the number of the corresponding chance groups in the coordinate space by using formulae (4) and (9) with the observational parameters of their members. The obtained sequences  $EX_{ij}^*$  are the monotonously increasing sequences in accordance with the algorithm used for adding of objects to an object  $A_j$ ;

8) one finds objects for which the inequality (6) ceases to be fulfilled for the increasing sequence  $EX_{ij}^*$ ;

9) the number  $i + 1$  determines a multiplicity  $n_1 = i + 1$  of a system (an object  $A_j$  and  $i$  of its companions) for which the condition of isolation is fulfilled in the coordinate space, and this system might be qualified as the certainly physical system in the field of objects under study;

10) a repetition of the operations 6) gives a number  $n^{**}$  of systems with a physical connection of their components isolated in the coordinate space. Using the statistical criterion of isolation in the velocity space, one may recognize the multiples — the certainly non-chance groups in this space — by repetition of operations 7) — 10).

## 8. CRITERIA FOR CLASSIFICATION OF DYNAMICAL STATES IN CERTAINLY PHYSICAL MULTIPLE SYSTEMS

The main characteristics of dynamical states within multiples which are certainly physical (the type III of the classification of multiple systems — see item III) are the values of their total energies  $E$  and the relative energy  $E_{ij}$  ( $i, j = 1, 2, \dots, n, i \neq j$ ) of every possible combinations of components — the subsystems of a smaller multiplicity. The signs of the energies  $E$  and  $E_{ij}$  determine the existence or absence of dynamical connection between the components and correspondingly the classes of multiples.

Class III — 1 — multiple systems in which *there is no dynamical connection* of the components, they have *non-negative total energies*  $E \geq 0$ . The following cases are possible:

a — 1)  $E \geq 0, E_{ij} \geq 0; i, j = 1, 2, \dots, n; i \neq j$

for all possible combinations of components in a system — *the dynamical connection is absent for all components*;

a — 2)  $E \geq 0, E_{ij} < 0; i, j = 1, \dots, s; i \neq j; s < n$

(for some subsystems of a lower multiplicity) — in a multiple system there are  $s$  components connected dynamically, the rest of  $n - s$  components are not dynamically connected with them and with each other;

b) the subclass — „recession” of components *connected genetically* (a *co-formation*) in a system shows a special case when two or a few components have a positive

relative energy and move in the opposite directions with a large relative velocity.

Class III-2 — multiple systems in which there is a dynamical connection between all components, they have a negative total energy  $E < 0$ .

In order to relate two types of dynamics in multiple systems (stable or unstable systems) with the components connected dynamically and physically (class III — 2b) one should use the criteria developed in celestial mechanics (see e.g. Timoshkova and Kholshchikov 1982, Anosova 1985) for stability of the systems consisting of  $N$  gravitating bodies.

III — 1 — *dynamically hierarchical stable* multiple systems with Keplerian character of motions of the bodies — the stability criteria (the conditions of isolation of the distant bodies from the subsystems of other bodies) are fulfilled during all the time of dynamical evolution of a multiple system.

III — II — *dynamically non-hierarchical unstable* multiple systems are separated by two forms:

a) the conditions of an escape (a hyperbolicity of mainly radial motion of a distant component regarding to a subsystem of other bodies) are fulfilled from the very beginning of a study of the dynamical evolution

b) the escape conditions in a system will be fulfilled after a certain lapse of time  $T$  from the beginning of tracking of its evolution.

## 9. TAKING INTO ACCOUNT THE UNCERTAINTIES IN THE OBSERVED DATA ON CLASSIFICATION OF MULTIPLE SYSTEMS

In order to estimate the dynamical state of an observed star or galaxy system one must take into account some uncertainties in the observational data i.e. take into account the errors in the initial state of this system.

In the present work, in order to take into consideration this effect one proposes to use a method of statistical tests — a method of variation of observational data in the limits of their uncertainties for the components of multiple systems.

Let us describe this method for the triple stellar systems; it could be easily generalized for a system with any multiplicity.

One has for the components within a triple star system a vector of observational parameters

$$\vec{X} = (x_1, x_2, \dots, x_{19}) = (\rho, \theta)_{AB, AC}; (\mu_\alpha, \mu_\delta, \nu, \pi, M)_{A, B, C} \quad (15)$$

and a vector of their errors

$$\vec{\delta x} = (\delta x_1, \delta x_2, \dots, \delta x_{19}). \quad (16)$$

The dynamical state of a triple system is determined by the following energetic characteristics: the

total energy

$$E = E(\vec{X}), \sigma_E = \sigma_E(\vec{X}, \vec{\delta x}) \quad (17)$$

and the relative energies of pairs of components

$$E_{ij} = E_{ij}(\vec{X}), \sigma E_{ij} = \sigma E_{ij}(\vec{X}, \vec{\delta x}) \quad (18)$$

Let us use the Monte Carlo method of the variations of values  $x_i$  within the confidence intervals

$$x_{ij} \in [x_i - \kappa \delta_{x_i}, x_i + \kappa \delta_{x_i}] \quad (19)$$

where  $i = 1, 2, \dots, 19$  is the number of the observational parameters,  $x_i$  are their observed quantities,  $j = 1, 2, \dots, N$  is the number of the test. Proposing the Gaussian distribution for the uncertainties  $\delta_{x_i}$  truncated at the confidence probability  $P = 0.95$  one has a quantity  $\kappa = 2$ .

For every multiple system, one can make  $N$  tests varying all (or by turns) in order to obtain every time new quantities for these parameters and to calculate by them the energetic characteristics  $E$  and  $E_{ij}$  which determine every time the class of the dynamical state of this multiple system. For a large number of tests ( $N \approx 10^3 - 10^4$ ), the frequency of realization of the classes of dynamical states determines the probabilities of these states for a multiple system under consideration.

## 10. DYNAMICAL STATES FOR SELECTED TRIPLE STARS

An analysis of data from nearly 60 Catalogues received from the Centre de Données Stellaires in Strasbourg by the Centre of Astronomical Data of the Astronomical Council of the Academy of Sciences of the U.S.S.R. has shown that at present the total complex of observational data necessary for solution of the problems formulated above (see section II) concerning the study of multiple systems exists for 16 nearby and bright triple stars including such well-known systems such as  $\alpha$  Cen,  $\alpha$  Gem (Castor),  $\gamma$  And etc. However even for these systems, the estimations of uncertainties in the observational data are not present in the Catalogues for all components. In the present paper 8 triple stars are investigated: ADS 1630, 2926, 6175 (Castor), 6650, 6811, 7114, 9626, and 9909.

The results of application of the method of simultaneous variations of all observational parameters within the limits of their errors are given in Table 9 for these triple stars. In Table 9 there are the probabilities of dynamical states of these systems, the mean quantities of their energetic characteristics — the total energy  $E$  and energy  $E_b$  of a close pair and the mean quantities  $\sigma E$  and  $\sigma E_b$  for the boundaries of confidence intervals at the level  $1\sigma$  for these values.

Table 9

The probabilities of dynamical states and means of energetic parameters of the triple stellar systems

| Name           | ADS  | $(r_{pc})$ | Probabilities P of states |       |             | $E \pm \sigma_E$ | $E_b \pm \sigma_{E_b}$ |
|----------------|------|------------|---------------------------|-------|-------------|------------------|------------------------|
|                |      |            | I ( $E \geq 0$ )          | III-I | ( $E > 0$ ) |                  |                        |
| $\gamma$ And   | 1630 | 80         | 0.00                      | 0.53  |             | $-117 \pm 25$    | $-104 \pm 19$          |
| Castor         | 6175 | 14         | 0.02                      | 0.12  |             | $-18 \pm 10$     | $-17 \pm 10$           |
| $\gamma$ Sco   | 9909 | 22         | 0.00                      | 0.20  |             | $-531 \pm 8.6$   | $-44.3 \pm 7.5$        |
| $\zeta$ Cnc    | 6650 | 19         | 0.29                      |       | 0.71        | $-12 \pm 25$     | $-31 \pm 17$           |
| $\mu$ Boo      | 9626 | 29         | 0.11                      |       | 0.89        | $-10.0 \pm 8.4$  | $-19.6 \pm 6.4$        |
| 21 Cnc         | 6811 | 50         | 0.30                      |       | 0.70        | $-50 \pm 140$    | $-80 \pm 110$          |
| $\epsilon$ UMa | 7114 | 16         | 0.20                      |       | 0.80        | $-4.6 \pm 4.5$   | $-2.5 \pm 2.6$         |
|                | 2926 | 170        | 0.97                      |       | 0.03        | $+23 \pm 23$     | $+15 \pm 23$           |

One may formulate the results obtained as the following ones:

1) the triple stars ADS 1630, 6175, and 9909 located at the distances from the Sun of 80, 14, and 22 pc, respectively, are certainly dynamically connected systems with a probability  $P \geq 0.98$  (the variations of

energies are  $\delta E = \left| \frac{\sigma E}{E} \right|$ ,  $\delta E_b = \left| \frac{\sigma E_b}{E_b} \right| \leq 0.2, 0.6$ ).

2) the triples ADS 2926, 6650, 6811, 7114, and 9626 have large variations of the total energy  $\delta E \approx 1-3$ . Therefore, for them one cannot certainly obtain the values of the total energies. However, the probabilities of dynamical connections in these systems, except in ADS 2926, are large  $P(E < 0) > 0.7$ . The triple star ADS 2926 has a positive energy  $P(E > 0) = 0.97$  according to the observed data existing at present. Moreover, the maximum contribution in the positive energy  $E$  appears to make a positive energy  $E_b$  of the close pair AB with an angular separation  $\rho = 7''.6$  between the components  $P(E_b > 0) = 0.77$ . It should be noted that the kinematical parameters of an inertia centre of the pair AB and a distant component C are in good agreement, but the uncertainties of space velocities of A and B are significantly large. Therefore, the problem of physical connections of the components of ADS 2926 may be solved only after a closer definition of the kinematical characteristics of the close pair;

3) the triple systems ADS 6650 and ADS 9626 have small variations of the energies of the close pairs  $\delta E_b \approx 0.2, 0.5$  and these pairs are dynamically connected binaries with a probability  $P = 0.96$ ; in order to establish some dynamical connection between these binaries and the third distant component one must verify the kinematical parameters for the latter one.

4) in the triple stars ADS 6811 and ADS 7114, one cannot certainly estimate the total energy  $E_b$  of a close pair (the variations  $\delta E_b \approx 1$ ), although marked orbital motions of the components are observed in them and the probability of its dynamical connection is

$P > 0.85$ . One must verify the space velocities of the close stars in these systems;

5) the certainly physical triple stars ADS 6175 ( $r = 14$  pc) and ADS 9909 ( $r = 22$  pc) are dynamically non-hierarchical unstable triple systems with a probability  $P > 0.80$  in spite of an apparent high hierarchy of their configurations: ADS 6175 —  $\beta = \rho_{AC}/\rho_{AB} \approx 12$ , ADS 9909 —  $\beta \approx 6$ . In the triple star ADS 1630 ( $r = 80$  pc) one can make no certain conclusion on a type of dynamics because of the large uncertainties in the space velocity of the distant component A with respect to the close pair BC.

## 11. A STUDY OF DYNAMICAL EVOLUTION OF TRIPLE STAR ADS 9909 ( $\zeta$ Sco)

The data from Table 9 show that the study of dynamical states of triple star systems has given the certain results at least for two triple stars ADS 6175 and ADS 9909.

A study of dynamical evolution for the second system was carried out in detail.

The triple star ADS 9909 has the following observational parameters: the precise coordinates for the epoch 1950.0 —  $\alpha = 16^h 01^m 36^s.889$ ,  $\delta = -11^\circ 14' 12''.27$ ; the primary component A with an apparent magnitude  $m_A = 4^m 16$  has a close companion B with  $m_B = 5^m 2$  at the angular separation  $\rho_{AB} = 1''.30$  and also a more distant companion C with  $m_C = 7^m 36$  at the angular separation  $\rho_{AC} = 7''.43$ ; the spectral type of the pair AB is F 5-8 IV-V and the one of C is G 7-8 V.

One has a vector of observational data at the epoch  $T_0 = 1920.5$  for this system

$$\vec{X} = \rho_{AB}; \rho_{AC}; \theta_{AB}; \theta_{AC}; (\Delta\mu_a)_{AB}; (\Delta\mu_\delta)_{AB}; (\Delta\mu_a)_{AC}; (\Delta\mu_\delta)_{AC}; V_{A,B,C}; \pi_{A,B,C}; \quad (20)$$

$$M_{A,B,C} = 1^{\circ}30, 7^{\circ}43, 9^{\circ}0, 60^{\circ}2, \\ (0.044, 0.035, 0.009, -0.009)'' \text{ per year}; \\ (-33.6, -33.6, -33.8) \text{ km/s}; 0^{\circ}044; (1.60, 1.20, \\ 0.80) M_{\odot}$$

and a vector of the uncertainties for these data

$$\vec{\delta x} = \delta \rho_{AB}; \delta \rho_{AC}; \delta \theta_{AB}; \delta \theta_{AC}; (\delta \Delta \mu_{\alpha})_{AB}; (\delta \Delta \mu_{\alpha})_{AC}; \\ (\delta \Delta \mu_{\delta})_{AC}; (\delta \Delta \mu_{\delta})_{AC}; \delta(v)_{A,B,C}; \delta(\pi)_{A,B,C}; (21) \\ \delta(M)_{A,B,C} = 0^{\circ}04, 0^{\circ}01, 0^{\circ}7, 0^{\circ}2; \\ (0.005, 0.001, 0.003, 0.003)'' \text{ per year}; (0.2, \\ 0.2, 0.2) \text{ km/s}, 0.002; (0.10, 0.10, 0.10) M_{\odot}$$

The configuration of triple star system ADS 9909 as well as the vectors of relative proper motions of components are in Figure 1.

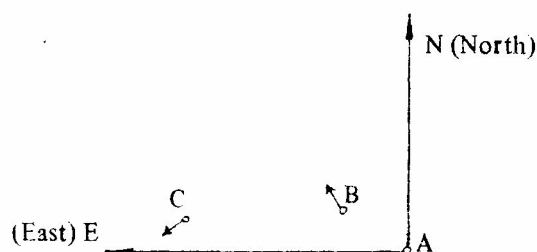


Fig. 1

The masses  $M$  of stars are calculated by the following formulae

$$\lg M = \frac{6.76 - M_{bol}}{3.85} \text{ for } M_{bol} > 7^m.5 \quad (22)$$

$$\text{and } \lg M = \frac{4.62 - M_{bol}}{10.03} \text{ for } M_{bol} < 7^m.5$$

the quantities  $M$  are expressed in the solar masses;  $M_{bol}$  is the bolometric absolute magnitude of stars to be obtained by their spectral types and luminosity classes.

The following system of units is assumed (see Anosova 1985)

$$\begin{aligned} \text{unit of distance } [r] &= 0.01 l_* \text{ pc} = 2062.65 l_* \text{ a.u.} \\ \text{unit of mass } [M] &= 2 \cdot 10^{33} \mu_* g, \\ \text{unit of time } [t] &= 10^4 k_* \text{ years,} \end{aligned} \quad (23)$$

One may assume  $l_* = \mu_* = k_* = 1$  for the multiple systems with components – the solar type stars. The unit star velocity is  $[v] = 0.9778 \text{ km/s}$ ,  $G = 0.4474$ .

In Table 9 (the third line) there are given the results of determining the dynamical state of the triple star ADS 9909 – the probabilities of dynamical connection

between components and the quantities of energetic parameters. These data show that this triple star is a certainly physically connected system with the probability  $P \approx 1$ ; its energies  $E$  and  $E_b$  are reliably obtained

$$\text{with the variations } \delta E = \left| \frac{\sigma E}{E} \right| \leq 0.2, \delta E_b = \left| \frac{\sigma E_b}{E_b} \right| \leq 0.2.$$

Therefore, one can solve the problem of determining its dynamics type stable or unstable (see item IX and Anosova 1985, Anosova and Orlov 1985, Anosova 1986).

In order to solve this problem one may again use the method of statistical tests proposed above for 50 runs varying the observational data (20) of their doubled errors assuming the Gaussian distribution of these uncertainties. One calculates the means, and rms deviations of the basic dynamical parameters (see Anosova 1985, Anosova and Orlov 1985, Anosova 1986) at an initial time moment  $T_0$ .

The following initial data have been obtained as a result of the tests carried out – the coordinates and velocities of the components are in the baricentric coordinate system the masses of the bodies are relative

$$\begin{aligned} x_1 &= -0.0162, & x_2 &= -0.0017, & x_3 &= 0.0356 \\ &\pm 0.0007 & &\pm 0.0014 & &\pm 0.0021 \\ y_1 &= 0.0139, & y_2 &= -0.0139, & y_3 &= -0.0501 \\ &\pm 0.0016 & &\pm 0.0016 & &\pm 0.0033 \\ z_1 &= 0, & z_2 &= 0, & z_3 &= 0 \\ \dot{x}_1 &= -1.37, & \dot{x}_2 &= 3.20, & \dot{x}_3 &= -2.15 \\ &\pm 0.19 & &\pm 0.21 & &\pm 0.31 \\ \dot{y}_1 &= 1.64, & \dot{y}_2 &= -2.47, & \dot{y}_3 &= 0.47 \\ &\pm 0.24 & &\pm 0.45 & &\pm 0.30 \\ \dot{z}_1 &= 0.02, & \dot{z}_2 &= -0.02, & \dot{z}_3 &= 0.09 \\ &\pm 1.32 & &\pm 1.66 & &\pm 1.38 \\ M_1 &= 1.0, & M_2 &= 0.76, & M_3 &= 0.49 \\ & & &\pm 0.08 & &\pm 0.07 \end{aligned}$$

where the indexes 1,2,3 correspond to the components A,B,C, respectively.

The main dynamical parameters of the triple star ADS 9909 have the following values at an initial time moment  $T_0 = 1920.5$ :

$$\begin{aligned} \text{mean dimension } d &= (32 \pm 2) \text{ a.u.,} \\ \text{mean crossing time } \tau &= (2.7 \pm 3) \text{ years,} \\ \text{total energy } E &= (-53.2 \pm 8.6) - \text{energy units in the} \\ &\text{system of units (23);} \\ \text{total energy of the close binary } E_b &= (-44.3 \pm 7.5) - \\ &\text{energy units;} \\ \text{virial coefficient } k_0 &= \frac{T_0^*}{U_0} = (0.28 \pm 0.01) \text{ where} \end{aligned}$$

$T_0^*$  and  $U_0$  are the kinetic and potential energies of the system at  $t = T_0$ ; an angular momentum  $L = (0.11 \pm 0.02)$  units of angular momentum; the dynamical elements of the inner pair (AB) orbit: major semi-axis  $a_{in} = (19.5 \pm 0.4) \text{ a.u.}$ , eccentricity  $e = (0.78 \pm 0.02)$ , period

$P_{in} = (54 \pm 1)$  years; the dynamical elements for the external pair AB—C:  $a_{ex} = (170 \pm 50)$  a.u.,  $e_{ex} = (0.71 \pm 0.21)$ ,  $P_{ex} = (1.2 \pm 0.2) \cdot 10^3$  years; coefficient of sta-

bility  $s = \frac{a_{ex}(1 - e_{ex})}{a_{in}} = (2.3 \pm 0.9)$ , its critical

quantity  $s^* = 3.5$  (if  $s > s^*$  a triple system must be stable — according to Harringtons 1972) criterion.

The probability that the triple system ADS 9909 is stable is equal  $P_s = 0.05$ , the probability of instability is  $P_{is} = 0.95$ .

In connection with the conclusion that ADS 9909 has the unstable type II of dynamics one may study the dynamical evolution of this system by computer simulations (see Anosova 1985, 1986, Anosova and Orlov 1985). A corresponding study carried out from  $T_0 = 1920.5$  has given the following results: a lower limit of escape time is  $t_e = (1.2 \pm 0.3) \cdot 10^3$  years (in 38% of the cases under consideration, the system did not disrupt during a time  $t = 100 \tau = 3 \cdot 10^3$  years); one has observed during the evolution  $n = 4.3 \pm 2.6$  of triple approaches of bodies which have a perimeter  $p = \sum_{i \neq j} r_{ij} \leq 100$  a.u. where  $r_{ij}$  is the distances between two components;

a triple approach causing an escape has the perimeter  $p = (56 \pm 18)$  a.u.; a final binary AB (after the escape of component C) has a semiaxis major  $a_f = (5.1 \pm 1.6)$  a.u., an eccentricity  $e_f = 0.70 \pm 0.27$ , and a period  $P_f = (23 \pm 7)$  years; a value of  $\cos \chi = 0.95 \pm 0.05$  where  $\chi$  is an inclination of the orbit of the escaper C to the orbit of the final binary AB — both orbits are approximately co-planar (as at the initial time moment T); the inclination of the velocity vector of the escaper C to the angular momentum vector of the triple system is given by  $\cos \gamma = 0.017 \pm 0.011$ ; the final value of the virial coefficient is  $k = 0.43 \pm 0.16$  at the end of evolution (after escape of component C  $\gamma$  — the system is near an equilibrium state; an excess of the energy taken away by the component C is equal to  $DE = 0.14 \pm 0.80$  — an excess of the kinetic energy of escaper over the one necessary for an escape of triple system according to the criterion of G.A. Tevzadze (see 1962).

Thus, the study of the dynamical state and dynamical evolution of the triple star ADS 9909 ( $\gamma$  Sco) carried out here has shown that this system is certainly a physical one and it has probably the unstable type II dynamics. The quantitative results obtained on the basis

Table 10

## Individual contribution of uncertainties of the observational data

| Parameter             | Uncertainty                                  | $\pi = 0^{\circ}070$ |                                            | $\pi = 0^{\circ}010$ |                                            |
|-----------------------|----------------------------------------------|----------------------|--------------------------------------------|----------------------|--------------------------------------------|
| $x_1$                 | $\delta x_1$                                 | $x_1$                | $\delta E$                                 | $x_1$                | $\delta E$                                 |
| $\pi''$               | $\pm 0.005$<br>0.002                         | 0.070                | 0.05<br>0.04                               | 0.010                | 0.45<br>0.20                               |
| $(\mu_{AB})''/y$      | $\pm 0.005$ — 0.026, + 0.006<br>0.0005       |                      | 0.02<br>0.00                               | —0.0022, 0.003       | 0.25<br>0.03                               |
| $\mu_{AB}(\mu_0)$     | $\pm 0.5$<br>0.2                             | 0.6                  | 0.25<br>0.10                               | 0.4                  | 0.10<br>0.04                               |
| $\mu_c''/s$           | $\pm 0.005$<br>0.0005                        | 0.048, — 0.037       | 0.05<br>0.01                               | 0.002, 0.002         | 0.08<br>0.01                               |
| $V_{AB}$ km/s         | $\pm 1.0$<br>0.3                             | — 7.2                | 0.03<br>0.01                               | 3.4                  | 0.08<br>0.02                               |
| $V_c$ km/s            | $\pm 1.0$<br>0.3                             | 3.2                  | 0.02<br>0.01                               | 1.6                  | 0.06<br>0.02                               |
| $\rho_{AB}''$         | $\pm 0.1$<br>0.005                           | 6.25                 | 0.02<br>0.00                               | 7.58                 | 0.02<br>0.00                               |
| $M_c(M_0)$            | $\pm 0.5$<br>0.2                             | 2.2                  | 0.02<br>0.01                               | 2.1                  | 0.01<br>0.00                               |
| $\rho_{AC}''$         | $\pm 0.1$<br>0.005                           | 73.41                | $0.1 \cdot 10^{-3}$<br>$0.5 \cdot 10^{-5}$ | 57.64                | $0.3 \cdot 10^{-2}$<br>$0.2 \cdot 10^{-5}$ |
| Integral contribution | $(\delta x_1)_{obs}$<br>$(\delta x_1)_{min}$ |                      | 0.27<br>0.10                               |                      | 0.50<br>0.25                               |



of observational data have given a large dispersion in values of the evolutionary parameters; in order to obtain more certain results one should improve the accuracy of the observational data.

## 12. THE NECESSARY ACCURACY LEVEL OF THE OBSERVATIONAL DATA

The method proposed in order to take into account the uncertainties in the observational data for the multiple star components allows to estimate the individual contributions from the uncertainties of every characteristics observed and to evaluate the accuracy level necessary for solving the problem produced – revealing the dynamical states of objects under study.

In the present work, such a study has been carried out for two triple stars  $\alpha$  Gem (Castor) – ADS 6175 and ADS 2926 whose parallaxes are equal to 0".070 and 0".010 respectively.

The results are given in Table 10. In the first column of this Table there are the observed data  $x_1$ ; in the second column there are their uncertainties  $\delta x_1$  obtained from the observations (the upper lines and the values  $(\delta x_1)_{\min}$  corresponding to the maximum accuracy level reached at present by the systematically planned observations (the lower lines) – see Kiselev and Kiyeva 1980, Anosova 1984, Anosova and Orlov 1985, Dommanget 1985, Anosova 1986, Anosova and Sudakov 1987, Anosova et al. 1987.

The conditions of reaching such an accuracy level in the observational data for the components of triple stars will be given below. In the following columns of Table 10 there are the values of the observed characteristics  $x_1$  and the variations  $\delta E = \left| \frac{\sigma_E}{E} \right| = \left| \frac{E(x+\delta x) - E(x)}{E(x)} \right|$  of a relative change of the total energy for the systems ADS 2926 and ADS 6175 under consideration.

The study carried out has given the following results: 1) the variations of energy are  $\delta E \sim \kappa \delta x$ ,  $\kappa = \text{const}$  for all values  $x_1$ ; 2) the main contribution in  $\delta E$  for rather distant triple stars is given by the uncertainties in the parallaxes being a growth of  $\delta E$  with a decrease of  $\pi$  (Table 11).

Table 11

Dependence  $\delta\pi$  on  $\pi$

| $\pi$  | $\delta\pi = \pm 0''.005$ | $\delta\pi = \pm 0''.002$ |
|--------|---------------------------|---------------------------|
| 0".070 | 0.08                      | 0.03                      |
| 0.040  | 0.20                      | 0.08                      |
| 0.020  | 0.50                      | 0.20                      |
| 0.010  | —                         | 0.40                      |

3) therefore, a reliable study of dynamics for the triple stars with  $\delta\pi = \pm 0''.005$  is possible only for  $\pi \geq$

0".020 (the probability of dynamical connection between components  $P(E - 2\sigma_E \leq 0) \sim 1$  on  $\delta E \leq 0.50$  and  $E < 0$ ); in the opposite case, the sign of the total energy and, therefore, the probability of dynamical connection is not determined. The study of triple stars with  $\pi \geq 0''.010$  is possible for  $\delta\pi = \pm 0''.002$  (see Dommanget 1985);

4) taking into account the sizes  $\Delta z$  of triples along the line-of sight for  $\delta\pi = \pm 0''.005$  a reliable study is possible only for the triple star  $\alpha$  Cen (Table 12) supposing  $\Delta z = 0.01$  pc – a mean size of triple systems whose components are solar-type stars. Some attempts of analogous study for the triple star ADS 3093 are possible for  $\delta\pi = \pm 0''.001 - 0''.002$  (using the observations by the cosmic observatories – see Dommanget 1985). Taking into account the sizes along the line-of-sight for more distant systems a reliable study is possible only statistically.

Table 12

| $\Delta\pi''$<br>( $\Delta z = 0.01$ pc) | $\pi''$           | triple system |
|------------------------------------------|-------------------|---------------|
| $\pm 0.010$                              | $0.756 \pm 0.003$ | $\alpha$ Cen  |
| 0.001                                    | $0.202 \pm 0.006$ | ADS 3093      |
| 0.0002                                   | $0.074 \pm 0.001$ | $\alpha$ Gem  |

In order to take into account the sizes of systems along the line-of-sight by statistics one must obtain the relative distances  $R_{ij}$  between the components  $i$  and  $j$  with the angular separation  $\rho_{ij}$  and positional angle  $\theta_{ij}$  according to the formula

$$R_{ij} = \frac{4}{\pi} \rho_{ij}$$

where  $\rho_{ij} = R_{ij} \cos \omega$ ,  $\omega$  is the angle between the vectors  $R_{ij}$  and  $\rho_{ij}$ ,

$$\rho_{ij} = \frac{1}{4} \int_0^{2\pi} \int_{-\pi/2}^{\pi/2} R_{ij} \cos^2 \omega d\theta_{ij} d\omega = \frac{\pi}{4} R_{ij}$$

(according to Kleiber's theorem) assuming an equal distribution of angles  $\omega$  and  $\theta_{ij}$  within the intervals  $[-\pi/2, \pi/2]$  and  $[0, 2\pi]$ ;

5) for the hierarchical triple stars, taking into account of observed parameters for a close pair (at first, the relative masses of components, then, their relative proper motions) plays a great role;

6) the smallest contribution in the variations  $\delta E$  of multiple systems is made by the uncertainties in the relative coordinates.

The necessary accuracy level of observations might be reached on the following conditions:

a) for the astrometrical observations an accuracy  $\delta\rho = \pm 0''.005$  and  $\delta\mu = \pm 0''.0005$  per year ( $\rho, \mu$  are the relative coordinates and proper motions of components) may be achieved on  $\rho > 3''$  by the dense series of ob-

servations at the long-focus refractors during 10–15 years (Kiselev and Kiyaeva 1980); for the systems containing the close pairs with  $\rho < 2''$ , one must carry out the speckle interferometry observations;

b) the uncertainties of the radial velocities  $\delta_v = \pm 0.1\text{--}0.5$  km/s are reached by the spectroscopic observations using the equipment of CORAVEL's type (Anosova et al. 1987);

c) one may obtain the uncertainties  $\delta_M = \pm 0.2 M_\odot$  of star masses using the differences of their apparent magnitudes (data from the photoelectric photometry) in the nearby triple systems with the well-known trigonometric parallaxes for every component provided that any peculiarity in their spectra is absent.

d) an accuracy level  $\delta_\pi = \pm 0.002$  of the stellar parallaxes is proposed to be reached by the observations on board of the European astrometric satellite HIPPARCOS;

e) an essential increase in the accuracy of astrophysical and astrometrical data ( $\delta_\mu, \delta_\pi = \pm 0.0003$ ) will be reached by the observations on board of the HUBBLE SPACE TELESCOPE.

A program of the Leningrad University Observatory consisting of 137 nearby and bright multiple stars and made with a purpose to study their dynamical states has been included in the HIPPARCOS Input Catalogue (in part, in accordance with the technical possibilities) and submitted to the HUBBLE SPACE TELESCOPE Science Institute.

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## ТРАГАЊЕ И КЛАСИФИКАЦИЈА ВИШЕСТРУКИХ СИСТЕМА У ОПШТЕМ ПОЉУ

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УДК 523.83

Оригинални научни рад

Предмет овог рада је проучавање вишеструких звезда и галаксија са циљем да се класификују њихова динамичка стања и да се пронађу статистички критеријуми за разликовање случајних група објеката од неслучајних. Предложени статистички критеријум је

примењен на неке вишеструке звезде и галаксије. Разрађен је одговарајући алгоритам и на крају су проучена динамичка стања тројног система ADS 9909 (Sco) узимајући у обзир грешке посматрачких података.

## AN APPROACH TO THE PROBLEM OF SECULAR ACCELERATION OF THE MOON

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**SUMMARY:** If we adopt the solution of extended method in the Delaunay theory of the Moon as real and entirely logical and substitute the square term in the Moon's mean longitude by the very long period inequality, the remaining residuals – fluctuations – can be treated as the consequence of collected effect of a few other inequalities. The frequencies of these periodical terms correspond to the identical relative positions of the Moon's node, Sun and Earth.

On the basis of such an approach to the problem of secular acceleration of the Moon and fluctuations, lunar observations in the period 1681 – 1985 are analysed.

The results are quite consistent with values presented by other authors.

### 1. INTRODUCTION

The secular quadratic term was introduced in the expression for the Moon's longitude on the basis of Halley's conclusion that the mean lunar motion was not constant (Halley, 1695). The term had an empirical character and from the very beginning there have been great difficulties in attempts of establishing its real amount and finding an acceptable theoretical explanation. Unfortunately, in spite of the efforts of many investigators during almost three whole centuries, we cannot claim that in this field significant progress has been achieved.

Even the theory of nonuniformity in the Earth's rotation based on the lunar tidal effect, contrary to expectations, has failed in giving a complete explanation of the difference between the lunar secular acceleration derived theoretically and the values resulting from observations. Brumberg and Kovalevsky (1986), and especially Seidelmann (1986), certainly for this reason put this problem among the unsolved problems of Celestial Mechanics since it is doubtlessly important

also from the point of view of the Earth–Moon's stability system.

However, if one thinks about the reasons why the final solution of the problem is still uncertain, it is not difficult to suppose that this situation may be the consequence of assuming a priori the notion of the secular acceleration in the mean lunar motion as an evident fact and of accepting the existing formal theoretical explanation as a proof for its real existence. But such a concept certainly includes a quite different approach to the problem and a subsequent analytical solution, more adequate for the explanation of the phenomenon.

### 2. MEAN LONGITUDE OF THE MOON

Supposing that such a line of reasoning is correct and justified, it is of interest to envisage what kind of result can be obtained if the residuals found in the lunar longitude are expressed as a collective effect of several long-period inequalities; in other words, if an alter-

native assumption is introduced. The alternation possibility was also mentioned by Newcomb in his „Researches“ (Newcomb, 1878), in addition to the hypothesis of nonuniformity in the Earth's rotation. However, we do not limit ourselves in this procedure to pure fluctuations alone, but we also take into account the secular quadratic term completely. A sufficiently reliable basis to such an approach is the already known analytical solutions of the differential equations of mass-point motion through the procedure applied in Delaunay's theory of the Moon. Solutions of this kind have been the subjects of many studies and cases of their application in Celestial Mechanics become more numerous today (e. g. the problem of motion near the libration points, the problem of central motion of an unlimited number of massive bodies, etc). The use of modern methods adapted to software application aimed at finding such solutions also contributes to this.

Without going into details, it will be enough to write down only the solution defining the mean longitude analytically:

$$L = L_0 + n \cdot t + \sum_{i=1}^n A_i \sin(a_i \cdot t + \beta_i) \quad (1)$$

mentioning that analogous relations are obtainable also for the cases of  $\bar{\omega}$  and  $\bar{\Omega}$  (pericentre longitude and node of an orbit) and that in the expressions yielding  $a$ ,  $e$ ,  $i$  (semi-major axis, eccentricity and inclination) there is no secular linear term. As for the parameters  $L_0$ ,  $n$ ,  $A_i$ ,  $a_i$ ,  $\beta_i$ , the best way is their determination from direct observations since according to the existing experience only then one can avoid the differences appearing usually between their real values and the theoretically derived ones.

As seen, there are no quadratic and mixed terms in which  $t$  is before the sign  $\Sigma$ , here. This means that such solutions are in accordance with the oscillatory nature of central motions of celestial bodies being essentially true, but in macrodimensions. In addition they are not contradictory to Kepler's laws and the stability of a system is not violated, in particular of the Earth-Moon system.

It should be mentioned that Brown's theory of the Moon is practically also based on solutions of this kind, though the classical definition and the presentation of secular inequalities as a series are preserved in it:

$$P_1 \cdot t + P_2 \cdot t^2 + \dots$$

In this way Brown, like Hansen and Newcomb before him, had no choice but to introduce also an empirical long-period term in the longitude expression. For residual deviations, the minor fluctuations as they were named by Newcomb, had been looked for and various solutions were found until de Sitter (1927) and later on, Spencer Jones (1939) proposed their solutions in which the fluctuations were interpreted

as a set containing the difference between the observational and theoretical secular acceleration value and the minor fluctuations. The consequences of such an approach are well known.

### 3. OBSERVATIONAL DATA ANALYSIS AND RESULTS

By reducing the discrepancies (O-C) in the Moon's mean longitude to the quasi-keplerian motion, taking also into account the total amount of the secular acceleration, M. Protitch (1987) attempted their explanation following the conclusions mentioned above. In this way, he demonstrated after the revision and analysis of Newcomb's results from 1878 and 1917, firstly in Hansen's system and afterwards by reducing to Brown's system, that all ancient, Babylonian-Hellenic-Arabian, and later (by the end of 17th century) eclipses of the Moon can be well represented by substituting the quadratic term with an inequality of a very long period. He also established that as a consequence of such an interpretation a periodical character in the fluctuations is clearly seen and that their frequencies are correlated with cycles whose durations are determined by the time needed for the restitution of the same, or nearly the same, relative positions of the Sun, the Earth, the node and the perigee of the lunar orbit.

The plots presented here (Fig. 1, a, b) display the trend of the residuals in Hansen's system before and after the elimination of its secular quadratic term ( $n = +26''.68$  arc sec/cy<sup>2</sup> epoch 1900.0). One should add that the parameters of this inequality are derived in a way similar to Newcomb's one (Newcomb, 1917) but omitting his correction to the secular acceleration.

These results gave us an impetus to carry out a verification of such an approach to the problem based on an analysis of later lunar observations (from the period 1681-1985) not considered by him and to establish whether an alternative concept of the secular acceleration, phenomenologically and according to what contains very different from the present one, is justified or not.

The data used by us for this purpose are taken from Brouwer's (1952) thorough study. On the basis of his values B, which are fluctuations in the Moon's mean longitude, by applying a corresponding correction G and also the long-period Venus term A, accepted from Hansen's theory, we obtain the residuals with respect to the quasi-keplerian motion. With regard to (1) we should have:

$$\delta L_k = (O-C)_k = \delta L_0 + \delta n \cdot t + \sum_{i=1}^n C_i \sin(a_i \cdot t + \beta_i) = B + G + A \quad (2)$$

where:  $\delta L_0$  and  $\delta n$  are the longitude corrections for the epoch and for the mean diurnal motion,  $C_i$ ,  $a_i$  and  $\beta_i$

are the parameters of the assumed inequalities which should be determined, B are Brouwer's fluctuation values derived from occultations, G and A are the corrections of the form:

$$G = 4''.65 + 12''.96T + 12''.36T^2 + A$$

$$A = +14''.27 \sin(131''.92T + 344''.82)$$

(T from 1900.0 in Julian centuries).

One should say that the values B do not contain Brown's great empirical term and that the quadratic term in G is the tropic value of the secular acceleration derived from observations (theoretical value + de Sitter's correction  $7''.14T + 5''.22T^2$ ) also assumed by Spencer Jones (1939).

In Brouwer's series there are data by 1948.5 only. Therefore, to obtain the further data (by 1985) we use the published values of  $\Delta T$  according to Clemence's (1948) definition:

$$B'' = 0''.5491 \cdot T - 13''.77 - 39''.71 \cdot T - 16''.44T^2$$

where T is in time seconds.

Though inhomogeneous the material prepared in this way gave nevertheless a sufficiently reliable base for solving the problem. The data from the period 1920–1950 are treated by use of the third-degree-five-points-least-square-smoothing procedure.

The main problem which should be solved requires a number of periodical terms, which can be important, to be known. One of them is found immediately: we assume the long-period inequality having been the substitution for the secular quadratic term in an earlier paper (Protitch, 1987). In addition, it is a part of global fluctuations so that finding a real solution for its residual part would be at the same time a confirmation to its reality.

The numerical value of this inequality derived from observations covering an interval greater than 24 centuries is:  $+2369''.9 \cdot \cos(6''.883T + 270''.33)$ . Its period is 5230 tropic years, or 64686 synodic, 69325 anomalistic and 70197 draconistic lunar revolutions. The amplitude is, as seen, identical to the variation amplitude. The introducing of it implies a mean longitude correction for 1900.0 of:  $\delta L_0 = -14''.07$  and a reduction in the annual mean motion of  $\delta n = -2''.9316$ . By omitting this term denoted as  $\delta L_1$  one would obtain the fluctuation amount with respect to the quasi-keplerian motion:

$$B_k = \delta L - \delta L_1 = \Delta \delta L \quad (3)$$

which should be represented through the corresponding long-period functions.

In our analysis we just interpret  $\Delta \delta L$  and on the basis of the smoothed curve for the interval 1695–1985.

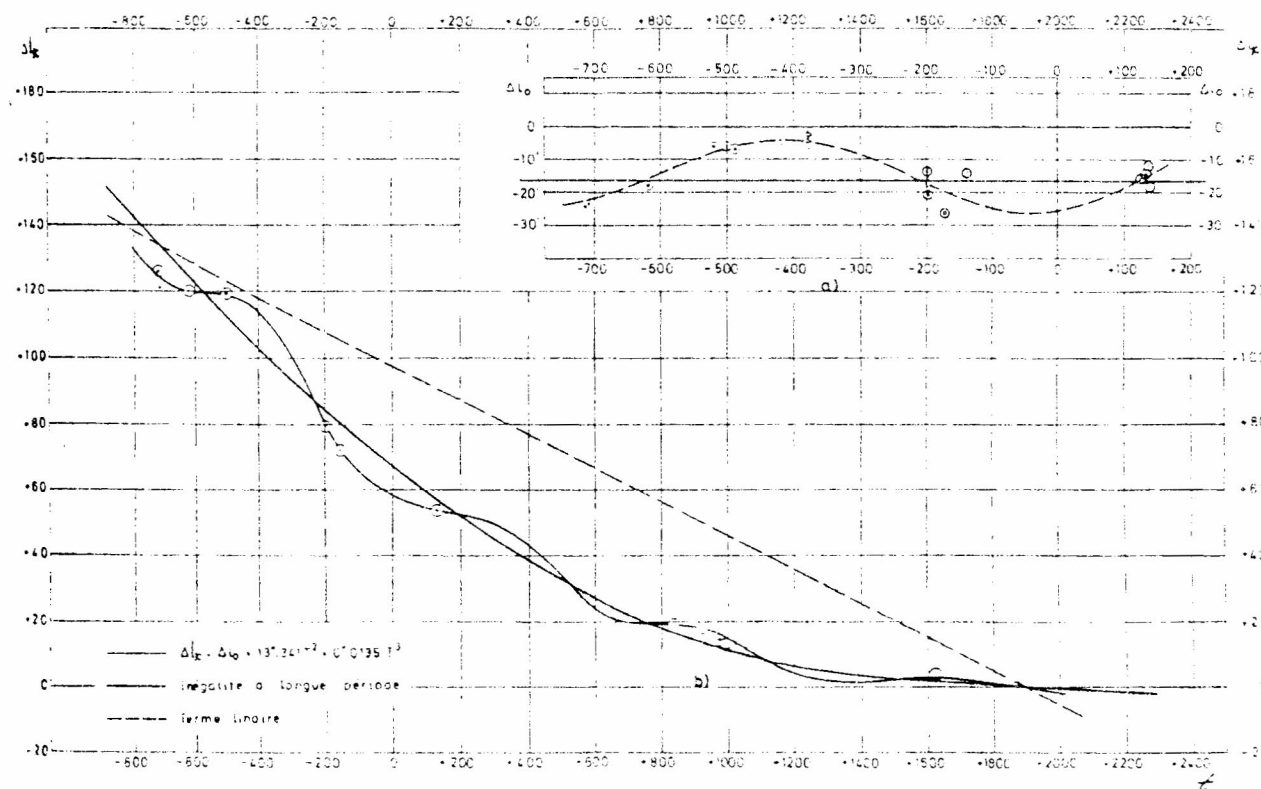


Figure 1. The trend of residuals in the mean longitude of the Moon (Hansen); a -- secular quadratic term included, b -- in the quasi-keplerian system secular quadratic term eliminated.



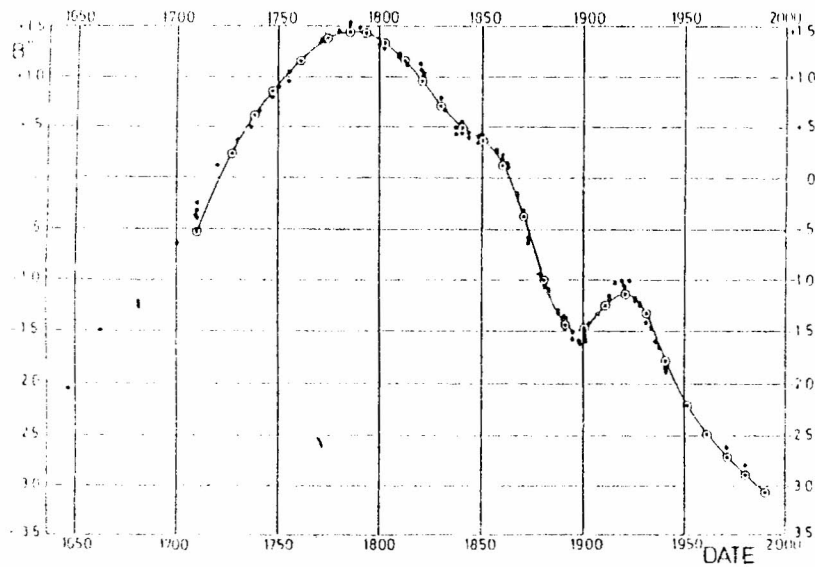


Figure 2. Fluctuations in the Moon's mean longitude. The dots represent observed values used by various authors (De Sitter, Sp. Jones, Brouwer, Morrison) and the full line represents the calculated values (Protitch).

in which a periodical character is clearly seen, we choose twenty equidistant values.

By applying the classical procedure of determining the parameters of a periodical function and assuming  $i = 4$  we determine  $C_i, a_i, \beta_i$ . The obtained periods indicate their similarity to the commensurability periods for longitudes of the Sun, the Moon's node and the Earth and therefore they are reduced to the latter ones. However, the inspection of the residuals reveals the presence of at least two additional periodical terms. Repeating the procedure we find the periods for which the following rounded values are assumed: 46.5 and 74.5 years. These periods appear to be commensurable with the length of the eclipse year and begin at the times when the lunar nodes and the Sun are in the same point of ecliptic. An insight into Oppolzer's (1887) Canon or Meeuse-Mucke's (1983) Canon is in favour of their reality.

Without insisting upon a high precision in deriving the parameters  $C_i$  and  $\beta_i$  assuming that the seven long-period inequalities can be substituted as the input data with a sufficient accuracy (within +1 arc second) we determine the values  $(B_0)_C$  by applying the inverse procedure. Their trend is presented in Fig. 2 together with the values used by other authors. True, as far as we know, Stoyko (1967) and Pejcev (1986) mentioned in their papers concerning the nonuniformity in the Earth's rotation that in this the longitude of the node of the lunar orbit and the Moon's relative position with respect to the Sun have some part, but without answering the question completely. If we wanted to use our results concerning this matter, we would establish that the correction  $\Delta T$  has a tendency of further increase.

#### 4. CONCLUSION

We are fully aware of criticisms which can be addressed to such an attempt of explaining the fluctuations in the mean lunar longitude and also the ones in its secular acceleration. It is well known that many authors before us (Cowell, Brown, Radau, Ross, etc) have tried and found in a similar way various long-period terms, but without attempting to look for any explanation of their nature. Examples are the long-period empirical terms introduced by Newcomb, Brown, Fotheringham and others. Similar analyses and attempts to express the trend of the corrections  $\Delta T$  through periodical functions and consequently to determine the values for the near future by means of extrapolation, as done for example by Cholić (1989), are becoming more and more frequent nowadays.

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СЕКУЛАРНО УБРЗАЊЕ У СРЕДЊОЈ ЛОНГИТУДИ МЕСЕЦА: МОГУЋЕ ОБЈАШЊЕЊЕ

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*Оригинални научни рад*

Ако се прихвате као реална и сасвим логична решења добивена генерализацијом метода примењеног у Delaunay-евој теорији Месеца, па уместо секуларног квадратног члана у његовој средњој лонгитуди уведе дугопериодична неједнакост, преостали резидуи  $(O-C)$  — флукуације — могу се објаснити као последица сумарног ефекта суперпоновања неколико других неједнакости, различитог трајања и амплитуда. Фреквенце

тих неједнакости сразмерне су интервалима времена који деле тренутке наступања идентичних, или квази-идентичних релативних положаја чвора Месечеве путање, Земље и Сунца.

У овом раду приказани су резултати до којих се долази анализом података посматрања из периода 1681–1985. Тако изведене флукуације добро се слажу са вредностима које су дали други аутори.

A CONSIDERATION OF VELOCITY DISTRIBUTION WITHIN  
CORONAE OF GALAXIES

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**SUMMARY:** Coronae of galaxies are assumed to be spherically symmetric, self-consistent and in a steady state. The velocity distribution is studied on the basis of the hydrodynamical equation through the ratio  $\overline{v_t^2}/\overline{v_r^2}$  (transversal and radial velocity components, respectively). It is found that in the conditions supposed to occur in real galaxies the radial velocities prevail so that the fraction of the radial velocity in the total kinetic energy of the system attains even more than 50%. Applied to our Galaxy the results of the present paper suggest a value of the ratio mentioned above of a little bit greater than one at the galactocentric position of the Sun.

## 1. INTRODUCTION

It is well known that for the purpose of explaining some phenomena in stellar astronomy (rotation curves of spiral galaxies, etc) a concept of galactic coronae—vast, very massive systems, dominating the dynamics of their galaxies—has been developed (e. g. Trimble, 1987). Because of sufficiently flat rotation curves an inverse-square law has been usually assumed for the mass distribution within the coronae. Since the coronal constituents are unknown, there is no observational evidence on their velocity distribution. However, as well known, in the most simple case when spherically symmetric coronae are considered, the inverse-square law can be obtained by assuming an isotropic and isothermal velocity distribution. On the other hand Antonov and Chernin (1975, also Antonov et al., 1975) argued that an isotropic and isothermal velocity distribution cannot be expected within very rarefied systems such as coronae since their relaxation time is extremely long. The two authors proposed another velocity distribution characterised by a domination of radial velocities which may have resulted from the primordial

conditions. One should point out that a pure inverse-square law is not realistic for two reasons:

- i) it yields a singularity in the central density;
- ii) integrated over infinity it yields an infinite total mass. To avoid the second disadvantage one can assume that the inverse-square law is valid only within a finite radius. However, in this case we have a discontinuity at the boundary of the system since at the inner side of the boundary the density is greater than zero and at the outer one it vanishes.

The purpose of the present paper is to introduce more realistic conditions for the density function and then to consider the velocity distribution under these conditions.

## 2. THEORETICAL BASE

For reasons of simplicity it is here assumed that the corona of a galaxy is a self-consistent system. In such a case the most simple decision is to assume also the spherical symmetry and the steady state. In reality the coronae co-exist with discs of their galaxies so that

strictly speaking they cannot preserve the spherical symmetry which they might have if they existed separately.

These two assumptions mean that the Poisson equation and the hydrodynamical one (e. g. Ogorodnikov, 1958) are valid. The latter equation will be written here because in the present paper it is widely used

$$\overline{v_t^2} = u_c^2 + \frac{r}{\rho} \frac{d\rho}{dr} \overline{v_t^2} + 2\overline{v_r^2} + r \frac{d\overline{v_r^2}}{dr} \quad (1)$$

In equ. (1) the following designations are used:  $\overline{v_t^2}$ —the mean square of transversal velocity at a given radius  $r$ ,  $\overline{v_r^2}$ —the mean square of radial velocity,  $u_c$ —the circular velocity and  $\rho$  the density.

It can be proved that at the centre ( $r=0$ ) is valid  $\overline{v_t^2} = 2\overline{v_r^2}$  provided that the density function is realistic, i. e. being decreasing, finite at the centre, almost constant near it and vanishing at a certain radius  $r_1$ , so that the derivative is always negative, except at the centre where it vanishes, but near it its absolute value is very small. The proof easily follows from (1) since under such conditions must be  $u_c(0) = 0$ . Therefore, it is clear why in different families of models describing the spherically symmetric and self-consistent systems in a steady state the velocity distribution is isotropic at the centre (Binney and Tremaine, 1987, p. 242).

Beyond the centre the velocity distribution of a spherically symmetric system is generally anisotropic because in such systems it depends on two integrals of motion—the energy and the modulus of the angular momentum. Imposing a realistic condition on  $\overline{v_r^2}$ , i. e. introducing it as

$$\overline{v_r^2} = \overline{v_r^2}(0) f(r), \quad (2)$$

where  $f(r)$  is a monotonously decreasing function so that

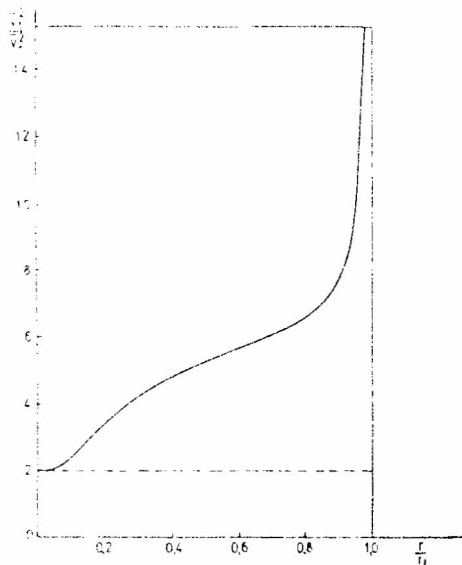


Figure 1 An example of „transversal” velocity distribution;  $r_c/r_1 = 0.1$ ,  $\overline{v_r^2}(0) = 0.15 \times 4\pi G A r_c^2$

$f(0) = 1$  and  $f(r_1) = 0$ , one finds that with respect to the ratio  $\overline{v_t^2}/\overline{v_r^2}$  one can define two kinds of velocity distributions for a given mass distribution. These are:

i) the „transversal” anisotropic —  $\overline{v_t^2} \geq 2\overline{v_r^2}$  (the equality corresponds to  $r = 0$ , see Fig. 1);

ii) the „radial” anisotropic where within some part  $re(0, r_a)$  is  $\overline{v_t^2} < 2\overline{v_r^2}$  and beyond that interval,

$r > r_a$ ,  $\overline{v_t^2} > 2\overline{v_r^2}$  (Fig. 2). Since all the objects belonging to a corona are within their potential wells, the central value of the radial-velocity square,  $\overline{v_r^2}(0)$ , must satisfy the condition  $\overline{v_r^2}(0) < (2/3)\Pi(0)$ , where  $\Pi$  is the potential of the system.

The form of the function describing the mass distribution within the corona of a galaxy in the present paper is the same as that in an earlier paper of the present author (Ninković, 1988). The corresponding solution of the Poisson equation was also given there. The task is to specify possible constraints on the velocity distribution for these conditions using equation (1).

### 3. PROCEDURE

Since in equ. (1) there are only two physical quantities — the distance and the velocity square — their units should be specified. The distance unit will be  $r_1$  (limiting radius) and the velocity square will be expressed in  $4\pi G A r_c^2$  ( $G$  is the gravitation constant, for the meaning of others see Ninković, 1988).

The scale parameter  $r_c$  must be specified, too. The circumstance that as a rough description of the distance dependence within a corona may be used the inverse-square law acts as a constraint to the choice of the ratio  $r_c/r_1$ . Intuitively one finds a value of 0.1 as the fair one. It agrees well with those values assumed in some models of our Galaxy (e. g. Caldwell and Ostriker, 1981; Rohlfs and Kreitschmann, 1981). With regard to the requirements concerning the function  $f(r)$  (2) it is convenient to choose expressions like  $(1-r/r_1)$ , i. e.  $(1-r^2/r_1^2)$ . The former expression raised to a power greater than 1 yields a sufficiently steep decrease in  $f(r)$  near the centre. The latter one acts as a smoothing term by enabling a more gradual decrease of  $f(r)$ . This is seen from the following examples.

In the case  $\overline{v_r^2}(0) = 1$  (units established above, equal to  $0.56\Pi(0)$ ) a solution of (1) is obtained with

$$f(r) = a_1 (1-r/r_c)^3 + a_2 (1-r/r_c)^2 + a_3 (1-r^2/r_c^2),$$

$$\sum_{i=1}^3 a_i = 1;$$

in the particular case  $a_1 = 0.09$ ,  $a_2 = 0.89$ ,  $a_3 = 0.02$ . (Fig. 3). The role of the first term is to make the decrease sufficiently steep near the centre (on the contrary one would obtain a negative  $\overline{v_t^2}$ ), the second one is the basic term (for this reason its coefficient is largest)

and the role of the third term is to diminish the increase of  $\bar{v}^2$  ( $\bar{v}^2 = \bar{v}_r^2 + \bar{v}_t^2$ ) near the boundary. For values of  $\bar{v}_r^2(0)$  as large as 1 this increase is inevitable because at  $r = r_1$  as easy to see it will be  $\bar{v}_t^2 = u_c^2 - 4a_3 \bar{v}_r^2(0)$ . Since  $\bar{v}_t^2$  cannot be negative, this is a limitation for the value of  $a_3$ . Only at  $\bar{v}_r^2(0)$  approximately as small as 0.8 ( $0.44\Pi(0)$ ) this limitation is not so strong and it is possible to obtain a function  $\bar{v}^2(r)$  always decreasing. However, as seen from Figs. 2-3 the minimum of the ratio  $\bar{v}_t^2/\bar{v}_r^2$  is much deeper in the second case (larger  $\bar{v}_r^2(0)$ ) achieving about 0.01 and occurring at about  $r = 0.55 r_1$ , whereas in the first case the value of the minimum is about 0.66 and it corresponds to the approximate value of  $r$  equal to  $0.7 r_1$ . The „critical” value of  $\bar{v}_r^2(0)$  above which is impossible to obtain a „transversal” solution of (1) (like in Fig. 1) occurs at about  $\bar{v}_r^2(0) = 0.15$  ( $0.08 \Pi(0)$ ).

The present procedure is repeated for two more cases:  $r_c/r_1 = 0.01$  and  $r_c/r_1 = 0.5$ . The latter one evidently does not correspond to the present purpose, thus it is used only as an illustrative one.

In the case  $r_c/r_1 = 0.01$  all the facts found in the former case ( $r_c/r_1 = 0.1$ ) become more strongly expressed. For example, if  $\bar{v}_r^2(0) = 2$  (about one half of  $\Pi(0)$ ) the dependence of the radial velocity square is given by

$$f(r) = a_1 (1-r/r_1)^4 + a_2 (1-r^2/r_1^2);$$

$$a_1 = 0.975, \quad a_2 = 0.025 \text{ (Fig. 4).}$$

The value of the coefficient  $a_2$  is large enough to achieve smoothing.  $\bar{v}^2(r)$  is a monotonously decreasing function. The minimum in  $\bar{v}_t^2/\bar{v}_r^2$  occurs at about  $r/r_1 = 0.26$  ( $26r_c$ ) and it is less than 0.001! A transversal solution is impossible to obtain above  $\bar{v}_r^2(0) \approx 0.2$  ( $0.06 \Pi(0)$ ).

For the case  $r_c/r_1 = 0.5$  the minima are not so deep by far and one can add that transversal solutions exist at about  $\bar{v}_r^2(0) = 0.1$  ( $0.25 \Pi(0)$ ).

Therefore, it is seen that within self-consistent coronae of galaxies velocity distributions with prominent radial motions are generally acceptable. If the arguments of cosmogony are also invoked, then distributions characterised by prominent radial motions are very probable (e. g. Jaaniste and Saar, 1975).

#### 4. DISCUSSION AND CONCLUSIONS

One could say that the general conclusions of the present paper and of that by Antonov and Chernin (1975) are similar. One should bear in mind that no quantitative comparison is possible since in the present paper a different mass distribution, with no singularity at the centre and no discontinuity at the boundary, is assumed. On account of this the ratio  $\bar{v}_t^2/\bar{v}_r^2$  is a function of distance whose values generally depend on the mass distribution unlike Antonov and Chernin who

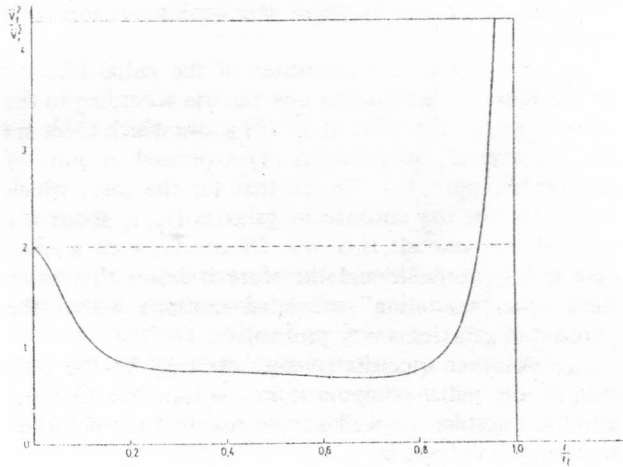


Figure 2 A „radial” solution;  $r_c/r_1 = 0.1$ ,  $\bar{v}_r^2(0) = 0.7 \times 4\pi G A r_c^2$ ,  $f(r) = 0.0571(1-r/r_1)^3 + 0.7714(1-r/r_1)^2 + 0.1714(1-r^2/r_1^2)$

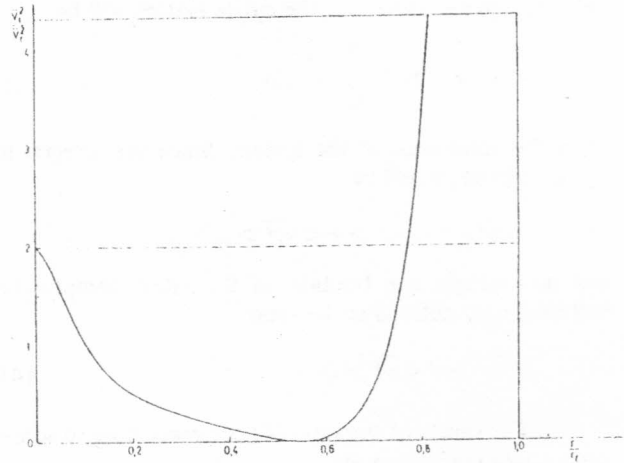


Figure 3  $r_c/r_1 = 0.1$ ,  $\bar{v}_r^2(0) = 4\pi G A r_c^2$ ,  $f(r) = 0.09(1-r/r_1)^3 + 0.89(1-r/r_1)^2 + 0.02(1-r^2/r_1^2)$

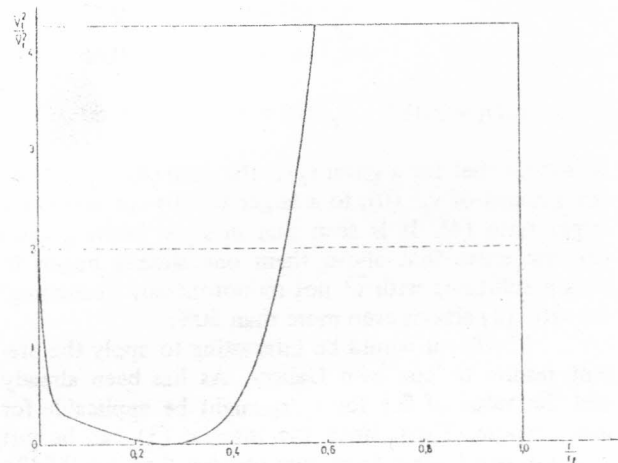


Figure 4  $r_c/r_1 = 0.01$ ,  $\bar{v}_r^2(0) = 2 \times 4\pi G A r_c^2$ ,  $f(r) = 0.975(1-r/r_1)^4 + 0.025(1-r^2/r_1^2)$

obtained an arbitrarily small and weakly variable  $\bar{v}_t^2 / \bar{v}_r^2$  ratio.

As quantitative measures of the radial fraction in the velocity distribution one can use according to the present author the value of  $\bar{v}_r^2(0)$  above which there are no „transversal” solutions of (1) expressed in units of the central potential. We see that for the cases which are likely for the coronae of galaxies ( $r_c/r_1$  about 0.1 or less) this amount is 6–8%. Of course, such a small rate is low probable and therefore it seems that some kind of „domination” of radial motions within the coronae of galaxies is very probable.

Another quantitative measure may be the fraction of the radial component in the total kinetic energy of the system. As well known the double total kinetic energy is defined as

$$2W_k = \int_0^{r_1} \bar{v}^2 dM,$$

where  $dM$  is the mass differential. Accordingly the mean velocity square taken over the entire system will be

$$\langle \bar{v}^2 \rangle = M^{-1} \int_0^{r_1} \bar{v}^2 dM; \quad (3)$$

$M$  is the total mass of the system. Since the integral in (3) is additive, it will be

$$\langle \bar{v}^2 \rangle = \langle \bar{v}_r^2 \rangle + \langle \bar{v}_t^2 \rangle$$

and accordingly the fraction of the radial component will be simply defined as the ratio

$$\langle \bar{v}_r^2 \rangle / \langle \bar{v}^2 \rangle. \quad (4)$$

The values of the ratio (4) corresponding to some cases considered above are

|                  |                         |      |
|------------------|-------------------------|------|
| $r_c/r_1 = 0.1$  | $\bar{v}_r^2(0) = 0.15$ | 0.19 |
|                  | $\bar{v}_r^2(0) = 0.7$  | 0.55 |
|                  | $\bar{v}_r^2(0) = 1$    | 0.66 |
| $r_c/r_1 = 0.01$ | $\bar{v}_r^2(0) = 2$    | 0.67 |

It is clear that for a given  $r_c/r_1$  the ratio (4) depends on the amount of  $\bar{v}_r^2(0)$ ; to a larger  $\bar{v}_r^2(0)$  corresponds a larger ratio (4). It is seen that in some limiting cases (in the sense that above them one already begins to obtain solutions with  $\bar{v}^2$  not monotonously decreasing) the ratio (4) attains even more than 50%.

Finally, it would be interesting to apply the present results to our own Galaxy. As has been already said the value of 0.1 for  $r_c/r_1$  might be applicable for this purpose. Then, since the integral (3) can be put into a dimensionless form, one obtains  $\langle \bar{v}^2 \rangle = 0.547 \times 4\pi G A r_c^2$  regardless of  $\bar{v}_r^2(0)$  assumed. If one assumes as rough values  $r_c = 10$  kpc and  $A = 0.01 M_\odot \text{ pc}^{-3}$ ,

one obtains  $\langle \bar{v}^2 \rangle = 175^2 \text{ km}^2 \text{ s}^{-2}$ . The mean square of the radial velocity taken over the entire system naturally depends on  $\bar{v}_r^2(0)$  assumed in the analysis. For the two cases presented in Figs. 2–3 it is  $\langle \bar{v}_r^2 \rangle = 0.298 \times 4\pi G A r_c^2$ , i. e.  $0.363 \times 4\pi G A r_c^2$ , or  $129^2 \text{ km}^2 \text{ s}^{-2}$ ,  $143^2 \text{ km}^2 \text{ s}^{-2}$ . If the value of 8.5 kpc is assumed for the galactocentric distance of the Sun according to the IAU, then at the Sun we shall have  $\bar{v}_t^2/\bar{v}_r^2 \approx 1$ . Of course, all these conclusions are tentative since they are valid for the case of a spherically symmetric and self-consistent galactic corona which, strictly speaking, is not true. Perhaps, such a situation is not far from the truth (see galactic models, e. g. by Caldwell and Ostriker, 1981 and by Rohlfs and Kreitschmann, 1981). In any case a study taking into account these circumstances is desirable.

One should certainly emphasize once again that the coronal constituents are unknown, so that any observational verification of the present conclusions meets extremely serious difficulties. The only chance is to study eventual consequences for models of the Galaxy (and also for other galaxies).

The principal conclusion of the present paper is that the conclusions of Antonov and Chernin (1975) are confirmed in principle and that they are made more complete by introducing the ratio (4) as a quantitative measure of the radial-component fraction in the kinetic energy of the coronae of galaxies.

## NOTE

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РАЗМАТРАЊЕ РАСПОДЕЛЕ БРЗИНЕ У КОРОНАМА ГАЛАКСИЈА

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*Оригинални научни рад*

Претпоставља се да су короне галаксија сферно-симетричне, само-усаглашене и у стационарном стању. Расподела брзине се проучава на основу хидродинамичке једначине преко односа  $\overline{v_t^2}/\overline{v_r^2}$  /трансверзална и радијална компонента брзине, респективно/. Нађено је да у условима који се срећу у стварним га-

лаксијама радијална кретања преовлађују тако да удео радијалне компоненте брзине у укупној кинетичкој енергији система достиже и више од 50%. На основу резултата овог рада примењених на нашу Галаксију проистиче да је за галактоцентрични положај Сунца вредност горњег односа нешто мало већа од јединице.



## STARK BROADENING OF K I LINES

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**SUMMARY:** Using a semiclassical approach, we have calculated electron-, proton- and ionized helium-impact widths and shifts of 51 neutral potassium multiplets as a function of electron temperature and electron density.

## 1. INTRODUCTION

Stark broadening parameters for potassium lines are useful in astrophysics as well as in plasma diagnostics, technology of high pressure discharge lamps etc. Solar abundance of potassium is 4.70 (Hack and Struve, 1969). K abundance is also determined by using line profiles, e.g. for  $\gamma$  Ser and  $\xi$  Her (Hack and Struve, 1969). Potassium line profiles are also important for the study of pulsed lamps at medium and high pressures, containing K vapors. Such lamps are important for neodymium laser optical pumping, since potassium lines coincide with absorption bands of laser material.

Using a semiclassical-perturbation formalism (Sahal-Bréchet, 1969a, b) we have calculated recently (Dimitrijević and Sahal-Bréchet, 1987) electron-, proton- and ArII-impact line widths and shifts of 50 neutral potassium multiplets at electron density  $N_e = 10^{15} \text{ cm}^{-3}$ . Due to Debye screening, obtained data are not always linear with electron density, especially in the case of transitions between more excited states. Since the corrections proposed e. g. by Griem (1974) are not simple to do, we recalculated Stark broadening data as a function of electron density also. Moreover, we improved the integration procedure (the improvements influence especially the shift at higher temperatures) and we included ionized helium-impact broadening parameters due to its astrophysical meaning.

## 2. THEORY

Details concerning the calculation procedure are given elsewhere (Sahal-Bréchet, 1969a, b) and only a few details will be given here. Within the framework of semiclassical-perturbational formalism developed using impact approximation, the full halfwidth (2W) and shift (D) of an electron-impact broadened line can be expressed as (Sahal-Bréchet, 1969a, b):

$$2W = N_e \int_0^\infty v f(v) dv \left[ \sum_{i' \neq i} \sigma_{ii'}(v) + \sum_{f' \neq f} \sigma_{ff'}(v) + \sigma_{el}(v) \right] \quad (1)$$

$$D = N_e \int_0^\infty v f(v) dv \int_{R_3}^{R_D} 2\pi \rho d\rho \sin 2\varphi_p.$$

Here,  $N_e$  is the electron density,  $f(v)$  the Maxwellian velocity distribution function for electrons,  $\rho$  denotes the impact parameter of the incoming electron,  $i$  and  $f$  denote the initial and final atomic energy level and  $i'$ ,  $f'$  their perturbing levels. The inelastic crosssection  $\sigma_{ii'}(v)$  can be expressed by an integration over the impact parameter of the transition probability  $P_{ii'}(\rho, v)$

$$\sum_{i' \neq i} \sigma_{ii'}(v) = \frac{1}{2} \pi R_1^2 + \int_{R_1}^{R_D} 2\pi \rho d\rho \sum_{i' \neq i} P_{ii'}(\rho, v) \quad (2)$$

and the elastic cross section is given by

$$\sigma_{el} = 2\pi R_2^2 + \int_{R_2}^{R_D} 8\pi\rho d\rho \sin^2 \delta \quad (3)$$

$$\delta = [\varphi_p^2 + \varphi_q^2]^{1/2}$$

The phase shifts  $\varphi_p$  and  $\varphi_q$  due respectively to the polarization potential ( $r^{-4}$ ) and to the quadrupolar potential ( $r^{-3}$ ) part, are given in §3 of Section 3 in the paper of Sahal-Bréchet (1969a). All the cut offs  $R_1$ ,  $R_2$ ,  $R_3$ ,  $R_D$  are described in § 1 of Section 3 of Sahal-Bréchet (1969b).

If we want to make certain that a line is isolated, we can use the parameter  $c$  defined by Dimitrijević and Sahal-Bréchet (1984) and given in Table. For an electron concentration lower than

$$N_e(\text{cm}^{-3}) = [c/2W(\text{\AA})] [N(\text{cm}^{-3})/10^{15}] \quad (4)$$

the line can be treated as isolated in the core, even if weak forbidden components due to the failure of this approximation still appear in the wing.

### 3. RESULTS AND DISCUSSION

Data for needed energy levels were taken from Bashkin and Stoner (1975). Oscillator strengths have been calculated using the method of Bates and Damgaard (1949) and tables of Oertel and Shomo (1968), while for low-lying levels, the oscillator strengths were taken from Wiese, Smith and Miles (1969). For higher levels, when tables of Oertel and Shomo are not applicable, the method described by Van Regemorter, Hoang Binh Dy and Prud'homme (1979) was used.

The results are shown in Table 1 for a number of temperatures (2500; 5000; 10000; 20000; 40000 and 80000 K) and for electron densities from  $10^{13} \text{ cm}^{-3}$  to  $10^{18} \text{ cm}^{-3}$ . In table is also given a parameter denoted by  $c$  (see Eq. 4) which can be used to obtain an estimate for the maximum electron density for which the line may be treated as isolated.

We checked also is the collision volume ( $V$ ) multiplied by the electron density ( $N_e$ ) much lesser than one for values given in the table. In such a case, the impact approximation is valid (Sahal-Bréchet, 1969). The values for which  $N_e V > 0.5$  are not given in the table, while values where  $0.1 < N_e V \leq 0.5$  are denoted with an asterisk and are given in order to enable interpolation to lower densities. In the cases when the impact approximation is not valid, the ion broadening contribution may be estimated by the quasistatic ion-broadening parameter (Griem, 1974) introduced by Griem et al (1962). Ar II impact linewidths and shifts for 50 neutral potassium multiplets at  $N_e = 10^{15} \text{ cm}^{-3}$  may be found in Dimitrijević and Sahal-Bréchet (1987).

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Table 1. This table lists electron-, proton- and ionized helium-impact broadening parameters for K I lines for electron densities from  $10^{13} \text{ cm}^{-3}$  to  $10^{18} \text{ cm}^{-3}$  and temperatures from 2500 K to 80000 K. Transitions and averaged wavelengths for the multiplet (in Å) are also given. Under  $2W$  are given full halfwidths (in Å) while  $D$  denote corresponding shifts. By using  $c$  [see Eq. (4)], we obtain an estimate for the maximum electron density for which the line may be treated as isolated and the tabulated values may be used. Asterisk denotes cases when the collision volume multiplied by the electron density (condition for the validity of the impact approximation) lies between 0.1 and 0.5.

## STARK BROADENING OF K I LINES

NE= 0.1E+14

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS   |            | IONIZED HELIUM |            |
|-------------|--------|-----------|------------|-----------|------------|----------------|------------|
|             |        | 2WE (A)   | DE (A)     | 2WI (A)   | DI (A)     | 2WI (A)        | DI (A)     |
| 3D - 4P     | 2500.  | 3.60      | -0.470E-01 | 1.61*     | 1.38*      | 1.27*          | 1.09*      |
| 91050.0A    | 5000.  | 3.39      | -0.877E-01 | 1.86      | 1.61       | 1.44*          | 1.27*      |
| C= 0.27E+19 | 10000. | 3.11      | -0.110     | 2.11      | 1.89       | 1.64*          | 1.46*      |
|             | 20000. | 2.80      | -0.619E-01 | 2.17      | 2.26       | 1.89           | 1.67       |
|             | 30000. | 2.62      | -0.510E-01 | 2.04      | 2.45       | 2.04           | 1.83       |
|             | 80000. | 2.17      | -0.242E-01 | 1.43      | 2.50       | 2.15           | 2.31       |
| 3D - 5P     | 2500.  | 0.573E-02 | 0.333E-02  | 0.210E-02 | 0.883E-03  | 0.205E-02      | 0.709E-03  |
| 31453.0A    | 5000.  | 0.655E-02 | 0.398E-02  | 0.215E-02 | 0.993E-03  | 0.207E-02      | 0.798E-03  |
| C= 0.27E+21 | 10000. | 0.770E-02 | 0.404E-02  | 0.220E-02 | 0.112E-02  | 0.211E-02      | 0.897E-03  |
|             | 20000. | 0.942E-02 | 0.364E-02  | 0.227E-02 | 0.125E-02  | 0.215E-02      | 0.101E-02  |
|             | 30000. | 0.107E-01 | 0.311E-02  | 0.232E-02 | 0.134E-02  | 0.218E-02      | 0.108E-02  |
|             | 80000. | 0.140E-01 | 0.240E-02  | 0.247E-02 | 0.158E-02  | 0.228E-02      | 0.127E-02  |
| 3D - 6P     | 2500.  | 0.352E-02 | 0.230E-02  | 0.132E-02 | 0.605E-03  | 0.127E-02      | 0.486E-03  |
| 13384.0A    | 5000.  | 0.410E-02 | 0.270E-02  | 0.135E-02 | 0.681E-03  | 0.129E-02      | 0.547E-03  |
| C= 0.21E+20 | 10000. | 0.480E-02 | 0.264E-02  | 0.139E-02 | 0.767E-03  | 0.132E-02      | 0.616E-03  |
|             | 20000. | 0.572E-02 | 0.243E-02  | 0.145E-02 | 0.862E-03  | 0.136E-02      | 0.693E-03  |
|             | 30000. | 0.640E-02 | 0.218E-02  | 0.149E-02 | 0.922E-03  | 0.138E-02      | 0.741E-03  |
|             | 80000. | 0.788E-02 | 0.167E-02  | 0.160E-02 | 0.109E-02  | 0.146E-02      | 0.873E-03  |
| 3D - 7P     | 2500.  | 0.560E-02 | 0.370E-02  | 0.201E-02 | 0.961E-03  | 0.193E-02      | 0.769E-03  |
| 10482.0A    | 5000.  | 0.655E-02 | 0.420E-02  | 0.206E-02 | 0.109E-02  | 0.197E-02      | 0.871E-03  |
| C= 0.68E+19 | 10000. | 0.772E-02 | 0.418E-02  | 0.214E-02 | 0.122E-02  | 0.201E-02      | 0.981E-03  |
|             | 20000. | 0.925E-02 | 0.343E-02  | 0.223E-02 | 0.137E-02  | 0.207E-02      | 0.110E-02  |
|             | 30000. | 0.103E-01 | 0.298E-02  | 0.229E-02 | 0.147E-02  | 0.211E-02      | 0.118E-02  |
|             | 80000. | 0.123E-01 | 0.197E-02  | 0.248E-02 | 0.173E-02  | 0.224E-02      | 0.139E-02  |
| 3D - 8P     | 2500.  | 0.974E-02 | 0.646E-02  | 0.332E-02 | 0.164E-02  | 0.318E-02      | 0.131E-02  |
| 9348.6A     | 5000.  | 0.114E-01 | 0.694E-02  | 0.342E-02 | 0.186E-02  | 0.324E-02      | 0.149E-02  |
| C= 0.32E+19 | 10000. | 0.136E-01 | 0.650E-02  | 0.355E-02 | 0.209E-02  | 0.333E-02      | 0.168E-02  |
|             | 20000. | 0.164E-01 | 0.505E-02  | 0.372E-02 | 0.236E-02  | 0.343E-02      | 0.189E-02  |
|             | 30000. | 0.183E-01 | 0.410E-02  | 0.383E-02 | 0.253E-02  | 0.351E-02      | 0.203E-02  |
|             | 80000. | 0.212E-01 | 0.220E-02  | 0.417E-02 | 0.298E-02  | 0.374E-02      | 0.240E-02  |
| 3D - 9P     | 2500.  | 0.167E-01 | 0.107E-01  | 0.539E-02 | 0.274E-02  | 0.515E-02      | 0.218E-02  |
| 8764.8A     | 5000.  | 0.196E-01 | 0.112E-01  | 0.558E-02 | 0.311E-02  | 0.527E-02      | 0.249E-02  |
| C= 0.18E+19 | 10000. | 0.236E-01 | 0.102E-01  | 0.582E-02 | 0.352E-02  | 0.542E-02      | 0.282E-02  |
|             | 20000. | 0.288E-01 | 0.740E-02  | 0.610E-02 | 0.397E-02  | 0.561E-02      | 0.319E-02  |
|             | 30000. | 0.318E-01 | 0.557E-02  | 0.630E-02 | 0.425E-02  | 0.574E-02      | 0.341E-02  |
|             | 80000. | 0.361E-01 | 0.247E-02  | 0.689E-02 | 0.502E-02  | 0.614E-02      | 0.403E-02  |
| 3D - 4F     | 2500.  | 0.264E-02 | -0.110E-02 | 0.595E-03 | -0.377E-03 | 0.550E-03      | -0.302E-03 |
| 15165.0A    | 5000.  | 0.295E-02 | -0.702E-03 | 0.627E-03 | -0.424E-03 | 0.571E-03      | -0.340E-03 |
| C= 0.17E+20 | 10000. | 0.355E-02 | -0.358E-03 | 0.666E-03 | -0.476E-03 | 0.598E-03      | -0.383E-03 |
|             | 20000. | 0.408E-02 | -0.111E-03 | 0.713E-03 | -0.535E-03 | 0.631E-03      | -0.430E-03 |
|             | 30000. | 0.439E-02 | -0.114E-03 | 0.745E-03 | -0.572E-03 | 0.654E-03      | -0.460E-03 |
|             | 80000. | 0.508E-02 | 0.416E-04  | 0.837E-03 | -0.674E-03 | 0.719E-03      | -0.542E-03 |

| NE= 0.1E+14 |        |           |            |           |           |                |           |
|-------------|--------|-----------|------------|-----------|-----------|----------------|-----------|
| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS   |           | IONIZED HELIUM |           |
|             |        | 2WE(A)    | DE(A)      | 2WI(A)    | DI(A)     | 2WI(A)         | DI(A)     |
| 3D - 5F     | 2500.  | 0.236E-01 | 0.348E-02  | 0.839E-02 | 0.754E-02 | 0.674E-02      | 0.600E-02 |
| 11022.3A    | 5000.  | 0.216E-01 | 0.137E-02  | 0.949E-02 | 0.859E-02 | 0.756E-02      | 0.687E-02 |
| C= 0.14E+18 | 10000. | 0.197E-01 | 0.734E-03  | 0.108E-01 | 0.977E-02 | 0.851E-02      | 0.781E-02 |
|             | 20000. | 0.180E-01 | -0.200E-03 | 0.125E-01 | 0.112E-01 | 0.963E-02      | 0.885E-02 |
|             | 30000. | 0.170E-01 | -0.202E-03 | 0.134E-01 | 0.124E-01 | 0.104E-01      | 0.950E-02 |
|             | 80000. | 0.147E-01 | -0.975E-04 | 0.136E-01 | 0.152E-01 | 0.127E-01      | 0.114E-01 |
| 4S - 4P     | 2500.  | 0.448E-04 | 0.339E-04  | 0.277E-04 | 0.942E-05 | 0.273E-04      | 0.757E-05 |
| 7676.2A     | 5000.  | 0.509E-04 | 0.401E-04  | 0.280E-04 | 0.106E-04 | 0.275E-04      | 0.850E-05 |
| C= 0.47E+20 | 10000. | 0.624E-04 | 0.454E-04  | 0.284E-04 | 0.119E-04 | 0.277E-04      | 0.955E-05 |
|             | 20000. | 0.825E-04 | 0.461E-04  | 0.290E-04 | 0.133E-04 | 0.281E-04      | 0.107E-04 |
|             | 30000. | 0.973E-04 | 0.410E-04  | 0.294E-04 | 0.143E-04 | 0.283E-04      | 0.115E-04 |
|             | 80000. | 0.139E-03 | 0.285E-04  | 0.306E-04 | 0.168E-04 | 0.291E-04      | 0.135E-04 |
| 4S - 5P     | 2500.  | 0.963E-04 | 0.606E-04  | 0.406E-04 | 0.165E-04 | 0.397E-04      | 0.133E-04 |
| 4045.2A     | 5000.  | 0.110E-03 | 0.719E-04  | 0.414E-04 | 0.186E-04 | 0.401E-04      | 0.149E-04 |
| C= 0.44E+19 | 10000. | 0.126E-03 | 0.777E-04  | 0.424E-04 | 0.209E-04 | 0.407E-04      | 0.168E-04 |
|             | 20000. | 0.148E-03 | 0.763E-04  | 0.436E-04 | 0.235E-04 | 0.415E-04      | 0.189E-04 |
|             | 30000. | 0.164E-03 | 0.670E-04  | 0.445E-04 | 0.251E-04 | 0.420E-04      | 0.202E-04 |
|             | 80000. | 0.206E-03 | 0.492E-04  | 0.472E-04 | 0.296E-04 | 0.438E-04      | 0.238E-04 |
| 4S - 6P     | 2500.  | 0.233E-03 | 0.152E-03  | 0.920E-04 | 0.409E-04 | 0.893E-04      | 0.328E-04 |
| 3446.7A     | 5000.  | 0.271E-03 | 0.176E-03  | 0.942E-04 | 0.460E-04 | 0.906E-04      | 0.370E-04 |
| C= 0.14E+19 | 10000. | 0.315E-03 | 0.183E-03  | 0.969E-04 | 0.518E-04 | 0.922E-04      | 0.416E-04 |
|             | 20000. | 0.373E-03 | 0.171E-03  | 0.100E-03 | 0.582E-04 | 0.945E-04      | 0.468E-04 |
|             | 30000. | 0.414E-03 | 0.150E-03  | 0.103E-03 | 0.623E-04 | 0.960E-04      | 0.501E-04 |
|             | 80000. | 0.505E-03 | 0.107E-03  | 0.110E-03 | 0.734E-04 | 0.101E-03      | 0.590E-04 |
| 4S - 7P     | 2500.  | 0.526E-03 | 0.346E-03  | 0.193E-03 | 0.909E-04 | 0.186E-03      | 0.728E-04 |
| 3217.3A     | 5000.  | 0.615E-03 | 0.395E-03  | 0.198E-03 | 0.103E-03 | 0.190E-03      | 0.824E-04 |
| C= 0.64E+18 | 10000. | 0.723E-03 | 0.385E-03  | 0.205E-03 | 0.116E-03 | 0.194E-03      | 0.928E-04 |
|             | 20000. | 0.864E-03 | 0.333E-03  | 0.214E-03 | 0.130E-03 | 0.199E-03      | 0.104E-03 |
|             | 30000. | 0.961E-03 | 0.282E-03  | 0.220E-03 | 0.139E-03 | 0.203E-03      | 0.112E-03 |
|             | 80000. | 0.114E-02 | 0.184E-03  | 0.237E-03 | 0.164E-03 | 0.215E-03      | 0.132E-03 |
| 4S - 8P     | 2500.  | 0.107E-02 | 0.700E-03  | 0.368E-03 | 0.180E-03 | 0.354E-03      | 0.144E-03 |
| 3101.9A     | 5000.  | 0.125E-02 | 0.765E-03  | 0.380E-03 | 0.204E-03 | 0.361E-03      | 0.164E-03 |
| C= 0.36E+18 | 10000. | 0.149E-02 | 0.738E-03  | 0.394E-03 | 0.230E-03 | 0.370E-03      | 0.185E-03 |
|             | 20000. | 0.180E-02 | 0.580E-03  | 0.412E-03 | 0.259E-03 | 0.381E-03      | 0.208E-03 |
|             | 30000. | 0.200E-02 | 0.479E-03  | 0.425E-03 | 0.278E-03 | 0.390E-03      | 0.223E-03 |
|             | 80000. | 0.232E-02 | 0.277E-03  | 0.461E-03 | 0.328E-03 | 0.415E-03      | 0.264E-03 |
| 4S - 9P     | 2500.  | 0.199E-02 | 0.128E-02  | 0.650E-03 | 0.328E-03 | 0.621E-03      | 0.262E-03 |
| 3034.8A     | 5000.  | 0.235E-02 | 0.134E-02  | 0.672E-03 | 0.373E-03 | 0.635E-03      | 0.298E-03 |
| C= 0.22E+18 | 10000. | 0.282E-02 | 0.124E-02  | 0.700E-03 | 0.422E-03 | 0.653E-03      | 0.338E-03 |
|             | 20000. | 0.344E-02 | 0.931E-03  | 0.735E-03 | 0.476E-03 | 0.675E-03      | 0.382E-03 |
|             | 30000. | 0.380E-02 | 0.760E-03  | 0.758E-03 | 0.510E-03 | 0.691E-03      | 0.409E-03 |
|             | 80000. | 0.431E-02 | 0.395E-03  | 0.828E-03 | 0.602E-03 | 0.739E-03      | 0.484E-03 |



# STARK BROADENING OF K I LINES

NE= 0.1E+14

| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS   |           | IONIZED HELIUM |           |
|-------------|--------|-----------|-----------|-----------|-----------|----------------|-----------|
|             |        | 2WE (A)   | DE (A)    | 2WI (A)   | DI (A)    | 2WI (A)        | DI (A)    |
| 4P - 5S     | 2500.  | 0.584E-03 | 0.412E-03 | 0.136E-03 | 0.114E-03 | 0.116E-03      | 0.914E-04 |
| 12492.0A    | 5000.  | 0.672E-03 | 0.490E-03 | 0.150E-03 | 0.128E-03 | 0.126E-03      | 0.103E-03 |
| C= 0.58E+20 | 10000. | 0.748E-03 | 0.573E-03 | 0.165E-03 | 0.144E-03 | 0.138E-03      | 0.116E-03 |
|             | 20000. | 0.844E-03 | 0.566E-03 | 0.182E-03 | 0.161E-03 | 0.151E-03      | 0.130E-03 |
|             | 30000. | 0.900E-03 | 0.513E-03 | 0.193E-03 | 0.173E-03 | 0.160E-03      | 0.139E-03 |
|             | 80000. | 0.115E-02 | 0.361E-03 | 0.224E-03 | 0.203E-03 | 0.184E-03      | 0.163E-03 |
| 4P - 6S     | 2500.  | 0.665E-03 | 0.488E-03 | 0.143E-03 | 0.133E-03 | 0.116E-03      | 0.107E-03 |
| 6929.5A     | 5000.  | 0.765E-03 | 0.572E-03 | 0.160E-03 | 0.150E-03 | 0.130E-03      | 0.120E-03 |
| C= 0.75E+19 | 10000. | 0.824E-03 | 0.625E-03 | 0.180E-03 | 0.169E-03 | 0.145E-03      | 0.136E-03 |
|             | 20000. | 0.916E-03 | 0.619E-03 | 0.202E-03 | 0.190E-03 | 0.163E-03      | 0.152E-03 |
|             | 30000. | 0.950E-03 | 0.554E-03 | 0.216E-03 | 0.203E-03 | 0.174E-03      | 0.163E-03 |
|             | 80000. | 0.117E-02 | 0.413E-03 | 0.254E-03 | 0.239E-03 | 0.204E-03      | 0.192E-03 |
| 4P - 7S     | 2500.  | 0.126E-02 | 0.936E-03 | 0.265E-03 | 0.247E-03 | 0.213E-03      | 0.198E-03 |
| 5795.3A     | 5000.  | 0.151E-02 | 0.110E-02 | 0.297E-03 | 0.278E-03 | 0.239E-03      | 0.223E-03 |
| C= 0.27E+19 | 10000. | 0.154E-02 | 0.110E-02 | 0.333E-03 | 0.313E-03 | 0.268E-03      | 0.252E-03 |
|             | 20000. | 0.170E-02 | 0.103E-02 | 0.374E-03 | 0.352E-03 | 0.301E-03      | 0.283E-03 |
|             | 30000. | 0.184E-02 | 0.896E-03 | 0.400E-03 | 0.377E-03 | 0.322E-03      | 0.303E-03 |
|             | 80000. | 0.224E-02 | 0.642E-03 | 0.471E-03 | 0.445E-03 | 0.379E-03      | 0.358E-03 |
| 4P - 8S     | 2500.  | 0.232E-02 | 0.168E-02 | 0.468E-03 | 0.434E-03 | 0.377E-03      | 0.347E-03 |
| 5334.3A     | 5000.  | 0.260E-02 | 0.191E-02 | 0.526E-03 | 0.492E-03 | 0.423E-03      | 0.394E-03 |
| C= 0.13E+19 | 10000. | 0.298E-02 | 0.189E-02 | 0.590E-03 | 0.554E-03 | 0.474E-03      | 0.445E-03 |
|             | 20000. | 0.323E-02 | 0.153E-02 | 0.662E-03 | 0.624E-03 | 0.533E-03      | 0.501E-03 |
|             | 30000. | 0.360E-02 | 0.127E-02 | 0.709E-03 | 0.668E-03 | 0.570E-03      | 0.537E-03 |
|             | 80000. | 0.425E-02 | 0.762E-03 | 0.835E-03 | 0.788E-03 | 0.671E-03      | 0.634E-03 |
| 4P - 9S     | 2500.  | 0.431E-02 | 0.317E-02 | 0.870E-03 | 0.800E-03 | 0.700E-03      | 0.638E-03 |
| 5094.3A     | 5000.  | 0.475E-02 | 0.346E-02 | 0.977E-03 | 0.908E-03 | 0.786E-03      | 0.727E-03 |
| C= 0.76E+18 | 10000. | 0.537E-02 | 0.319E-02 | 0.110E-02 | 0.103E-02 | 0.882E-03      | 0.824E-03 |
|             | 20000. | 0.623E-02 | 0.244E-02 | 0.123E-02 | 0.116E-02 | 0.990E-03      | 0.929E-03 |
|             | 30000. | 0.695E-02 | 0.189E-02 | 0.132E-02 | 0.124E-02 | 0.106E-02      | 0.996E-03 |
|             | 80000. | 0.796E-02 | 0.907E-03 | 0.155E-02 | 0.146E-02 | 0.125E-02      | 0.118E-02 |
| 4P -10S     | 2500.  | 0.730E-02 | 0.522E-02 | 0.146E-02 | 0.133E-02 | 0.118E-02      | 0.106E-02 |
| 4951.4A     | 5000.  | 0.807E-02 | 0.544E-02 | 0.164E-02 | 0.152E-02 | 0.132E-02      | 0.121E-02 |
| C= 0.48E+18 | 10000. | 0.924E-02 | 0.498E-02 | 0.184E-02 | 0.172E-02 | 0.148E-02      | 0.138E-02 |
|             | 20000. | 0.111E-01 | 0.357E-02 | 0.207E-02 | 0.194E-02 | 0.166E-02      | 0.156E-02 |
|             | 30000. | 0.123E-01 | 0.261E-02 | 0.222E-02 | 0.208E-02 | 0.178E-02      | 0.167E-02 |
|             | 80000. | 0.138E-01 | 0.105E-02 | 0.261E-02 | 0.246E-02 | 0.210E-02      | 0.198E-02 |
| 4P -11S     | 2500.  | 0.119E-01 | 0.843E-02 | 0.230E-02 | 0.207E-02 | 0.185E-02      | 0.164E-02 |
| 4859.0A     | 5000.  | 0.131E-01 | 0.818E-02 | 0.259E-02 | 0.237E-02 | 0.208E-02      | 0.189E-02 |
| C= 0.33E+18 | 10000. | 0.152E-01 | 0.706E-02 | 0.290E-02 | 0.270E-02 | 0.234E-02      | 0.216E-02 |
|             | 20000. | 0.187E-01 | 0.491E-02 | 0.326E-02 | 0.305E-02 | 0.262E-02      | 0.245E-02 |
|             | 30000. | 0.206E-01 | 0.364E-02 | 0.349E-02 | 0.327E-02 | 0.281E-02      | 0.263E-02 |
|             | 80000. | 0.228E-01 | 0.124E-02 | 0.412E-02 | 0.387E-02 | 0.330E-02      | 0.311E-02 |

| NE= 0.1E+14 |        |           |           |           |           |                |            |
|-------------|--------|-----------|-----------|-----------|-----------|----------------|------------|
| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS   |           | IONIZED HELIUM |            |
|             |        | 2WE(A)    | DE(A)     | 2WI(A)    | DI(A)     | 2WI(A)         | DI(A)      |
| 4P - 12S    | 2500.  | 0.173E-01 | 0.118E-01 | 0.334E-02 | 0.297E-02 | 0.269E-02*     | 0.235E-02* |
| 4795.7A     | 5000.  | 0.206E-01 | 0.116E-01 | 0.375E-02 | 0.341E-02 | 0.301E-02      | 0.272E-02  |
| C= 0.24E+18 | 10000. | 0.238E-01 | 0.917E-02 | 0.421E-02 | 0.389E-02 | 0.338E-02      | 0.311E-02  |
|             | 20000. | 0.298E-01 | 0.624E-02 | 0.473E-02 | 0.441E-02 | 0.380E-02      | 0.353E-02  |
|             | 30000. | 0.327E-01 | 0.465E-02 | 0.506E-02 | 0.474E-02 | 0.407E-02      | 0.380E-02  |
|             | 80000. | 0.358E-01 | 0.144E-02 | 0.597E-02 | 0.560E-02 | 0.479E-02      | 0.450E-02  |
| 4P - 3D     | 2500.  | 0.253E-03 | 0.131E-03 | 0.873E-04 | 0.348E-04 | 0.854E-04      | 0.279E-04  |
| 11745.0A    | 5000.  | 0.271E-03 | 0.144E-03 | 0.888E-04 | 0.390E-04 | 0.863E-04      | 0.314E-04  |
| C= 0.44E+20 | 10000. | 0.312E-03 | 0.142E-03 | 0.908E-04 | 0.438E-04 | 0.875E-04      | 0.352E-04  |
|             | 20000. | 0.394E-03 | 0.111E-03 | 0.933E-04 | 0.492E-04 | 0.890E-04      | 0.396E-04  |
|             | 30000. | 0.464E-03 | 0.944E-04 | 0.952E-04 | 0.526E-04 | 0.901E-04      | 0.423E-04  |
|             | 80000. | 0.639E-03 | 0.673E-04 | 0.101E-03 | 0.620E-04 | 0.937E-04      | 0.498E-04  |
| 4P - 4D     | 2500.  | 0.766E-03 | 0.563E-03 | 0.200E-03 | 0.147E-03 | 0.177E-03      | 0.118E-03  |
| 6955.2A     | 5000.  | 0.839E-03 | 0.605E-03 | 0.215E-03 | 0.166E-03 | 0.188E-03      | 0.133E-03  |
| C= 0.35E+19 | 10000. | 0.914E-03 | 0.579E-03 | 0.232E-03 | 0.186E-03 | 0.201E-03      | 0.150E-03  |
|             | 20000. | 0.101E-02 | 0.457E-03 | 0.253E-03 | 0.210E-03 | 0.217E-03      | 0.168E-03  |
|             | 30000. | 0.109E-02 | 0.406E-03 | 0.267E-03 | 0.224E-03 | 0.227E-03      | 0.180E-03  |
|             | 80000. | 0.120E-02 | 0.282E-03 | 0.305E-03 | 0.264E-03 | 0.256E-03      | 0.212E-03  |
| 4P - 5D     | 2500.  | 0.166E-02 | 0.124E-02 | 0.422E-03 | 0.316E-03 | 0.373E-03      | 0.253E-03  |
| 5825.3A     | 5000.  | 0.181E-02 | 0.128E-02 | 0.455E-03 | 0.357E-03 | 0.397E-03      | 0.286E-03  |
| C= 0.14E+19 | 10000. | 0.197E-02 | 0.122E-02 | 0.494E-03 | 0.401E-03 | 0.426E-03      | 0.322E-03  |
|             | 20000. | 0.221E-02 | 0.923E-03 | 0.540E-03 | 0.451E-03 | 0.460E-03      | 0.363E-03  |
|             | 30000. | 0.236E-02 | 0.776E-03 | 0.570E-03 | 0.483E-03 | 0.482E-03      | 0.388E-03  |
|             | 80000. | 0.254E-02 | 0.453E-03 | 0.654E-03 | 0.570E-03 | 0.546E-03      | 0.458E-03  |
| 4P - 6D     | 2500.  | 0.333E-02 | 0.249E-02 | 0.833E-03 | 0.626E-03 | 0.731E-03      | 0.500E-03  |
| 5354.1A     | 5000.  | 0.364E-02 | 0.252E-02 | 0.901E-03 | 0.710E-03 | 0.781E-03      | 0.568E-03  |
| C= 0.74E+18 | 10000. | 0.398E-02 | 0.225E-02 | 0.980E-03 | 0.802E-03 | 0.840E-03      | 0.644E-03  |
|             | 20000. | 0.452E-02 | 0.165E-02 | 0.107E-02 | 0.902E-03 | 0.909E-03      | 0.725E-03  |
|             | 30000. | 0.483E-02 | 0.128E-02 | 0.113E-02 | 0.967E-03 | 0.955E-03      | 0.776E-03  |
|             | 80000. | 0.512E-02 | 0.581E-03 | 0.130E-02 | 0.114E-02 | 0.108E-02      | 0.917E-03  |
| 4P - 7D     | 2500.  | 0.624E-02 | 0.467E-02 | 0.153E-02 | 0.116E-02 | 0.134E-02      | 0.923E-03  |
| 5107.2A     | 5000.  | 0.683E-02 | 0.445E-02 | 0.166E-02 | 0.132E-02 | 0.143E-02      | 0.105E-02  |
| C= 0.43E+18 | 10000. | 0.752E-02 | 0.385E-02 | 0.181E-02 | 0.149E-02 | 0.155E-02      | 0.120E-02  |
|             | 20000. | 0.863E-02 | 0.274E-02 | 0.199E-02 | 0.168E-02 | 0.168E-02      | 0.135E-02  |
|             | 30000. | 0.917E-02 | 0.204E-02 | 0.210E-02 | 0.180E-02 | 0.177E-02      | 0.145E-02  |
|             | 80000. | 0.960E-02 | 0.736E-03 | 0.242E-02 | 0.213E-02 | 0.201E-02      | 0.171E-02  |
| 4P - 8D     | 2500.  | 0.109E-01 | 0.789E-02 | 0.265E-02 | 0.200E-02 | 0.230E-02      | 0.159E-02  |
| 4960.2A     | 5000.  | 0.120E-01 | 0.778E-02 | 0.288E-02 | 0.229E-02 | 0.247E-02      | 0.183E-02  |
| C= 0.28E+18 | 10000. | 0.134E-01 | 0.616E-02 | 0.315E-02 | 0.260E-02 | 0.267E-02      | 0.208E-02  |
|             | 20000. | 0.154E-01 | 0.429E-02 | 0.346E-02 | 0.295E-02 | 0.291E-02      | 0.236E-02  |
|             | 30000. | 0.162E-01 | 0.314E-02 | 0.366E-02 | 0.316E-02 | 0.306E-02      | 0.254E-02  |
|             | 80000. | 0.168E-01 | 0.986E-03 | 0.423E-02 | 0.373E-02 | 0.349E-02      | 0.300E-02  |



## STARK BROADENING OF K I LINES

NE= 0.1E+14

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS    |            | IONIZED HELIUM |            |
|-------------|--------|-----------|------------|------------|------------|----------------|------------|
|             |        | 2WE (A)   | DE (A)     | 2WI (A)    | DI (A)     | 2WI (A)        | DI (A)     |
| 4P - 9D     | 2500.  | 0.180E-01 | 0.128E-01  | 0.432E-02* | 0.325E-02* | 0.373E-02*     | 0.257E-02* |
| 4865.2A     | 5000.  | 0.199E-01 | 0.122E-01  | 0.470E-02  | 0.375E-02  | 0.402E-02*     | 0.298E-02* |
| C= 0.19E+18 | 10000. | 0.224E-01 | 0.926E-02  | 0.515E-02  | 0.427E-02  | 0.436E-02      | 0.341E-02  |
|             | 20000. | 0.258E-01 | 0.642E-02  | 0.567E-02  | 0.484E-02  | 0.475E-02      | 0.388E-02  |
|             | 30000. | 0.270E-01 | 0.461E-02  | 0.600E-02  | 0.521E-02  | 0.501E-02      | 0.417E-02  |
|             | 80000. | 0.277E-01 | 0.134E-02  | 0.695E-02  | 0.616E-02  | 0.573E-02      | 0.495E-02  |
| 4D - 6P     | 2500.  | 0.675E-01 | 0.173E-01  | 0.231E-01  | 0.395E-02  | 0.231E-01      | 0.317E-02  |
| 62191.0A    | 5000.  | 0.935E-01 | 0.218E-01  | 0.231E-01  | 0.444E-02  | 0.231E-01      | 0.357E-02  |
| C= 0.28E+21 | 10000. | 0.127     | 0.235E-01  | 0.232E-01  | 0.499E-02  | 0.231E-01      | 0.401E-02  |
|             | 20000. | 0.166     | 0.206E-01  | 0.233E-01  | 0.560E-02  | 0.231E-01      | 0.450E-02  |
|             | 30000. | 0.189     | 0.184E-01  | 0.233E-01  | 0.599E-02  | 0.232E-01      | 0.482E-02  |
|             | 80000. | 0.232     | 0.154E-01  | 0.235E-01  | 0.707E-02  | 0.233E-01      | 0.567E-02  |
| 4D - 7P     | 2500.  | 0.369E-01 | 0.215E-01  | 0.124E-01  | 0.559E-02  | 0.120E-01      | 0.448E-02  |
| 27199.0A    | 5000.  | 0.451E-01 | 0.232E-01  | 0.127E-01  | 0.630E-02  | 0.122E-01      | 0.506E-02  |
| C= 0.46E+20 | 10000. | 0.561E-01 | 0.225E-01  | 0.131E-01  | 0.710E-02  | 0.124E-01      | 0.570E-02  |
|             | 20000. | 0.701E-01 | 0.178E-01  | 0.136E-01  | 0.799E-02  | 0.127E-01      | 0.642E-02  |
|             | 30000. | 0.790E-01 | 0.154E-01  | 0.139E-01  | 0.855E-02  | 0.129E-01      | 0.687E-02  |
|             | 80000. | 0.941E-01 | 0.945E-02  | 0.150E-01  | 0.101E-01  | 0.136E-01      | 0.810E-02  |
| 4D - 8P     | 2500.  | 0.477E-01 | 0.296E-01  | 0.156E-01  | 0.767E-02  | 0.150E-01      | 0.614E-02  |
| 20691.0A    | 5000.  | 0.569E-01 | 0.315E-01  | 0.161E-01  | 0.870E-02  | 0.153E-01      | 0.697E-02  |
| C= 0.16E+20 | 10000. | 0.690E-01 | 0.293E-01  | 0.167E-01  | 0.981E-02  | 0.157E-01      | 0.788E-02  |
|             | 20000. | 0.852E-01 | 0.212E-01  | 0.175E-01  | 0.110E-01  | 0.162E-01      | 0.887E-02  |
|             | 30000. | 0.951E-01 | 0.172E-01  | 0.180E-01  | 0.118E-01  | 0.165E-01      | 0.950E-02  |
|             | 80000. | 0.110     | 0.868E-02  | 0.196E-01  | 0.140E-01  | 0.176E-01      | 0.112E-01  |
| 4D - 4F     | 2500.  | 0.441     | -0.263     | 0.803E-01  | -0.704E-01 | 0.668E-01      | -0.565E-01 |
| 136923.A    | 5000.  | 0.484     | -0.276     | 0.889E-01  | -0.792E-01 | 0.735E-01      | -0.636E-01 |
| C= 0.14E+22 | 10000. | 0.527     | -0.228     | 0.987E-01  | -0.891E-01 | 0.812E-01      | -0.716E-01 |
|             | 20000. | 0.617     | -0.172     | 0.110      | -0.100     | 0.900E-01      | -0.805E-01 |
|             | 30000. | 0.670     | -0.156     | 0.117      | -0.107     | 0.956E-01      | -0.862E-01 |
|             | 80000. | 0.737     | -0.953E-01 | 0.137      | -0.126     | 0.111          | -0.102     |
| 4D - 5F     | 2500.  | 0.199     | 0.183E-01  | 0.665E-01  | 0.598E-01  | 0.533E-01      | 0.476E-01  |
| 31162.0A    | 5000.  | 0.184     | 0.184E-02  | 0.752E-01  | 0.682E-01  | 0.599E-01      | 0.545E-01  |
| C= 0.11E+19 | 10000. | 0.168     | -0.103E-01 | 0.861E-01  | 0.776E-01  | 0.674E-01      | 0.620E-01  |
|             | 20000. | 0.157     | -0.943E-02 | 0.991E-01  | 0.887E-01  | 0.764E-01      | 0.702E-01  |
|             | 30000. | 0.151     | -0.100E-01 | 0.106      | 0.968E-01  | 0.825E-01      | 0.754E-01  |
|             | 80000. | 0.133     | -0.642E-02 | 0.107      | 0.120      | 0.101          | 0.906E-01  |
| 5S - 5P     | 2500.  | 0.350E-02 | 0.127E-02  | 0.174E-02  | 0.362E-03  | 0.174E-02      | 0.291E-03  |
| 27114.0A    | 5000.  | 0.416E-02 | 0.120E-02  | 0.175E-02  | 0.407E-03  | 0.174E-02      | 0.327E-03  |
| C= 0.20E+21 | 10000. | 0.550E-02 | 0.767E-03  | 0.176E-02  | 0.456E-03  | 0.175E-02      | 0.367E-03  |
|             | 20000. | 0.767E-02 | 0.485E-03  | 0.177E-02  | 0.512E-03  | 0.175E-02      | 0.412E-03  |
|             | 30000. | 0.913E-02 | 0.402E-03  | 0.177E-02  | 0.548E-03  | 0.175E-02      | 0.441E-03  |
|             | 80000. | 0.123E-01 | 0.272E-03  | 0.180E-02  | 0.646E-03  | 0.177E-02      | 0.519E-03  |

| NE= 0.1E+14 |        |           |           |           |           |                |           |
|-------------|--------|-----------|-----------|-----------|-----------|----------------|-----------|
| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS   |           | IONIZED HELIUM |           |
|             |        | 2WE (A)   | DE (A)    | 2WI (A)   | DI (A)    | 2WI (A)        | DI (A)    |
| 5S - 6P     | 2500.  | 0.302E-02 | 0.191E-02 | 0.120E-02 | 0.502E-03 | 0.117E-02      | 0.403E-03 |
| 12531.0A    | 5000.  | 0.352E-02 | 0.215E-02 | 0.123E-02 | 0.565E-03 | 0.119E-02      | 0.454E-03 |
| C= 0.19E+20 | 10000. | 0.420E-02 | 0.217E-02 | 0.126E-02 | 0.636E-03 | 0.120E-02      | 0.511E-03 |
|             | 20000. | 0.514E-02 | 0.176E-02 | 0.130E-02 | 0.715E-03 | 0.123E-02      | 0.574E-03 |
|             | 30000. | 0.585E-02 | 0.153E-02 | 0.133E-02 | 0.765E-03 | 0.125E-02      | 0.615E-03 |
|             | 80000. | 0.732E-02 | 0.116E-02 | 0.141E-02 | 0.901E-03 | 0.130E-02      | 0.724E-03 |
| 5S - 7P     | 2500.  | 0.503E-02 | 0.329E-02 | 0.184E-02 | 0.855E-03 | 0.178E-02      | 0.685E-03 |
| 9951.3A     | 5000.  | 0.588E-02 | 0.368E-02 | 0.189E-02 | 0.965E-03 | 0.181E-02      | 0.775E-03 |
| C= 0.62E+19 | 10000. | 0.699E-02 | 0.370E-02 | 0.195E-02 | 0.109E-02 | 0.185E-02      | 0.873E-03 |
|             | 20000. | 0.844E-02 | 0.299E-02 | 0.203E-02 | 0.122E-02 | 0.190E-02      | 0.983E-03 |
|             | 30000. | 0.946E-02 | 0.247E-02 | 0.209E-02 | 0.131E-02 | 0.193E-02      | 0.105E-02 |
|             | 80000. | 0.113E-01 | 0.160E-02 | 0.225E-02 | 0.154E-02 | 0.204E-02      | 0.124E-02 |
| 5S - 8P     | 2500.  | 0.886E-02 | 0.588E-02 | 0.305E-02 | 0.148E-02 | 0.292E-02      | 0.119E-02 |
| 8924.4A     | 5000.  | 0.104E-01 | 0.623E-02 | 0.314E-02 | 0.168E-02 | 0.298E-02      | 0.135E-02 |
| C= 0.29E+19 | 10000. | 0.124E-01 | 0.598E-02 | 0.326E-02 | 0.190E-02 | 0.306E-02      | 0.152E-02 |
|             | 20000. | 0.151E-01 | 0.433E-02 | 0.340E-02 | 0.214E-02 | 0.315E-02      | 0.172E-02 |
|             | 30000. | 0.168E-01 | 0.351E-02 | 0.351E-02 | 0.229E-02 | 0.322E-02      | 0.184E-02 |
|             | 80000. | 0.195E-01 | 0.183E-02 | 0.381E-02 | 0.270E-02 | 0.342E-02      | 0.217E-02 |
| 5S - 9P     | 2500.  | 0.153E-01 | 0.101E-01 | 0.497E-02 | 0.250E-02 | 0.474E-02      | 0.200E-02 |
| 8390.7A     | 5000.  | 0.180E-01 | 0.104E-01 | 0.514E-02 | 0.285E-02 | 0.485E-02      | 0.228E-02 |
| C= 0.17E+19 | 10000. | 0.216E-01 | 0.906E-02 | 0.535E-02 | 0.322E-02 | 0.499E-02      | 0.258E-02 |
|             | 20000. | 0.265E-01 | 0.597E-02 | 0.561E-02 | 0.363E-02 | 0.516E-02      | 0.292E-02 |
|             | 30000. | 0.292E-01 | 0.505E-02 | 0.579E-02 | 0.389E-02 | 0.528E-02      | 0.312E-02 |
|             | 80000. | 0.332E-01 | 0.210E-02 | 0.632E-02 | 0.459E-02 | 0.564E-02      | 0.369E-02 |
| 5P - 6S     | 2500.  | 0.180E-01 | 0.121E-01 | 0.442E-02 | 0.317E-02 | 0.396E-02      | 0.255E-02 |
| 36529.0A    | 5000.  | 0.209E-01 | 0.142E-01 | 0.473E-02 | 0.357E-02 | 0.418E-02      | 0.287E-02 |
| C= 0.21E+21 | 10000. | 0.247E-01 | 0.146E-01 | 0.511E-02 | 0.402E-02 | 0.445E-02      | 0.323E-02 |
|             | 20000. | 0.299E-01 | 0.126E-01 | 0.554E-02 | 0.451E-02 | 0.477E-02      | 0.363E-02 |
|             | 30000. | 0.344E-01 | 0.110E-01 | 0.583E-02 | 0.483E-02 | 0.499E-02      | 0.388E-02 |
|             | 80000. | 0.445E-01 | 0.868E-02 | 0.664E-02 | 0.569E-02 | 0.560E-02      | 0.457E-02 |
| 5P - 7S     | 2500.  | 0.122E-01 | 0.881E-02 | 0.255E-02 | 0.230E-02 | 0.209E-02      | 0.184E-02 |
| 17979.0A    | 5000.  | 0.139E-01 | 0.104E-01 | 0.284E-02 | 0.259E-02 | 0.232E-02      | 0.208E-02 |
| C= 0.26E+20 | 10000. | 0.154E-01 | 0.985E-02 | 0.317E-02 | 0.292E-02 | 0.258E-02      | 0.234E-02 |
|             | 20000. | 0.175E-01 | 0.896E-02 | 0.354E-02 | 0.328E-02 | 0.288E-02      | 0.264E-02 |
|             | 30000. | 0.197E-01 | 0.775E-02 | 0.378E-02 | 0.352E-02 | 0.307E-02      | 0.283E-02 |
|             | 80000. | 0.243E-01 | 0.543E-02 | 0.444E-02 | 0.414E-02 | 0.359E-02      | 0.333E-02 |
| 5P - 8S     | 2500.  | 0.169E-01 | 0.123E-01 | 0.345E-02 | 0.318E-02 | 0.279E-02      | 0.254E-02 |
| 14178.0A    | 5000.  | 0.188E-01 | 0.138E-01 | 0.387E-02 | 0.360E-02 | 0.312E-02      | 0.288E-02 |
| C= 0.93E+19 | 10000. | 0.217E-01 | 0.137E-01 | 0.434E-02 | 0.406E-02 | 0.350E-02      | 0.326E-02 |
|             | 20000. | 0.242E-01 | 0.107E-01 | 0.487E-02 | 0.457E-02 | 0.392E-02      | 0.367E-02 |
|             | 30000. | 0.272E-01 | 0.869E-02 | 0.521E-02 | 0.489E-02 | 0.419E-02      | 0.393E-02 |
|             | 80000. | 0.322E-01 | 0.509E-02 | 0.613E-02 | 0.577E-02 | 0.493E-02      | 0.464E-02 |

# STARK BROADENING OF K I LINES

NE= 0.1E+14

| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS   |           | IONIZED HELIUM |           |
|-------------|--------|-----------|-----------|-----------|-----------|----------------|-----------|
|             |        | 2WE (A)   | DE (A)    | 2WI (A)   | DI (A)    | 2WI (A)        | DI (A)    |
| 5P - 9S     | 2500.  | 0.263E-01 | 0.195E-01 | 0.531E-02 | 0.487E-02 | 0.428E-02      | 0.389E-02 |
| 12600.0A    | 5000.  | 0.290E-01 | 0.208E-01 | 0.596E-02 | 0.553E-02 | 0.480E-02      | 0.443E-02 |
| C= 0.46E+19 | 10000. | 0.332E-01 | 0.192E-01 | 0.669E-02 | 0.627E-02 | 0.539E-02      | 0.502E-02 |
|             | 20000. | 0.389E-01 | 0.134E-01 | 0.751E-02 | 0.705E-02 | 0.604E-02      | 0.566E-02 |
|             | 30000. | 0.436E-01 | 0.109E-01 | 0.804E-02 | 0.756E-02 | 0.646E-02      | 0.607E-02 |
|             | 80000. | 0.501E-01 | 0.509E-02 | 0.948E-02 | 0.892E-02 | 0.761E-02      | 0.717E-02 |
| 5P - 10S    | 2500.  | 0.412E-01 | 0.294E-01 | 0.824E-02 | 0.750E-02 | 0.663E-02      | 0.597E-02 |
| 11761.0A    | 5000.  | 0.456E-01 | 0.303E-01 | 0.926E-02 | 0.854E-02 | 0.744E-02      | 0.683E-02 |
| C= 0.27E+19 | 10000. | 0.523E-01 | 0.269E-01 | 0.104E-01 | 0.969E-02 | 0.836E-02      | 0.776E-02 |
|             | 20000. | 0.635E-01 | 0.174E-01 | 0.117E-01 | 0.109E-01 | 0.938E-02      | 0.878E-02 |
|             | 30000. | 0.706E-01 | 0.142E-01 | 0.125E-01 | 0.117E-01 | 0.100E-01      | 0.941E-02 |
|             | 80000. | 0.794E-01 | 0.557E-02 | 0.147E-01 | 0.139E-01 | 0.118E-01      | 0.111E-01 |
| 5P - 11S    | 2500.  | 0.639E-01 | 0.461E-01 | 0.124E-01 | 0.111E-01 | 0.993E-02      | 0.881E-02 |
| 11253.0A    | 5000.  | 0.702E-01 | 0.435E-01 | 0.139E-01 | 0.127E-01 | 0.112E-01      | 0.101E-01 |
| C= 0.18E+19 | 10000. | 0.817E-01 | 0.362E-01 | 0.156E-01 | 0.144E-01 | 0.125E-01      | 0.116E-01 |
|             | 20000. | 0.101     | 0.220E-01 | 0.175E-01 | 0.164E-01 | 0.141E-01      | 0.131E-01 |
|             | 30000. | 0.112     | 0.186E-01 | 0.187E-01 | 0.175E-01 | 0.150E-01      | 0.141E-01 |
|             | 80000. | 0.124     | 0.641E-02 | 0.221E-01 | 0.207E-01 | 0.177E-01      | 0.167E-01 |
| 5P - 4D     | 2500.  | 0.201E-01 | 0.138E-01 | 0.505E-02 | 0.369E-02 | 0.451E-02      | 0.296E-02 |
| 37255.0A    | 5000.  | 0.232E-01 | 0.135E-01 | 0.543E-02 | 0.416E-02 | 0.477E-02      | 0.334E-02 |
| C= 0.10E+21 | 10000. | 0.271E-01 | 0.101E-01 | 0.587E-02 | 0.467E-02 | 0.509E-02      | 0.376E-02 |
|             | 20000. | 0.341E-01 | 0.787E-02 | 0.639E-02 | 0.525E-02 | 0.548E-02      | 0.422E-02 |
|             | 30000. | 0.379E-01 | 0.673E-02 | 0.673E-02 | 0.562E-02 | 0.573E-02      | 0.452E-02 |
|             | 80000. | 0.446E-01 | 0.391E-02 | 0.769E-02 | 0.662E-02 | 0.645E-02      | 0.532E-02 |
| 5P - 5D     | 2500.  | 0.161E-01 | 0.115E-01 | 0.393E-02 | 0.303E-02 | 0.343E-02      | 0.243E-02 |
| 18272.0A    | 5000.  | 0.176E-01 | 0.121E-01 | 0.426E-02 | 0.343E-02 | 0.368E-02      | 0.275E-02 |
| C= 0.14E+20 | 10000. | 0.195E-01 | 0.106E-01 | 0.465E-02 | 0.386E-02 | 0.397E-02      | 0.310E-02 |
|             | 20000. | 0.227E-01 | 0.791E-02 | 0.509E-02 | 0.434E-02 | 0.430E-02      | 0.348E-02 |
|             | 30000. | 0.247E-01 | 0.670E-02 | 0.539E-02 | 0.465E-02 | 0.453E-02      | 0.373E-02 |
|             | 80000. | 0.273E-01 | 0.352E-02 | 0.621E-02 | 0.548E-02 | 0.515E-02      | 0.440E-02 |
| 5P - 6D     | 2500.  | 0.238E-01 | 0.171E-01 | 0.582E-02 | 0.445E-02 | 0.508E-02      | 0.355E-02 |
| 14319.0A    | 5000.  | 0.260E-01 | 0.172E-01 | 0.631E-02 | 0.504E-02 | 0.544E-02      | 0.404E-02 |
| C= 0.53E+19 | 10000. | 0.286E-01 | 0.151E-01 | 0.688E-02 | 0.569E-02 | 0.587E-02      | 0.457E-02 |
|             | 20000. | 0.330E-01 | 0.104E-01 | 0.754E-02 | 0.641E-02 | 0.637E-02      | 0.515E-02 |
|             | 30000. | 0.354E-01 | 0.839E-02 | 0.798E-02 | 0.687E-02 | 0.670E-02      | 0.552E-02 |
|             | 80000. | 0.380E-01 | 0.366E-02 | 0.919E-02 | 0.811E-02 | 0.762E-02      | 0.652E-02 |
| 5P - 7D     | 2500.  | 0.385E-01 | 0.290E-01 | 0.935E-02 | 0.712E-02 | 0.814E-02      | 0.568E-02 |
| 12679.0A    | 5000.  | 0.422E-01 | 0.270E-01 | 0.102E-01 | 0.811E-02 | 0.873E-02      | 0.648E-02 |
| C= 0.27E+19 | 10000. | 0.466E-01 | 0.224E-01 | 0.111E-01 | 0.919E-02 | 0.944E-02      | 0.736E-02 |
|             | 20000. | 0.537E-01 | 0.141E-01 | 0.122E-01 | 0.104E-01 | 0.103E-01      | 0.832E-02 |
|             | 30000. | 0.572E-01 | 0.118E-01 | 0.129E-01 | 0.111E-01 | 0.108E-01      | 0.892E-02 |
|             | 80000. | 0.603E-01 | 0.424E-02 | 0.149E-01 | 0.131E-01 | 0.123E-01      | 0.105E-01 |

| NE= 0.1E+14 |        |                     |           |                   |            |                          |            |
|-------------|--------|---------------------|-----------|-------------------|------------|--------------------------|------------|
| TRANSITION  | T(K)   | ELECTRONS<br>2WE(A) | DE(A)     | PROTONS<br>2WI(A) | DI(A)      | IONIZED HELIUM<br>2WI(A) | DI(A)      |
| 5P - 8D     | 2500.  | 0.620E-01           | 0.450E-01 | 0.149E-01         | 0.113E-01  | 0.129E-01                | 0.901E-02  |
| 11811.0A    | 5000.  | 0.682E-01           | 0.441E-01 | 0.162E-01         | 0.130E-01  | 0.139E-01                | 0.104E-01  |
| C= 0.16E+19 | 10000. | 0.760E-01           | 0.334E-01 | 0.178E-01         | 0.147E-01  | 0.151E-01                | 0.118E-01  |
|             | 20000. | 0.876E-01           | 0.200E-01 | 0.195E-01         | 0.167E-01  | 0.164E-01                | 0.134E-01  |
|             | 30000. | 0.926E-01           | 0.176E-01 | 0.207E-01         | 0.179E-01  | 0.173E-01                | 0.144E-01  |
|             | 80000. | 0.962E-01           | 0.540E-02 | 0.239E-01         | 0.212E-01  | 0.197E-01                | 0.170E-01  |
| 5P - 9D     | 2500.  | 0.968E-01           | 0.684E-01 | 0.232E-01*        | 0.175E-01* | 0.200E-01*               | 0.138E-01* |
| 11286.0A    | 5000.  | 0.107               | 0.661E-01 | 0.252E-01         | 0.201E-01  | 0.216E-01*               | 0.160E-01* |
| C= 0.10E+19 | 10000. | 0.121               | 0.480E-01 | 0.277E-01         | 0.230E-01  | 0.234E-01                | 0.184E-01  |
|             | 20000. | 0.139               | 0.294E-01 | 0.304E-01         | 0.261E-01  | 0.255E-01                | 0.209E-01  |
|             | 30000. | 0.146               | 0.250E-01 | 0.322E-01         | 0.280E-01  | 0.269E-01                | 0.224E-01  |
|             | 80000. | 0.150               | 0.715E-02 | 0.373E-01         | 0.331E-01  | 0.308E-01                | 0.266E-01  |
| NE= 0.1E+15 |        |                     |           |                   |            |                          |            |
| 3D - 4P     | 2500.  | 33.5                | -1.79     |                   |            |                          |            |
| 91050.0A    | 5000.  | 32.1                | -1.36     |                   |            |                          |            |
| C= 0.27E+19 | 10000. | 29.8                | -1.14     |                   |            |                          |            |
|             | 20000. | 27.2                | -0.619    | 21.7*             | 21.8*      |                          |            |
|             | 30000. | 25.5                | -0.510    | 20.3*             | 23.8*      |                          |            |
|             | 80000. | 21.3                | -0.242    | 14.3              | 24.7       | 21.5*                    | 22.7*      |
| 3D - 5P     | 2500.  | 0.573E-01           | 0.333E-01 | 0.210E-01         | 0.874E-02  | 0.205E-01                | 0.700E-02  |
| 31453.0A    | 5000.  | 0.655E-01           | 0.397E-01 | 0.214E-01         | 0.987E-02  | 0.207E-01                | 0.792E-02  |
| C= 0.27E+21 | 10000. | 0.770E-01           | 0.404E-01 | 0.220E-01         | 0.111E-01  | 0.211E-01                | 0.892E-02  |
|             | 20000. | 0.942E-01           | 0.364E-01 | 0.227E-01         | 0.125E-01  | 0.215E-01                | 0.100E-01  |
|             | 30000. | 0.107               | 0.311E-01 | 0.232E-01         | 0.134E-01  | 0.218E-01                | 0.108E-01  |
|             | 80000. | 0.140               | 0.240E-01 | 0.247E-01         | 0.158E-01  | 0.228E-01                | 0.127E-01  |
| 3D - 6P     | 2500.  | 0.352E-01           | 0.229E-01 | 0.132E-01         | 0.592E-02  | 0.127E-01                | 0.472E-02  |
| 13384.0A    | 5000.  | 0.410E-01           | 0.270E-01 | 0.135E-01         | 0.672E-02  | 0.129E-01                | 0.538E-02  |
| C= 0.21E+20 | 10000. | 0.480E-01           | 0.263E-01 | 0.139E-01         | 0.761E-02  | 0.132E-01                | 0.610E-02  |
|             | 20000. | 0.572E-01           | 0.243E-01 | 0.145E-01         | 0.857E-02  | 0.136E-01                | 0.688E-02  |
|             | 30000. | 0.640E-01           | 0.218E-01 | 0.149E-01         | 0.919E-02  | 0.138E-01                | 0.738E-02  |
|             | 80000. | 0.788E-01           | 0.167E-01 | 0.160E-01         | 0.108E-01  | 0.146E-01                | 0.872E-02  |
| 3D - 7P     | 2500.  | 0.560E-01           | 0.368E-01 | 0.200E-01         | 0.927E-02  | 0.193E-01                | 0.736E-02  |
| 10482.0A    | 5000.  | 0.655E-01           | 0.419E-01 | 0.206E-01         | 0.106E-01  | 0.197E-01                | 0.846E-02  |
| C= 0.68E+19 | 10000. | 0.772E-01           | 0.417E-01 | 0.214E-01         | 0.121E-01  | 0.201E-01                | 0.964E-02  |
|             | 20000. | 0.925E-01           | 0.343E-01 | 0.223E-01         | 0.136E-01  | 0.207E-01                | 0.109E-01  |
|             | 30000. | 0.103               | 0.298E-01 | 0.229E-01         | 0.146E-01  | 0.211E-01                | 0.118E-01  |
|             | 80000. | 0.123               | 0.197E-01 | 0.248E-01         | 0.173E-01  | 0.224E-01                | 0.139E-01  |
| 3D - 8P     | 2500.  | 0.974E-01           | 0.642E-01 | 0.330E-01         | 0.155E-01  | 0.316E-01                | 0.123E-01  |
| 9348.6A     | 5000.  | 0.114               | 0.690E-01 | 0.342E-01         | 0.180E-01  | 0.324E-01                | 0.143E-01  |
| C= 0.32E+19 | 10000. | 0.136               | 0.648E-01 | 0.355E-01         | 0.205E-01  | 0.332E-01                | 0.164E-01  |
|             | 20000. | 0.164               | 0.504E-01 | 0.372E-01         | 0.233E-01  | 0.343E-01                | 0.186E-01  |
|             | 30000. | 0.183               | 0.410E-01 | 0.383E-01         | 0.251E-01  | 0.351E-01                | 0.201E-01  |
|             | 80000. | 0.212               | 0.220E-01 | 0.417E-01         | 0.297E-01  | 0.374E-01                | 0.238E-01  |

## STARK BROADENING OF K I LINES

NE= 0.1E+15

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS    |            | IONIZED HELIUM |            |
|-------------|--------|-----------|------------|------------|------------|----------------|------------|
|             |        | 2WE(A)    | DE(A)      | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 3D - 9P     | 2500.  | 0.167     | 0.105      | 0.536E-01* | 0.254E-01* |                |            |
| 8764.8A     | 5000.  | 0.196     | 0.111      | 0.557E-01* | 0.297E-01* | 0.524E-01*     | 0.235E-01* |
| C= 0.18E+19 | 10000. | 0.236     | 0.102      | 0.581E-01  | 0.342E-01  | 0.541E-01*     | 0.272E-01* |
|             | 20000. | 0.288     | 0.740E-01  | 0.610E-01  | 0.390E-01  | 0.560E-01*     | 0.311E-01* |
|             | 30000. | 0.318     | 0.556E-01  | 0.630E-01  | 0.419E-01  | 0.574E-01*     | 0.336E-01* |
|             | 80000. | 0.361     | 0.247E-01  | 0.689E-01  | 0.499E-01  | 0.614E-01      | 0.401E-01  |
| 3D - 4F     | 2500.  | 0.264E-01 | -0.110E-01 | 0.595E-02  | -0.371E-02 | 0.550E-02      | -0.297E-02 |
| 15165.0A    | 5000.  | 0.295E-01 | -0.701E-02 | 0.627E-02  | -0.421E-02 | 0.571E-02      | -0.337E-02 |
| C= 0.17E+20 | 10000. | 0.355E-01 | -0.358E-02 | 0.666E-02  | -0.474E-02 | 0.598E-02      | -0.381E-02 |
|             | 20000. | 0.408E-01 | -0.111E-02 | 0.713E-02  | -0.533E-02 | 0.631E-02      | -0.428E-02 |
|             | 30000. | 0.439E-01 | -0.114E-02 | 0.745E-02  | -0.571E-02 | 0.654E-02      | -0.459E-02 |
|             | 80000. | 0.508E-01 | 0.416E-03  | 0.837E-02  | -0.674E-02 | 0.719E-02      | -0.542E-02 |
| 3D - 5F     | 2500.  | 0.235     | 0.286E-01  | 0.839E-01* | 0.681E-01* | 0.674E-01*     | 0.527E-01* |
| 11022.3A    | 5000.  | 0.215     | 0.118E-01  | 0.948E-01* | 0.808E-01* | 0.756E-01*     | 0.636E-01* |
| C= 0.14E+18 | 10000. | 0.196     | 0.687E-02  | 0.108*     | 0.940E-01* | 0.851E-01*     | 0.745E-01* |
|             | 20000. | 0.180     | -0.200E-02 | 0.125*     | 0.109*     | 0.962E-01*     | 0.857E-01* |
|             | 30000. | 0.169     | -0.202E-02 | 0.134      | 0.122      | 0.104*         | 0.927E-01* |
|             | 80000. | 0.147     | -0.975E-03 | 0.136      | 0.151      | 0.127          | 0.113      |
| 4S - 4P     | 2500.  | 0.448E-03 | 0.339E-03  | 0.277E-03  | 0.938E-04  | 0.273E-03      | 0.753E-04  |
| 7676.2A     | 5000.  | 0.509E-03 | 0.401E-03  | 0.280E-03  | 0.106E-03  | 0.275E-03      | 0.848E-04  |
| C= 0.47E+20 | 10000. | 0.624E-03 | 0.454E-03  | 0.284E-03  | 0.119E-03  | 0.277E-03      | 0.953E-04  |
|             | 20000. | 0.825E-03 | 0.461E-03  | 0.290E-03  | 0.133E-03  | 0.281E-03      | 0.107E-03  |
|             | 30000. | 0.973E-03 | 0.410E-03  | 0.294E-03  | 0.143E-03  | 0.283E-03      | 0.115E-03  |
|             | 80000. | 0.139E-02 | 0.285E-03  | 0.306E-03  | 0.168E-03  | 0.291E-03      | 0.135E-03  |
| 4S - 5P     | 2500.  | 0.963E-03 | 0.604E-03  | 0.406E-03  | 0.164E-03  | 0.397E-03      | 0.131E-03  |
| 4045.2A     | 5000.  | 0.110E-02 | 0.719E-03  | 0.414E-03  | 0.185E-03  | 0.401E-03      | 0.148E-03  |
| C= 0.44E+19 | 10000. | 0.126E-02 | 0.777E-03  | 0.424E-03  | 0.208E-03  | 0.407E-03      | 0.167E-03  |
|             | 20000. | 0.148E-02 | 0.763E-03  | 0.436E-03  | 0.234E-03  | 0.415E-03      | 0.188E-03  |
|             | 30000. | 0.164E-02 | 0.670E-03  | 0.445E-03  | 0.251E-03  | 0.420E-03      | 0.202E-03  |
|             | 80000. | 0.206E-02 | 0.492E-03  | 0.472E-03  | 0.296E-03  | 0.438E-03      | 0.238E-03  |
| 4S - 6P     | 2500.  | 0.233E-02 | 0.151E-02  | 0.919E-03  | 0.400E-03  | 0.891E-03      | 0.319E-03  |
| 3446.7A     | 5000.  | 0.271E-02 | 0.175E-02  | 0.941E-03  | 0.454E-03  | 0.905E-03      | 0.363E-03  |
| C= 0.14E+19 | 10000. | 0.315E-02 | 0.183E-02  | 0.969E-03  | 0.514E-03  | 0.922E-03      | 0.412E-03  |
|             | 20000. | 0.373E-02 | 0.171E-02  | 0.100E-02  | 0.579E-03  | 0.944E-03      | 0.465E-03  |
|             | 30000. | 0.414E-02 | 0.150E-02  | 0.103E-02  | 0.621E-03  | 0.960E-03      | 0.498E-03  |
|             | 80000. | 0.505E-02 | 0.107E-02  | 0.110E-02  | 0.733E-03  | 0.101E-02      | 0.589E-03  |
| 4S - 7P     | 2500.  | 0.526E-02 | 0.343E-02  | 0.193E-02  | 0.877E-03  | 0.186E-02      | 0.696E-03  |
| 3217.3A     | 5000.  | 0.615E-02 | 0.394E-02  | 0.198E-02  | 0.100E-02  | 0.189E-02      | 0.801E-03  |
| C= 0.64E+18 | 10000. | 0.723E-02 | 0.384E-02  | 0.205E-02  | 0.114E-02  | 0.194E-02      | 0.912E-03  |
|             | 20000. | 0.864E-02 | 0.333E-02  | 0.214E-02  | 0.129E-02  | 0.199E-02      | 0.103E-02  |
|             | 30000. | 0.961E-02 | 0.282E-02  | 0.220E-02  | 0.138E-02  | 0.203E-02      | 0.111E-02  |
|             | 80000. | 0.114E-01 | 0.184E-02  | 0.237E-02  | 0.164E-02  | 0.215E-02      | 0.131E-02  |



| NE= 0.1E+15 |        |           |           |            |            |                |            |
|-------------|--------|-----------|-----------|------------|------------|----------------|------------|
| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|             |        | 2WE (A)   | DE (A)    | 2WI (A)    | DI (A)     | 2WI (A)        | DI (A)     |
| 4S - 8P     | 2500.  | 0.107E-01 | 0.692E-02 | 0.367E-02  | 0.171E-02  | 0.351E-02*     | 0.135E-02* |
| 3101.9A     | 5000.  | 0.125E-01 | 0.761E-02 | 0.379E-02  | 0.198E-02  | 0.360E-02*     | 0.157E-02* |
| C= 0.36E+18 | 10000. | 0.149E-01 | 0.738E-02 | 0.394E-02  | 0.226E-02  | 0.369E-02      | 0.180E-02  |
|             | 20000. | 0.180E-01 | 0.579E-02 | 0.412E-02  | 0.256E-02  | 0.381E-02      | 0.205E-02  |
|             | 30000. | 0.200E-01 | 0.479E-02 | 0.425E-02  | 0.276E-02  | 0.390E-02      | 0.221E-02  |
|             | 80000. | 0.232E-01 | 0.277E-02 | 0.461E-02  | 0.326E-02  | 0.415E-02      | 0.262E-02  |
| 4S - 9P     | 2500.  | 0.199E-01 | 0.126E-01 | 0.646E-02* | 0.305E-02* |                |            |
| 3034.8A     | 5000.  | 0.235E-01 | 0.133E-01 | 0.671E-02* | 0.356E-02* | 0.632E-02*     | 0.282E-02* |
| C= 0.22E+18 | 10000. | 0.282E-01 | 0.124E-01 | 0.700E-02  | 0.410E-02  | 0.652E-02*     | 0.326E-02* |
|             | 20000. | 0.344E-01 | 0.930E-02 | 0.734E-02  | 0.467E-02  | 0.675E-02*     | 0.373E-02* |
|             | 30000. | 0.380E-01 | 0.760E-02 | 0.758E-02  | 0.503E-02  | 0.691E-02      | 0.403E-02  |
|             | 80000. | 0.431E-01 | 0.395E-02 | 0.828E-02  | 0.599E-02  | 0.739E-02      | 0.480E-02  |
| 4P - 5S     | 2500.  | 0.584E-02 | 0.411E-02 | 0.136E-02  | 0.113E-02  | 0.116E-02      | 0.903E-03  |
| 12492.0A    | 5000.  | 0.672E-02 | 0.489E-02 | 0.150E-02  | 0.127E-02  | 0.126E-02      | 0.102E-02  |
| C= 0.58E+20 | 10000. | 0.748E-02 | 0.573E-02 | 0.165E-02  | 0.143E-02  | 0.138E-02      | 0.115E-02  |
|             | 20000. | 0.844E-02 | 0.566E-02 | 0.182E-02  | 0.161E-02  | 0.151E-02      | 0.129E-02  |
|             | 30000. | 0.900E-02 | 0.513E-02 | 0.193E-02  | 0.172E-02  | 0.160E-02      | 0.139E-02  |
|             | 80000. | 0.115E-01 | 0.361E-02 | 0.224E-02  | 0.203E-02  | 0.184E-02      | 0.163E-02  |
| 4P - 6S     | 2500.  | 0.665E-02 | 0.486E-02 | 0.143E-02  | 0.131E-02  | 0.116E-02      | 0.104E-02  |
| 6929.5A     | 5000.  | 0.765E-02 | 0.571E-02 | 0.161E-02  | 0.148E-02  | 0.130E-02      | 0.119E-02  |
| C= 0.75E+19 | 10000. | 0.824E-02 | 0.625E-02 | 0.180E-02  | 0.168E-02  | 0.145E-02      | 0.135E-02  |
|             | 20000. | 0.916E-02 | 0.619E-02 | 0.202E-02  | 0.189E-02  | 0.163E-02      | 0.152E-02  |
|             | 30000. | 0.950E-02 | 0.554E-02 | 0.216E-02  | 0.202E-02  | 0.174E-02      | 0.162E-02  |
|             | 80000. | 0.117E-01 | 0.413E-02 | 0.254E-02  | 0.239E-02  | 0.204E-02      | 0.192E-02  |
| 4P - 7S     | 2500.  | 0.126E-01 | 0.930E-02 | 0.264E-02  | 0.239E-02  | 0.213E-02      | 0.190E-02  |
| 5795.3A     | 5000.  | 0.151E-01 | 0.110E-01 | 0.297E-02  | 0.273E-02  | 0.239E-02      | 0.218E-02  |
| C= 0.27E+19 | 10000. | 0.154E-01 | 0.110E-01 | 0.333E-02  | 0.310E-02  | 0.268E-02      | 0.248E-02  |
|             | 20000. | 0.170E-01 | 0.103E-01 | 0.374E-02  | 0.350E-02  | 0.301E-02      | 0.281E-02  |
|             | 30000. | 0.184E-01 | 0.895E-02 | 0.400E-02  | 0.375E-02  | 0.322E-02      | 0.301E-02  |
|             | 80000. | 0.224E-01 | 0.642E-02 | 0.471E-02  | 0.444E-02  | 0.379E-02      | 0.356E-02  |
| 4P - 8S     | 2500.  | 0.232E-01 | 0.166E-01 | 0.468E-02  | 0.414E-02  | 0.376E-02      | 0.327E-02  |
| 5334.3A     | 5000.  | 0.260E-01 | 0.190E-01 | 0.525E-02  | 0.477E-02  | 0.423E-02      | 0.379E-02  |
| C= 0.13E+19 | 10000. | 0.298E-01 | 0.189E-01 | 0.590E-02  | 0.544E-02  | 0.474E-02      | 0.435E-02  |
|             | 20000. | 0.323E-01 | 0.153E-01 | 0.662E-02  | 0.617E-02  | 0.533E-02      | 0.494E-02  |
|             | 30000. | 0.360E-01 | 0.127E-01 | 0.709E-02  | 0.663E-02  | 0.570E-02      | 0.531E-02  |
|             | 80000. | 0.425E-01 | 0.762E-02 | 0.835E-02  | 0.785E-02  | 0.671E-02      | 0.630E-02  |
| 4P - 9S     | 2500.  | 0.431E-01 | 0.314E-01 | 0.870E-02  | 0.747E-02  | 0.700E-02*     | 0.585E-02* |
| 5094.3A     | 5000.  | 0.475E-01 | 0.345E-01 | 0.977E-02  | 0.870E-02  | 0.785E-02*     | 0.689E-02* |
| C= 0.76E+18 | 10000. | 0.537E-01 | 0.318E-01 | 0.110E-01  | 0.100E-01  | 0.882E-02      | 0.796E-02  |
|             | 20000. | 0.623E-01 | 0.243E-01 | 0.123E-01  | 0.114E-01  | 0.990E-02      | 0.910E-02  |
|             | 30000. | 0.695E-01 | 0.189E-01 | 0.132E-01  | 0.123E-01  | 0.106E-01      | 0.981E-02  |
|             | 80000. | 0.796E-01 | 0.907E-02 | 0.155E-01  | 0.145E-01  | 0.125E-01      | 0.117E-01  |



## STARK BROADENING OF K I LINES

NE= 0.1E+15

| TRANSITION | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|------------|--------|-----------|-----------|------------|------------|----------------|------------|
|            |        | 2WE (A)   | DE (A)    | 2WI (A)    | DI (A)     | 2WI (A)        | DI (A)     |
| 4P -10S    | 2500.  | 0.730E-01 | 0.512E-01 | 0.146E-01* | 0.121E-01* | 0.118E-01*     | 0.940E-02* |
| 4951.4A    | 5000.  | 0.807E-01 | 0.540E-01 | 0.164E-01* | 0.143E-01* | 0.132E-01*     | 0.113E-01* |
| ☉ 0.48E+18 | 10000. | 0.924E-01 | 0.497E-01 | 0.184E-01  | 0.166E-01  | 0.148E-01*     | 0.132E-01* |
|            | 20000. | 0.111     | 0.357E-01 | 0.207E-01  | 0.190E-01  | 0.166E-01*     | 0.151E-01* |
|            | 30000. | 0.123     | 0.260E-01 | 0.221E-01  | 0.205E-01  | 0.178E-01*     | 0.164E-01* |
|            | 80000. | 0.138     | 0.105E-01 | 0.261E-01  | 0.244E-01  | 0.210E-01      | 0.196E-01  |
| 4P -11S    | 2500.  | 0.119     | 0.840E-01 | 0.230E-01* | 0.183E-01* |                |            |
| 4859.0A    | 5000.  | 0.131     | 0.809E-01 | 0.252E-01* | 0.220E-01* |                |            |
| ☉ 0.33E+18 | 10000. | 0.152     | 0.705E-01 | 0.290E-01* | 0.257E-01* | 0.233E-01*     | 0.204E-01* |
|            | 20000. | 0.187     | 0.490E-01 | 0.326E-01* | 0.296E-01* | 0.262E-01*     | 0.236E-01* |
|            | 30000. | 0.206     | 0.364E-01 | 0.349E-01* | 0.320E-01* | 0.280E-01*     | 0.255E-01* |
|            | 80000. | 0.228     | 0.124E-01 | 0.412E-01  | 0.383E-01  | 0.331E-01*     | 0.307E-01* |
| 4P -12S    | 2500.  | 0.173     | 0.116     |            |            |                |            |
| 4795.7A    | 5000.  | 0.206     | 0.116     |            |            |                |            |
| ☉ 0.24E+18 | 10000. | 0.238     | 0.914E-01 | 0.421E-01* | 0.368E-01* |                |            |
|            | 20000. | 0.298     | 0.622E-01 | 0.472E-01* | 0.425E-01* | 0.380E-01*     | 0.338E-01* |
|            | 30000. | 0.327     | 0.465E-01 | 0.506E-01* | 0.461E-01* | 0.406E-01*     | 0.367E-01* |
|            | 80000. | 0.358     | 0.144E-01 | 0.598E-01* | 0.553E-01* | 0.479E-01*     | 0.442E-01* |
| 4P - 3D    | 2500.  | 0.253E-02 | 0.131E-02 | 0.873E-03  | 0.346E-03  | 0.854E-03      | 0.278E-03  |
| 11745.0A   | 5000.  | 0.271E-02 | 0.144E-02 | 0.888E-03  | 0.389E-03  | 0.863E-03      | 0.313E-03  |
| ☉ 0.44E+20 | 10000. | 0.312E-02 | 0.142E-02 | 0.908E-03  | 0.438E-03  | 0.875E-03      | 0.352E-03  |
|            | 20000. | 0.394E-02 | 0.111E-02 | 0.933E-03  | 0.492E-03  | 0.890E-03      | 0.395E-03  |
|            | 30000. | 0.464E-02 | 0.944E-03 | 0.952E-03  | 0.526E-03  | 0.901E-03      | 0.423E-03  |
|            | 80000. | 0.639E-02 | 0.673E-03 | 0.101E-02  | 0.620E-03  | 0.937E-03      | 0.498E-03  |
| 4P - 4D    | 2500.  | 0.766E-02 | 0.560E-02 | 0.199E-02  | 0.144E-02  | 0.177E-02      | 0.115E-02  |
| 6955.2A    | 5000.  | 0.839E-02 | 0.604E-02 | 0.215E-02  | 0.164E-02  | 0.188E-02      | 0.131E-02  |
| ☉ 0.35E+19 | 10000. | 0.914E-02 | 0.579E-02 | 0.232E-02  | 0.185E-02  | 0.201E-02      | 0.149E-02  |
|            | 20000. | 0.101E-01 | 0.457E-02 | 0.253E-02  | 0.209E-02  | 0.217E-02      | 0.167E-02  |
|            | 30000. | 0.109E-01 | 0.406E-02 | 0.267E-02  | 0.224E-02  | 0.227E-02      | 0.180E-02  |
|            | 80000. | 0.120E-01 | 0.282E-02 | 0.305E-02  | 0.264E-02  | 0.256E-02      | 0.212E-02  |
| 4P - 5D    | 2500.  | 0.166E-01 | 0.123E-01 | 0.422E-02  | 0.304E-02  | 0.372E-02      | 0.241E-02  |
| 5825.3A    | 5000.  | 0.181E-01 | 0.128E-01 | 0.455E-02  | 0.348E-02  | 0.397E-02      | 0.278E-02  |
| ☉ 0.14E+19 | 10000. | 0.197E-01 | 0.122E-01 | 0.494E-02  | 0.396E-02  | 0.425E-02      | 0.316E-02  |
|            | 20000. | 0.221E-01 | 0.922E-02 | 0.540E-02  | 0.448E-02  | 0.460E-02      | 0.359E-02  |
|            | 30000. | 0.236E-01 | 0.775E-02 | 0.570E-02  | 0.480E-02  | 0.482E-02      | 0.386E-02  |
|            | 80000. | 0.254E-01 | 0.453E-02 | 0.654E-02  | 0.568E-02  | 0.546E-02      | 0.456E-02  |
| 4P - 6D    | 2500.  | 0.333E-01 | 0.247E-01 | 0.831E-02  | 0.591E-02  | 0.729E-02*     | 0.466E-02* |
| 5354.1A    | 5000.  | 0.364E-01 | 0.252E-01 | 0.900E-02  | 0.685E-02  | 0.780E-02      | 0.544E-02  |
| ☉ 0.74E+18 | 10000. | 0.398E-01 | 0.225E-01 | 0.980E-02  | 0.783E-02  | 0.839E-02      | 0.625E-02  |
|            | 20000. | 0.452E-01 | 0.164E-01 | 0.107E-01  | 0.890E-02  | 0.909E-02      | 0.712E-02  |
|            | 30000. | 0.483E-01 | 0.128E-01 | 0.113E-01  | 0.958E-02  | 0.955E-02      | 0.767E-02  |
|            | 80000. | 0.512E-01 | 0.581E-02 | 0.130E-01  | 0.114E-01  | 0.108E-01      | 0.911E-02  |

| NE= 0.1E+15        |        |           |           |            |            |                |            |
|--------------------|--------|-----------|-----------|------------|------------|----------------|------------|
| TRANSITION         | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|                    |        | 2WE(A)    | DE(A)     | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 4P - 7D            | 2500.  | 0.624E-01 | 0.466E-01 | 0.153E-01* | 0.106E-01* | 0.133E-01*     | 0.830E-02* |
| 5107.2A            | 5000.  | 0.683E-01 | 0.441E-01 | 0.166E-01* | 0.125E-01* | 0.143E-01*     | 0.988E-02* |
| $\approx$ 0.43E+18 | 10000. | 0.752E-01 | 0.384E-01 | 0.181E-01  | 0.144E-01  | 0.155E-01*     | 0.115E-01* |
|                    | 20000. | 0.863E-01 | 0.273E-01 | 0.199E-01  | 0.165E-01  | 0.168E-01*     | 0.132E-01* |
|                    | 30000. | 0.917E-01 | 0.204E-01 | 0.210E-01  | 0.178E-01  | 0.176E-01      | 0.142E-01  |
|                    | 80000. | 0.960E-01 | 0.736E-02 | 0.242E-01  | 0.212E-01  | 0.201E-01      | 0.170E-01  |
| 4P - 8D            | 2500.  | 0.109     | 0.778E-01 | 0.264E-01* | 0.178E-01* |                |            |
| 4960.2A            | 5000.  | 0.120     | 0.776E-01 | 0.287E-01* | 0.213E-01* |                |            |
| $\approx$ 0.28E+18 | 10000. | 0.134     | 0.615E-01 | 0.314E-01* | 0.249E-01* | 0.267E-01*     | 0.197E-01* |
|                    | 20000. | 0.154     | 0.428E-01 | 0.345E-01* | 0.286E-01* | 0.291E-01*     | 0.228E-01* |
|                    | 30000. | 0.162     | 0.314E-01 | 0.366E-01* | 0.309E-01* | 0.306E-01*     | 0.247E-01* |
|                    | 80000. | 0.168     | 0.986E-02 | 0.423E-01  | 0.370E-01  | 0.349E-01*     | 0.296E-01* |
| 4P - 9D            | 2500.  | 0.180     | 0.127     |            |            |                |            |
| 4865.2A            | 5000.  | 0.199     | 0.122     |            |            |                |            |
| $\approx$ 0.19E+18 | 10000. | 0.224     | 0.923E-01 | 0.515E-01* | 0.403E-01* |                |            |
|                    | 20000. | 0.258     | 0.642E-01 | 0.566E-01* | 0.467E-01* |                |            |
|                    | 30000. | 0.270     | 0.461E-01 | 0.600E-01* | 0.506E-01* |                |            |
|                    | 80000. | 0.277     | 0.134E-01 | 0.695E-01* | 0.607E-01* | 0.573E-01*     | 0.486E-01* |
| 4D - 6P            | 2500.  | 0.675     | 0.173     | 0.231      | 0.390E-01  | 0.230          | 0.312E-01  |
| 62191.0A           | 5000.  | 0.935     | 0.218     | 0.231      | 0.441E-01  | 0.231          | 0.354E-01  |
| $\approx$ 0.28E+21 | 10000. | 1.27      | 0.235     | 0.232      | 0.497E-01  | 0.231          | 0.399E-01  |
|                    | 20000. | 1.66      | 0.206     | 0.233      | 0.559E-01  | 0.231          | 0.449E-01  |
|                    | 30000. | 1.89      | 0.184     | 0.233      | 0.599E-01  | 0.232          | 0.481E-01  |
|                    | 80000. | 2.32      | 0.154     | 0.235      | 0.707E-01  | 0.233          | 0.567E-01  |
| 4D - 7P            | 2500.  | 0.369     | 0.213     | 0.124      | 0.541E-01  | 0.119          | 0.430E-01  |
| 27199.0A           | 5000.  | 0.451     | 0.231     | 0.127      | 0.618E-01  | 0.121          | 0.493E-01  |
| $\approx$ 0.46E+20 | 10000. | 0.561     | 0.225     | 0.131      | 0.701E-01  | 0.124          | 0.561E-01  |
|                    | 20000. | 0.701     | 0.178     | 0.136      | 0.794E-01  | 0.127          | 0.636E-01  |
|                    | 30000. | 0.790     | 0.154     | 0.139      | 0.850E-01  | 0.129          | 0.683E-01  |
|                    | 80000. | 0.941     | 0.945E-01 | 0.150      | 0.101      | 0.136          | 0.807E-01  |
| 4D - 8P            | 2500.  | 0.477     | 0.293     | 0.156      | 0.729E-01  | 0.149*         | 0.575E-01* |
| 20691.0A           | 5000.  | 0.569     | 0.315     | 0.161      | 0.842E-01  | 0.152*         | 0.669E-01* |
| $\approx$ 0.16E+20 | 10000. | 0.690     | 0.293     | 0.167      | 0.961E-01  | 0.156          | 0.768E-01  |
|                    | 20000. | 0.852     | 0.212     | 0.175      | 0.109      | 0.162          | 0.873E-01  |
|                    | 30000. | 0.951     | 0.171     | 0.180      | 0.117      | 0.165          | 0.940E-01  |
|                    | 80000. | 1.10      | 0.868E-01 | 0.196      | 0.139      | 0.176          | 0.112      |
| 4D - 4F            | 2500.  | 4.41      | -2.62     | 0.802      | -0.687     | 0.668          | -0.548     |
| 136923.A           | 5000.  | 4.84      | -2.76     | 0.889      | -0.781     | 0.735          | -0.625     |
| $\approx$ 0.14E+22 | 10000. | 5.27      | -2.28     | 0.987      | -0.885     | 0.812          | -0.708     |
|                    | 20000. | 6.17      | -1.72     | 1.10       | -0.996     | 0.900          | -0.800     |
|                    | 30000. | 6.70      | -1.56     | 1.17       | -1.07      | 0.956          | -0.858     |
|                    | 80000. | 7.37      | -0.953    | 1.37       | -1.26      | 1.11           | -1.01      |

## STARK BROADENING OF K I LINES

NE= 0.1E+15

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS    |            | IONIZED HELIUM |            |
|-------------|--------|-----------|------------|------------|------------|----------------|------------|
|             |        | 2WE(A)    | DE(A)      | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 4D - 5F     | 2500.  | 1.98      | 0.142      | 0.665*     | 0.541*     | 0.533*         | 0.419*     |
| 31162.0A    | 5000.  | 1.84      | -0.352E-02 | 0.752*     | 0.642*     | 0.599*         | 0.505*     |
| C= 0.11E+19 | 10000. | 1.68      | -0.107     | 0.860*     | 0.746*     | 0.674*         | 0.591*     |
|             | 20000. | 1.57      | -0.963E-01 | 0.991      | 0.866      | 0.763*         | 0.681*     |
|             | 30000. | 1.51      | -0.100     | 1.06       | 0.952      | 0.825*         | 0.736*     |
|             | 80000. | 1.33      | -0.642E-01 | 1.07       | 1.20       | 1.01           | 0.897      |
| 5S - 5P     | 2500.  | 0.350E-01 | 0.127E-01  | 0.174E-01  | 0.360E-02  | 0.174E-01      | 0.288E-02  |
| 27114.0A    | 5000.  | 0.416E-01 | 0.120E-01  | 0.175E-01  | 0.405E-02  | 0.174E-01      | 0.325E-02  |
| C= 0.20E+21 | 10000. | 0.550E-01 | 0.767E-02  | 0.176E-01  | 0.455E-02  | 0.175E-01      | 0.366E-02  |
|             | 20000. | 0.767E-01 | 0.485E-02  | 0.177E-01  | 0.512E-02  | 0.175E-01      | 0.411E-02  |
|             | 30000. | 0.913E-01 | 0.402E-02  | 0.177E-01  | 0.548E-02  | 0.175E-01      | 0.441E-02  |
|             | 80000. | 0.123     | 0.272E-02  | 0.180E-01  | 0.646E-02  | 0.177E-01      | 0.519E-02  |
| 5S - 6P     | 2500.  | 0.302E-01 | 0.190E-01  | 0.120E-01  | 0.491E-02  | 0.117E-01      | 0.392E-02  |
| 12531.0A    | 5000.  | 0.352E-01 | 0.215E-01  | 0.123E-01  | 0.558E-02  | 0.119E-01      | 0.446E-02  |
| C= 0.19E+20 | 10000. | 0.420E-01 | 0.217E-01  | 0.126E-01  | 0.632E-02  | 0.120E-01      | 0.506E-02  |
|             | 20000. | 0.514E-01 | 0.176E-01  | 0.130E-01  | 0.711E-02  | 0.123E-01      | 0.571E-02  |
|             | 30000. | 0.585E-01 | 0.153E-01  | 0.133E-01  | 0.762E-02  | 0.125E-01      | 0.612E-02  |
|             | 80000. | 0.732E-01 | 0.116E-01  | 0.141E-01  | 0.900E-02  | 0.130E-01      | 0.723E-02  |
| 5S - 7P     | 2500.  | 0.503E-01 | 0.327E-01  | 0.184E-01  | 0.825E-02  | 0.177E-01      | 0.655E-02  |
| 9951.3A     | 5000.  | 0.588E-01 | 0.367E-01  | 0.189E-01  | 0.944E-02  | 0.181E-01      | 0.753E-02  |
| C= 0.62E+19 | 10000. | 0.699E-01 | 0.369E-01  | 0.195E-01  | 0.107E-01  | 0.185E-01      | 0.858E-02  |
|             | 20000. | 0.844E-01 | 0.299E-01  | 0.203E-01  | 0.121E-01  | 0.190E-01      | 0.973E-02  |
|             | 30000. | 0.946E-01 | 0.247E-01  | 0.209E-01  | 0.130E-01  | 0.193E-01      | 0.105E-01  |
|             | 80000. | 0.113     | 0.160E-01  | 0.225E-01  | 0.154E-01  | 0.204E-01      | 0.124E-01  |
| 5S - 8P     | 2500.  | 0.886E-01 | 0.584E-01  | 0.304E-01  | 0.141E-01  | 0.290E-01*     | 0.111E-01* |
| 8924.4A     | 5000.  | 0.104     | 0.620E-01  | 0.314E-01  | 0.163E-01  | 0.298E-01*     | 0.129E-01* |
| C= 0.29E+19 | 10000. | 0.124     | 0.598E-01  | 0.326E-01  | 0.186E-01  | 0.305E-01      | 0.148E-01  |
|             | 20000. | 0.151     | 0.432E-01  | 0.340E-01  | 0.211E-01  | 0.315E-01      | 0.169E-01  |
|             | 30000. | 0.168     | 0.351E-01  | 0.351E-01  | 0.227E-01  | 0.322E-01      | 0.182E-01  |
|             | 80000. | 0.195     | 0.183E-01  | 0.381E-01  | 0.269E-01  | 0.342E-01      | 0.216E-01  |
| 5S - 9P     | 2500.  | 0.153     | 0.997E-01  | 0.494E-01* | 0.232E-01* |                |            |
| 8390.7A     | 5000.  | 0.180     | 0.104      | 0.513E-01* | 0.272E-01* | 0.483E-01*     | 0.215E-01* |
| C= 0.17E+19 | 10000. | 0.216     | 0.905E-01  | 0.534E-01  | 0.313E-01  | 0.498E-01*     | 0.249E-01* |
|             | 20000. | 0.265     | 0.596E-01  | 0.561E-01  | 0.356E-01  | 0.516E-01*     | 0.285E-01* |
|             | 30000. | 0.292     | 0.505E-01  | 0.579E-01  | 0.384E-01  | 0.528E-01      | 0.307E-01  |
|             | 80000. | 0.332     | 0.210E-01  | 0.632E-01  | 0.457E-01  | 0.564E-01      | 0.367E-01  |
| 5P - 6S     | 2500.  | 0.180     | 0.120      | 0.441E-01  | 0.312E-01  | 0.395E-01      | 0.249E-01  |
| 36529.0A    | 5000.  | 0.209     | 0.142      | 0.473E-01  | 0.353E-01  | 0.418E-01      | 0.283E-01  |
| C= 0.21E+21 | 10000. | 0.247     | 0.146      | 0.511E-01  | 0.399E-01  | 0.445E-01      | 0.320E-01  |
|             | 20000. | 0.299     | 0.126      | 0.554E-01  | 0.449E-01  | 0.477E-01      | 0.361E-01  |
|             | 30000. | 0.344     | 0.110      | 0.583E-01  | 0.482E-01  | 0.499E-01      | 0.387E-01  |
|             | 80000. | 0.445     | 0.868E-01  | 0.664E-01  | 0.568E-01  | 0.560E-01      | 0.457E-01  |

| NE= 0.1E+15 |        |                     |           |                   |            |                          |            |
|-------------|--------|---------------------|-----------|-------------------|------------|--------------------------|------------|
| TRANSITION  | T(K)   | ELECTRONS<br>2WE(A) | DE(A)     | PROTONS<br>2WI(A) | DI(A)      | IONIZED HELIUM<br>2WI(A) | DI(A)      |
| 5P - 7S     | 2500.  | 0.122               | 0.875E-01 | 0.255E-01         | 0.223E-01  | 0.209E-01                | 0.177E-01  |
| 17979.0A    | 5000.  | 0.139               | 0.104     | 0.284E-01         | 0.254E-01  | 0.232E-01                | 0.203E-01  |
| C= 0.26E+20 | 10000. | 0.154               | 0.984E-01 | 0.317E-01         | 0.289E-01  | 0.258E-01                | 0.231E-01  |
|             | 20000. | 0.175               | 0.896E-01 | 0.355E-01         | 0.326E-01  | 0.288E-01                | 0.262E-01  |
|             | 30000. | 0.197               | 0.775E-01 | 0.378E-01         | 0.350E-01  | 0.307E-01                | 0.281E-01  |
|             | 80000. | 0.243               | 0.543E-01 | 0.444E-01         | 0.413E-01  | 0.359E-01                | 0.332E-01  |
| 5P - 8S     | 2500.  | 0.169               | 0.122     | 0.345E-01         | 0.303E-01  | 0.279E-01                | 0.239E-01  |
| 14178.0A    | 5000.  | 0.188               | 0.138     | 0.387E-01         | 0.349E-01  | 0.312E-01                | 0.278E-01  |
| C= 0.93E+19 | 10000. | 0.217               | 0.137     | 0.434E-01         | 0.398E-01  | 0.350E-01                | 0.318E-01  |
|             | 20000. | 0.242               | 0.107     | 0.487E-01         | 0.452E-01  | 0.392E-01                | 0.362E-01  |
|             | 30000. | 0.272               | 0.868E-01 | 0.521E-01         | 0.486E-01  | 0.419E-01                | 0.389E-01  |
|             | 80000. | 0.322               | 0.509E-01 | 0.613E-01         | 0.575E-01  | 0.493E-01                | 0.462E-01  |
| 5P - 9S     | 2500.  | 0.263               | 0.193     | 0.531E-01         | 0.455E-01  | 0.428E-01*               | 0.357E-01* |
| 12600.0A    | 5000.  | 0.290               | 0.208     | 0.596E-01         | 0.530E-01  | 0.480E-01*               | 0.420E-01* |
| C= 0.46E+19 | 10000. | 0.332               | 0.192     | 0.669E-01         | 0.609E-01  | 0.538E-01                | 0.485E-01  |
|             | 20000. | 0.389               | 0.133     | 0.751E-01         | 0.694E-01  | 0.604E-01                | 0.555E-01  |
|             | 30000. | 0.436               | 0.109     | 0.804E-01         | 0.747E-01  | 0.646E-01                | 0.598E-01  |
|             | 80000. | 0.501               | 0.509E-01 | 0.948E-01         | 0.887E-01  | 0.761E-01                | 0.713E-01  |
| 5P -10S     | 2500.  | 0.412               | 0.288     | 0.824E-01*        | 0.683E-01* | 0.663E-01*               | 0.530E-01* |
| 11761.0A    | 5000.  | 0.456               | 0.301     | 0.925E-01*        | 0.807E-01* | 0.744E-01*               | 0.635E-01* |
| C= 0.27E+19 | 10000. | 0.523               | 0.268     | 0.104             | 0.934E-01  | 0.835E-01*               | 0.742E-01* |
|             | 20000. | 0.635               | 0.174     | 0.117             | 0.107      | 0.938E-01*               | 0.853E-01* |
|             | 30000. | 0.706               | 0.141     | 0.125             | 0.115      | 0.100*                   | 0.921E-01* |
|             | 80000. | 0.794               | 0.557E-01 | 0.147             | 0.138      | 0.118                    | 0.110      |
| 5P -11S     | 2500.  | 0.639               | 0.455     | 0.123*            | 0.982E-01* |                          |            |
| 11253.0A    | 5000.  | 0.702               | 0.430     | 0.139*            | 0.118*     |                          |            |
| C= 0.18E+19 | 10000. | 0.817               | 0.362     | 0.156*            | 0.138*     | 0.125*                   | 0.109*     |
|             | 20000. | 1.01                | 0.220     | 0.175*            | 0.159*     | 0.140*                   | 0.126*     |
|             | 30000. | 1.12                | 0.186     | 0.187*            | 0.172*     | 0.150*                   | 0.137*     |
|             | 80000. | 1.24                | 0.641E-01 | 0.221             | 0.205      | 0.177*                   | 0.164*     |
| 5P - 4D     | 2500.  | 0.201               | 0.137     | 0.505E-01         | 0.362E-01  | 0.450E-01                | 0.289E-01  |
| 37255.0A    | 5000.  | 0.232               | 0.135     | 0.543E-01         | 0.411E-01  | 0.477E-01                | 0.329E-01  |
| C= 0.10E+21 | 10000. | 0.271               | 0.101     | 0.587E-01         | 0.464E-01  | 0.509E-01                | 0.373E-01  |
|             | 20000. | 0.341               | 0.787E-01 | 0.639E-01         | 0.523E-01  | 0.548E-01                | 0.420E-01  |
|             | 30000. | 0.379               | 0.673E-01 | 0.673E-01         | 0.560E-01  | 0.573E-01                | 0.450E-01  |
|             | 80000. | 0.446               | 0.391E-01 | 0.769E-01         | 0.661E-01  | 0.645E-01                | 0.532E-01  |
| 5P - 5D     | 2500.  | 0.161               | 0.114     | 0.393E-01         | 0.292E-01  | 0.343E-01                | 0.232E-01  |
| 18272.0A    | 5000.  | 0.176               | 0.121     | 0.426E-01         | 0.335E-01  | 0.368E-01                | 0.267E-01  |
| C= 0.14E+20 | 10000. | 0.195               | 0.106     | 0.465E-01         | 0.380E-01  | 0.397E-01                | 0.304E-01  |
|             | 20000. | 0.227               | 0.791E-01 | 0.509E-01         | 0.431E-01  | 0.430E-01                | 0.345E-01  |
|             | 30000. | 0.247               | 0.670E-01 | 0.539E-01         | 0.461E-01  | 0.453E-01                | 0.371E-01  |
|             | 80000. | 0.273               | 0.352E-01 | 0.621E-01         | 0.546E-01  | 0.515E-01                | 0.439E-01  |

# STARK BROADENING OF K I LINES

NE= 0.1E+15

| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|-------------|--------|-----------|-----------|------------|------------|----------------|------------|
|             |        | 2WE(A)    | DE(A)     | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 5P - 6D     | 2500.  | 0.238     | 0.169     | 0.581E-01  | 0.420E-01  | 0.507E-01*     | 0.331E-01* |
| 14319.0A    | 5000.  | 0.260     | 0.171     | 0.631E-01  | 0.486E-01  | 0.544E-01      | 0.386E-01  |
| C= 0.53E+19 | 10000. | 0.286     | 0.151     | 0.688E-01  | 0.557E-01  | 0.587E-01      | 0.444E-01  |
|             | 20000. | 0.330     | 0.104     | 0.754E-01  | 0.632E-01  | 0.637E-01      | 0.506E-01  |
|             | 30000. | 0.354     | 0.838E-01 | 0.798E-01  | 0.680E-01  | 0.670E-01      | 0.545E-01  |
|             | 80000. | 0.380     | 0.366E-01 | 0.919E-01  | 0.806E-01  | 0.762E-01      | 0.647E-01  |
| 5P - 7D     | 2500.  | 0.385     | 0.287     | 0.932E-01* | 0.655E-01* | 0.810E-01*     | 0.511E-01* |
| 12679.0A    | 5000.  | 0.422     | 0.268     | 0.101*     | 0.770E-01* | 0.872E-01*     | 0.608E-01* |
| C= 0.27E+19 | 10000. | 0.466     | 0.224     | 0.111      | 0.889E-01  | 0.943E-01*     | 0.707E-01* |
|             | 20000. | 0.537     | 0.141     | 0.122      | 0.102      | 0.102*         | 0.811E-01* |
|             | 30000. | 0.572     | 0.118     | 0.129      | 0.109      | 0.108          | 0.875E-01  |
|             | 80000. | 0.603     | 0.424E-01 | 0.149      | 0.130      | 0.123          | 0.105      |
| 5P - 8D     | 2500.  | 0.620     | 0.439     | 0.149*     | 0.101*     |                |            |
| 11811.0A    | 5000.  | 0.682     | 0.438     | 0.162*     | 0.121*     |                |            |
| C= 0.16E+19 | 10000. | 0.760     | 0.334     | 0.178*     | 0.141*     | 0.151*         | 0.112*     |
|             | 20000. | 0.876     | 0.199     | 0.195*     | 0.162*     | 0.164*         | 0.129*     |
|             | 30000. | 0.926     | 0.176     | 0.207*     | 0.175*     | 0.173*         | 0.140*     |
|             | 80000. | 0.962     | 0.540E-01 | 0.239      | 0.210      | 0.197*         | 0.168*     |
| 5P - 9D     | 2500.  | 0.968     | 0.661     |            |            |                |            |
| 11286.0A    | 5000.  | 1.07      | 0.653     |            |            |                |            |
| C= 0.10E+19 | 10000. | 1.21      | 0.478     | 0.276*     | 0.217*     |                |            |
|             | 20000. | 1.39      | 0.294     | 0.304*     | 0.251*     |                |            |
|             | 30000. | 1.46      | 0.250     | 0.322*     | 0.272*     |                |            |
|             | 80000. | 1.50      | 0.715E-01 | 0.373*     | 0.327*     | 0.308*         | 0.261*     |
| NE= 0.1E+16 |        |           |           |            |            |                |            |
| 3D - 5P     | 2500.  | 0.573     | 0.330     | 0.210      | 0.843E-01  | 0.204          | 0.669E-01  |
| 31453.0A    | 5000.  | 0.655     | 0.396     | 0.214      | 0.964E-01  | 0.207          | 0.769E-01  |
| C= 0.27E+21 | 10000. | 0.770     | 0.404     | 0.220      | 0.110      | 0.211          | 0.877E-01  |
|             | 20000. | 0.942     | 0.363     | 0.227      | 0.124      | 0.215          | 0.994E-01  |
|             | 30000. | 1.07      | 0.311     | 0.232      | 0.133      | 0.218          | 0.107      |
|             | 80000. | 1.40      | 0.240     | 0.247      | 0.157      | 0.228          | 0.126      |
| 3D - 6P     | 2500.  | 0.352     | 0.225     | 0.131      | 0.551E-01  | 0.126*         | 0.432E-01* |
| 13384.0A    | 5000.  | 0.410     | 0.269     | 0.135      | 0.643E-01  | 0.129*         | 0.509E-01* |
| C= 0.21E+20 | 10000. | 0.480     | 0.262     | 0.139      | 0.740E-01  | 0.132          | 0.589E-01  |
|             | 20000. | 0.572     | 0.243     | 0.145      | 0.843E-01  | 0.135          | 0.674E-01  |
|             | 30000. | 0.640     | 0.218     | 0.149      | 0.907E-01  | 0.138          | 0.726E-01  |
|             | 80000. | 0.788     | 0.167     | 0.160      | 0.108      | 0.146          | 0.866E-01  |
| 3D - 7P     | 2500.  | 0.560     | 0.357     | 0.197*     | 0.822E-01* |                |            |
| 10482.0A    | 5000.  | 0.655     | 0.414     | 0.205*     | 0.986E-01* | 0.194*         | 0.772E-01* |
| C= 0.68E+19 | 10000. | 0.772     | 0.417     | 0.213*     | 0.115*     | 0.200*         | 0.912E-01* |
|             | 20000. | 0.925     | 0.342     | 0.223*     | 0.133*     | 0.207*         | 0.106*     |
|             | 30000. | 1.03      | 0.297     | 0.229      | 0.143      | 0.211          | 0.114      |
|             | 80000. | 1.23      | 0.197     | 0.248      | 0.171      | 0.224          | 0.137      |



| NE= 0.1E+16 |        |                     |            |                   |            |                          |            |
|-------------|--------|---------------------|------------|-------------------|------------|--------------------------|------------|
| TRANSITION  | T(K)   | ELECTRONS<br>2WE(A) | DE(A)      | PROTONS<br>2WI(A) | DI(A)      | IONIZED HELIUM<br>2WI(A) | DI(A)      |
| 3D - 8P     | 2500.  | 0.974               | 0.618      |                   |            |                          |            |
| 9348.6A     | 5000.  | 1.14                | 0.676      |                   |            |                          |            |
| C= 0.32E+19 | 10000. | 1.36                | 0.641      | 0.354*            | 0.192*     |                          |            |
|             | 20000. | 1.64                | 0.503      | 0.371*            | 0.223*     |                          |            |
|             | 30000. | 1.83                | 0.410      | 0.383*            | 0.242*     | 0.350*                   | 0.193*     |
|             | 80000. | 2.12                | 0.220      | 0.417*            | 0.292*     | 0.374*                   | 0.233*     |
| 3D - 9P     | 2500.  | 1.66                | 0.990      |                   |            |                          |            |
| 8764.8A     | 5000.  | 1.96                | 1.07       |                   |            |                          |            |
| C= 0.18E+19 | 10000. | 2.36                | 1.01       |                   |            |                          |            |
|             | 20000. | 2.88                | 0.740      |                   |            |                          |            |
|             | 30000. | 3.18                | 0.554      | 0.629*            | 0.402*     |                          |            |
|             | 80000. | 3.61                | 0.247      | 0.688*            | 0.488*     |                          |            |
| 3D - 4F     | 2500.  | 0.264               | -0.108     | 0.594E-01         | -0.353E-01 | 0.548E-01                | -0.279E-01 |
| 15165.0A    | 5000.  | 0.295               | -0.695E-01 | 0.627E-01         | -0.407E-01 | 0.571E-01                | -0.324E-01 |
| C= 0.17E+20 | 10000. | 0.355               | -0.354E-01 | 0.666E-01         | -0.465E-01 | 0.598E-01                | -0.371E-01 |
|             | 20000. | 0.408               | -0.110E-01 | 0.713E-01         | -0.527E-01 | 0.631E-01                | -0.422E-01 |
|             | 30000. | 0.439               | -0.114E-01 | 0.745E-01         | -0.567E-01 | 0.654E-01                | -0.454E-01 |
|             | 80000. | 0.508               | 0.416E-02  | 0.837E-01         | -0.671E-01 | 0.719E-01                | -0.539E-01 |
| 3D - 5F     | 2500.  | 2.12                | 0.949E-01  |                   |            |                          |            |
| 11022.3A    | 5000.  | 1.99                | 0.295E-01  |                   |            |                          |            |
| C= 0.14E+18 | 10000. | 1.85                | 0.475E-02  |                   |            |                          |            |
|             | 20000. | 1.72                | -0.303E-01 |                   |            |                          |            |
|             | 30000. | 1.63                | -0.278E-01 |                   |            |                          |            |
|             | 80000. | 1.43                | -0.975E-02 | 1.36*             | 1.47*      |                          |            |
| 4S - 4P     | 2500.  | 0.448E-02           | 0.338E-02  | 0.277E-02         | 0.924E-03  | 0.273E-02                | 0.739E-03  |
| 7676.2A     | 5000.  | 0.509E-02           | 0.400E-02  | 0.280E-02         | 0.105E-02  | 0.275E-02                | 0.839E-03  |
| C= 0.47E+20 | 10000. | 0.624E-02           | 0.453E-02  | 0.284E-02         | 0.118E-02  | 0.277E-02                | 0.948E-03  |
|             | 20000. | 0.825E-02           | 0.461E-02  | 0.290E-02         | 0.133E-02  | 0.280E-02                | 0.107E-02  |
|             | 30000. | 0.973E-02           | 0.410E-02  | 0.294E-02         | 0.142E-02  | 0.283E-02                | 0.114E-02  |
|             | 80000. | 0.139E-01           | 0.285E-02  | 0.306E-02         | 0.168E-02  | 0.291E-02                | 0.135E-02  |
| 4S - 5P     | 2500.  | 0.964E-02           | 0.599E-02  | 0.405E-02         | 0.157E-02  | 0.395E-02                | 0.125E-02  |
| 4045.2A     | 5000.  | 0.110E-01           | 0.718E-02  | 0.413E-02         | 0.180E-02  | 0.401E-02                | 0.144E-02  |
| C= 0.44E+19 | 10000. | 0.126E-01           | 0.776E-02  | 0.424E-02         | 0.205E-02  | 0.407E-02                | 0.164E-02  |
|             | 20000. | 0.148E-01           | 0.763E-02  | 0.436E-02         | 0.232E-02  | 0.415E-02                | 0.186E-02  |
|             | 30000. | 0.164E-01           | 0.670E-02  | 0.445E-02         | 0.249E-02  | 0.420E-02                | 0.200E-02  |
|             | 80000. | 0.206E-01           | 0.492E-02  | 0.472E-02         | 0.295E-02  | 0.438E-02                | 0.237E-02  |
| 4S - 6P     | 2500.  | 0.233E-01           | 0.149E-01  | 0.913E-02         | 0.372E-02  | 0.879E-02*               | 0.291E-02* |
| 3446.7A     | 5000.  | 0.271E-01           | 0.174E-01  | 0.939E-02         | 0.434E-02  | 0.901E-02*               | 0.344E-02* |
| C= 0.14E+19 | 10000. | 0.315E-01           | 0.182E-01  | 0.968E-02         | 0.500E-02  | 0.921E-02                | 0.398E-02  |
|             | 20000. | 0.373E-01           | 0.171E-01  | 0.100E-01         | 0.569E-02  | 0.944E-02                | 0.455E-02  |
|             | 30000. | 0.414E-01           | 0.149E-01  | 0.103E-01         | 0.613E-02  | 0.960E-02                | 0.490E-02  |
|             | 80000. | 0.505E-01           | 0.107E-01  | 0.110E-01         | 0.728E-02  | 0.101E-01                | 0.585E-02  |

# STARK BROADENING OF K I LINES

NE= 0.1E+16

| TRANSITION | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|------------|--------|-----------|-----------|------------|------------|----------------|------------|
|            |        | 2WE(A)    | DE(A)     | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 4S - 7P    | 2500.  | 0.526E-01 | 0.333E-01 | 0.190E-01* | 0.778E-02* |                |            |
| 3217.3A    | 5000.  | 0.615E-01 | 0.391E-01 | 0.197E-01* | 0.933E-02* | 0.187E-01*     | 0.730E-02* |
| ☉ 0.64E+18 | 10000. | 0.723E-01 | 0.382E-01 | 0.205E-01* | 0.109E-01* | 0.193E-01*     | 0.863E-02* |
|            | 20000. | 0.864E-01 | 0.332E-01 | 0.214E-01  | 0.125E-01  | 0.199E-01*     | 0.998E-02* |
|            | 30000. | 0.961E-01 | 0.282E-01 | 0.219E-01  | 0.135E-01  | 0.203E-01      | 0.108E-01  |
|            | 80000. | 0.114     | 0.184E-01 | 0.237E-01  | 0.162E-01  | 0.215E-01      | 0.130E-01  |
| 4S - 8P    | 2500.  | 0.107     | 0.664E-01 |            |            |                |            |
| 3101.9A    | 5000.  | 0.125     | 0.748E-01 |            |            |                |            |
| ☉ 0.36E+18 | 10000. | 0.149     | 0.736E-01 | 0.393E-01* | 0.211E-01* |                |            |
|            | 20000. | 0.180     | 0.578E-01 | 0.412E-01* | 0.246E-01* |                |            |
|            | 30000. | 0.200     | 0.478E-01 | 0.424E-01* | 0.267E-01* | 0.389E-01*     | 0.212E-01* |
|            | 80000. | 0.232     | 0.277E-01 | 0.461E-01* | 0.321E-01* | 0.414E-01*     | 0.257E-01* |
| 4S - 9P    | 2500.  | 0.199     | 0.119     |            |            |                |            |
| 3034.8A    | 5000.  | 0.235     | 0.129     |            |            |                |            |
| ☉ 0.22E+18 | 10000. | 0.282     | 0.123     |            |            |                |            |
|            | 20000. | 0.344     | 0.927E-01 |            |            |                |            |
|            | 30000. | 0.380     | 0.757E-01 | 0.757E-01* | 0.482E-01* |                |            |
|            | 80000. | 0.431     | 0.395E-01 | 0.828E-01* | 0.585E-01* |                |            |
| 4P - 5S    | 2500.  | 0.584E-01 | 0.409E-01 | 0.136E-01  | 0.109E-01  | 0.116E-01      | 0.868E-02  |
| 12492.0A   | 5000.  | 0.672E-01 | 0.488E-01 | 0.149E-01  | 0.125E-01  | 0.126E-01      | 0.995E-02  |
| ☉ 0.58E+20 | 10000. | 0.748E-01 | 0.573E-01 | 0.165E-01  | 0.141E-01  | 0.138E-01      | 0.113E-01  |
|            | 20000. | 0.844E-01 | 0.566E-01 | 0.182E-01  | 0.160E-01  | 0.151E-01      | 0.128E-01  |
|            | 30000. | 0.900E-01 | 0.513E-01 | 0.193E-01  | 0.171E-01  | 0.160E-01      | 0.138E-01  |
|            | 80000. | 0.115     | 0.361E-01 | 0.224E-01  | 0.203E-01  | 0.184E-01      | 0.163E-01  |
| 4P - 6S    | 2500.  | 0.665E-01 | 0.477E-01 | 0.143E-01  | 0.123E-01  | 0.116E-01      | 0.962E-02  |
| 6929.5A    | 5000.  | 0.765E-01 | 0.566E-01 | 0.160E-01  | 0.142E-01  | 0.130E-01      | 0.113E-01  |
| ☉ 0.75E+19 | 10000. | 0.824E-01 | 0.623E-01 | 0.180E-01  | 0.163E-01  | 0.145E-01      | 0.130E-01  |
|            | 20000. | 0.916E-01 | 0.618E-01 | 0.202E-01  | 0.186E-01  | 0.163E-01      | 0.149E-01  |
|            | 30000. | 0.950E-01 | 0.553E-01 | 0.216E-01  | 0.200E-01  | 0.174E-01      | 0.160E-01  |
|            | 80000. | 0.117     | 0.413E-01 | 0.254E-01  | 0.237E-01  | 0.204E-01      | 0.191E-01  |
| 4P - 7S    | 2500.  | 0.126     | 0.907E-01 | 0.264E-01  | 0.214E-01  | 0.213E-01*     | 0.165E-01* |
| 5795.3A    | 5000.  | 0.151     | 0.109     | 0.297E-01  | 0.255E-01  | 0.239E-01*     | 0.200E-01* |
| ☉ 0.27E+19 | 10000. | 0.154     | 0.109     | 0.333E-01  | 0.297E-01  | 0.268E-01      | 0.235E-01  |
|            | 20000. | 0.170     | 0.103     | 0.374E-01  | 0.341E-01  | 0.301E-01      | 0.272E-01  |
|            | 30000. | 0.184     | 0.895E-01 | 0.400E-01  | 0.368E-01  | 0.322E-01      | 0.294E-01  |
|            | 80000. | 0.224     | 0.642E-01 | 0.471E-01  | 0.440E-01  | 0.379E-01      | 0.352E-01  |
| 4P - 8S    | 2500.  | 0.232     | 0.160     | 0.468E-01* | 0.351E-01* |                |            |
| 5334.3A    | 5000.  | 0.260     | 0.186     | 0.525E-01* | 0.432E-01* | 0.422E-01*     | 0.335E-01* |
| ☉ 0.13E+19 | 10000. | 0.298     | 0.188     | 0.590E-01* | 0.512E-01* | 0.474E-01*     | 0.403E-01* |
|            | 20000. | 0.323     | 0.152     | 0.662E-01  | 0.594E-01  | 0.532E-01*     | 0.471E-01* |
|            | 30000. | 0.360     | 0.127     | 0.708E-01  | 0.644E-01  | 0.570E-01*     | 0.513E-01* |
|            | 80000. | 0.425     | 0.762E-01 | 0.835E-01  | 0.774E-01  | 0.671E-01      | 0.619E-01  |

| NE= 0.1E+16 |        |           |           |            |            |                |            |
|-------------|--------|-----------|-----------|------------|------------|----------------|------------|
| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|             |        | 2WE(A)    | DE(A)     | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 4P - 9S     | 2500.  | 0.431     | 0.299     |            |            |                |            |
| 5094.3A     | 5000.  | 0.475     | 0.338     |            |            |                |            |
| C= 0.76E+18 | 10000. | 0.537     | 0.313     | 0.110*     | 0.916E-01* |                |            |
|             | 20000. | 0.623     | 0.243     | 0.123*     | 0.108*     |                |            |
|             | 30000. | 0.695     | 0.189     | 0.132*     | 0.118*     | 0.106*         | 0.932E-01* |
|             | 80000. | 0.796     | 0.907E-01 | 0.155*     | 0.142*     | 0.125*         | 0.114*     |
| 4P -10S     | 2500.  | 0.730     | 0.475     |            |            |                |            |
| 4951.4A     | 5000.  | 0.807     | 0.517     |            |            |                |            |
| C= 0.48E+18 | 10000. | 0.924     | 0.491     |            |            |                |            |
|             | 20000. | 1.11      | 0.357     |            |            |                |            |
|             | 30000. | 1.23      | 0.259     |            |            |                |            |
|             | 80000. | 1.38      | 0.105     | 0.261*     | 0.237*     |                |            |
| 4P -11S     | 2500.  | 1.19      | 0.771     |            |            |                |            |
| 4859.0A     | 5000.  | 1.31      | 0.763     |            |            |                |            |
| C= 0.33E+18 | 10000. | 1.52      | 0.690     |            |            |                |            |
|             | 20000. | 1.87      | 0.487     |            |            |                |            |
|             | 30000. | 2.06      | 0.364     |            |            |                |            |
|             | 80000. | 2.28      | 0.124     |            |            |                |            |
| 4P -12S     | 2500.  | 1.73      | 1.02      |            |            |                |            |
| 4795.7A     | 5000.  | 2.06      | 1.08      |            |            |                |            |
| C= 0.24E+18 | 10000. | 2.38      | 0.885     |            |            |                |            |
|             | 20000. | 2.98      | 0.616     |            |            |                |            |
|             | 30000. | 3.27      | 0.465     |            |            |                |            |
|             | 80000. | 3.58      | 0.144     |            |            |                |            |
| 4P - 3D     | 2500.  | 0.253E-01 | 0.130E-01 | 0.872E-02  | 0.339E-02  | 0.853E-02      | 0.271E-02  |
| 11745.0A    | 5000.  | 0.271E-01 | 0.143E-01 | 0.888E-02  | 0.385E-02  | 0.862E-02      | 0.308E-02  |
| C= 0.44E+20 | 10000. | 0.312E-01 | 0.142E-01 | 0.908E-02  | 0.435E-02  | 0.874E-02      | 0.349E-02  |
|             | 20000. | 0.394E-01 | 0.111E-01 | 0.933E-02  | 0.490E-02  | 0.890E-02      | 0.393E-02  |
|             | 30000. | 0.464E-01 | 0.944E-02 | 0.952E-02  | 0.525E-02  | 0.901E-02      | 0.421E-02  |
|             | 80000. | 0.639E-01 | 0.673E-02 | 0.101E-01  | 0.619E-02  | 0.937E-02      | 0.498E-02  |
| 4P - 4D     | 2500.  | 0.766E-01 | 0.551E-01 | 0.199E-01  | 0.135E-01  | 0.176E-01      | 0.106E-01  |
| 6955.2A     | 5000.  | 0.839E-01 | 0.599E-01 | 0.214E-01  | 0.157E-01  | 0.188E-01      | 0.124E-01  |
| C= 0.35E+19 | 10000. | 0.914E-01 | 0.579E-01 | 0.232E-01  | 0.180E-01  | 0.201E-01      | 0.144E-01  |
|             | 20000. | 0.101     | 0.457E-01 | 0.253E-01  | 0.205E-01  | 0.217E-01      | 0.164E-01  |
|             | 30000. | 0.109     | 0.405E-01 | 0.267E-01  | 0.221E-01  | 0.227E-01      | 0.177E-01  |
|             | 80000. | 0.120     | 0.282E-01 | 0.305E-01  | 0.262E-01  | 0.256E-01      | 0.211E-01  |
| 4P - 5D     | 2500.  | 0.166     | 0.120     | 0.419E-01* | 0.268E-01* | 0.367E-01*     | 0.206E-01  |
| 5825.3A     | 5000.  | 0.181     | 0.126     | 0.454E-01* | 0.323E-01* | 0.395E-01*     | 0.253E-01  |
| C= 0.14E+19 | 10000. | 0.197     | 0.122     | 0.494E-01  | 0.378E-01  | 0.425E-01*     | 0.299E-01  |
|             | 20000. | 0.221     | 0.921E-01 | 0.540E-01  | 0.435E-01  | 0.459E-01*     | 0.346E-01  |
|             | 30000. | 0.236     | 0.774E-01 | 0.570E-01  | 0.470E-01  | 0.482E-01      | 0.375E-01  |
|             | 80000. | 0.254     | 0.453E-01 | 0.654E-01  | 0.562E-01  | 0.546E-01      | 0.450E-01  |

# STARK BROADENING OF K I LINES

NE= 0.1E+16

| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|-------------|--------|-----------|-----------|------------|------------|----------------|------------|
|             |        | 2WE(A)    | DE(A)     | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 4P - 6D     | 2500.  | 0.333     | 0.237     |            |            |                |            |
| 5354.1A     | 5000.  | 0.364     | 0.247     | 0.896E-01* | 0.607E-01* |                |            |
| ☉= 0.74E+18 | 10000. | 0.398     | 0.224     | 0.978E-01* | 0.729E-01* |                |            |
|             | 20000. | 0.452     | 0.164     | 0.107*     | 0.851E-01* | 0.908E-01*     | 0.673E-01* |
|             | 30000. | 0.483     | 0.128     | 0.113      | 0.925E-01  | 0.954E-01*     | 0.735E-01* |
|             | 80000. | 0.512     | 0.581E-01 | 0.130      | 0.112      | 0.108*         | 0.891E-01* |
| 4P - 7D     | 2500.  | 0.624     | 0.440     |            |            |                |            |
| 5107.2A     | 5000.  | 0.682     | 0.424     |            |            |                |            |
| ☉= 0.43E+18 | 10000. | 0.752     | 0.378     |            |            |                |            |
|             | 20000. | 0.863     | 0.272     |            |            |                |            |
|             | 30000. | 0.917     | 0.204     | 0.210*     | 0.169*     |                |            |
|             | 80000. | 0.960     | 0.736E-01 | 0.242*     | 0.206*     |                |            |
| 4P - 8D     | 2500.  | 1.09      | 0.707     |            |            |                |            |
| 4960.2A     | 5000.  | 1.20      | 0.737     |            |            |                |            |
| ☉= 0.28E+18 | 10000. | 1.34      | 0.600     |            |            |                |            |
|             | 20000. | 1.54      | 0.424     |            |            |                |            |
|             | 30000. | 1.62      | 0.314     |            |            |                |            |
|             | 80000. | 1.68      | 0.986E-01 |            |            |                |            |
| 4P - 9D     | 2500.  | 1.80      | 1.11      |            |            |                |            |
| 4865.2A     | 5000.  | 1.99      | 1.12      |            |            |                |            |
| ☉= 0.19E+18 | 10000. | 2.24      | 0.886     |            |            |                |            |
|             | 20000. | 2.58      | 0.640     |            |            |                |            |
|             | 30000. | 2.70      | 0.460     |            |            |                |            |
|             | 80000. | 2.77      | 0.134     |            |            |                |            |
| 4D - 7P     | 2500.  | 3.69      | 2.08      | 1.22*      | 0.484*     |                |            |
| 27199.0A    | 5000.  | 4.51      | 2.29      | 1.26*      | 0.578*     | 1.20*          | 0.453*     |
| ☉= 0.46E+20 | 10000. | 5.61      | 2.25      | 1.30*      | 0.673*     | 1.24*          | 0.533*     |
|             | 20000. | 7.01      | 1.78      | 1.36       | 0.772      | 1.27*          | 0.615*     |
|             | 30000. | 7.90      | 1.54      | 1.39       | 0.834      | 1.29*          | 0.666*     |
|             | 80000. | 9.41      | 0.945     | 1.50       | 0.996      | 1.36           | 0.798      |
| 4D - 8P     | 2500.  | 4.77      | 2.81      |            |            |                |            |
| 20691.0A    | 5000.  | 5.69      | 3.12      |            |            |                |            |
| ☉= 0.16E+20 | 10000. | 6.90      | 2.92      | 1.66*      | 0.901*     |                |            |
|             | 20000. | 8.52      | 2.12      | 1.74*      | 1.05*      |                |            |
|             | 30000. | 9.51      | 1.71      | 1.80*      | 1.14*      | 1.65*          | 0.904*     |
|             | 80000. | 11.0      | 0.868     | 1.96       | 1.37       | 1.76*          | 1.09*      |
| 5S - 5P     | 2500.  | 0.350     | 0.126     | 0.174      | 0.350E-01  | 0.173          | 0.278E-01  |
| 27114.0A    | 5000.  | 0.416     | 0.119     | 0.175      | 0.398E-01  | 0.174          | 0.318E-01  |
| ☉= 0.20E+21 | 10000. | 0.550     | 0.766E-01 | 0.176      | 0.451E-01  | 0.174          | 0.361E-01  |
|             | 20000. | 0.767     | 0.485E-01 | 0.177      | 0.509E-01  | 0.175          | 0.409E-01  |
|             | 30000. | 0.913     | 0.402E-01 | 0.177      | 0.545E-01  | 0.175          | 0.438E-01  |
|             | 80000. | 1.23      | 0.272E-01 | 0.180      | 0.645E-01  | 0.177          | 0.518E-01  |

| NE= 0.1E+16        |        |           |       |         |            |                |            |
|--------------------|--------|-----------|-------|---------|------------|----------------|------------|
| TRANSITION         | T(K)   | ELECTRONS |       | PROTONS |            | IONIZED HELIUM |            |
|                    |        | 2WE(A)    | DE(A) | 2WI(A)  | DI(A)      | 2WI(A)         | DI(A)      |
| 5S - 6P            | 2500.  | 0.302     | 0.186 | 0.119   | 0.458E-01  | 0.115*         | 0.359E-01* |
| 12531.0A           | 5000.  | 0.352     | 0.213 | 0.122   | 0.535E-01  | 0.118*         | 0.423E-01* |
| $\approx 0.19E+20$ | 10000. | 0.420     | 0.217 | 0.126   | 0.614E-01  | 0.120          | 0.489E-01  |
|                    | 20000. | 0.514     | 0.176 | 0.130   | 0.699E-01  | 0.123          | 0.559E-01  |
|                    | 30000. | 0.585     | 0.153 | 0.132   | 0.753E-01  | 0.125          | 0.603E-01  |
|                    | 80000. | 0.732     | 0.116 | 0.141   | 0.894E-01  | 0.130          | 0.719E-01  |
| 5S - 7P            | 2500.  | 0.503     | 0.317 | 0.181*  | 0.732E-01* |                |            |
| 9951.3A            | 5000.  | 0.588     | 0.361 | 0.188*  | 0.878E-01* | 0.178*         | 0.688E-01* |
| $\approx 0.62E+19$ | 10000. | 0.699     | 0.367 | 0.195*  | 0.103*     | 0.184*         | 0.812E-01* |
|                    | 20000. | 0.844     | 0.298 | 0.203   | 0.118      | 0.189*         | 0.939E-01* |
|                    | 30000. | 0.946     | 0.247 | 0.208   | 0.127      | 0.193*         | 0.102*     |
|                    | 80000. | 1.13      | 0.160 | 0.225   | 0.152      | 0.204          | 0.122      |
| 5S - 8P            | 2500.  | 0.886     | 0.560 |         |            |                |            |
| 8924.4A            | 5000.  | 1.04      | 0.604 |         |            |                |            |
| $\approx 0.29E+19$ | 10000. | 1.24      | 0.592 | 0.324*  | 0.174*     |                |            |
|                    | 20000. | 1.51      | 0.430 | 0.340*  | 0.202*     |                |            |
|                    | 30000. | 1.68      | 0.350 | 0.350*  | 0.220*     | 0.321*         | 0.175*     |
|                    | 80000. | 1.95      | 0.183 | 0.381*  | 0.264*     | 0.342*         | 0.211*     |
| 5S - 9P            | 2500.  | 1.53      | 0.940 |         |            |                |            |
| 8390.7A            | 5000.  | 1.80      | 0.998 |         |            |                |            |
| $\approx 0.17E+19$ | 10000. | 2.16      | 0.887 |         |            |                |            |
|                    | 20000. | 2.65      | 0.591 |         |            |                |            |
|                    | 30000. | 2.92      | 0.505 | 0.578*  | 0.367*     |                |            |
|                    | 80000. | 3.32      | 0.210 | 0.632*  | 0.446*     |                |            |
| 5P - 6S            | 2500.  | 1.80      | 1.19  | 0.441   | 0.294      | 0.394          | 0.231      |
| 36529.0A           | 5000.  | 2.09      | 1.41  | 0.473   | 0.340      | 0.417          | 0.270      |
| $\approx 0.21E+21$ | 10000. | 2.47      | 1.46  | 0.510   | 0.390      | 0.445          | 0.311      |
|                    | 20000. | 2.99      | 1.26  | 0.554   | 0.443      | 0.477          | 0.354      |
|                    | 30000. | 3.44      | 1.09  | 0.583   | 0.477      | 0.499          | 0.382      |
|                    | 80000. | 4.45      | 0.868 | 0.664   | 0.565      | 0.560          | 0.454      |
| 5P - 7S            | 2500.  | 1.22      | 0.853 | 0.255   | 0.200      | 0.209*         | 0.154*     |
| 17979.0A           | 5000.  | 1.39      | 1.03  | 0.284   | 0.238      | 0.232*         | 0.187*     |
| $\approx 0.26E+20$ | 10000. | 1.54      | 0.977 | 0.317   | 0.277      | 0.258          | 0.220      |
|                    | 20000. | 1.75      | 0.895 | 0.354   | 0.318      | 0.288          | 0.253      |
|                    | 30000. | 1.97      | 0.775 | 0.378   | 0.343      | 0.307          | 0.274      |
|                    | 80000. | 2.43      | 0.543 | 0.444   | 0.410      | 0.359          | 0.328      |
| 5P - 8S            | 2500.  | 1.69      | 1.17  | 0.345*  | 0.256*     |                |            |
| 14178.0A           | 5000.  | 1.88      | 1.35  | 0.387*  | 0.316*     | 0.312*         | 0.244*     |
| $\approx 0.93E+19$ | 10000. | 2.17      | 1.36  | 0.434*  | 0.375*     | 0.350*         | 0.295*     |
|                    | 20000. | 2.42      | 1.07  | 0.487*  | 0.435*     | 0.392*         | 0.345*     |
|                    | 30000. | 2.72      | 0.866 | 0.521   | 0.471      | 0.419*         | 0.375*     |
|                    | 80000. | 3.22      | 0.509 | 0.613   | 0.566      | 0.493          | 0.453      |



# STARK BROADENING OF K I LINES

NE= 0.1E+16

| TRANSITION  | T (K)  | ELECTRONS |        | PROTONS |        | IONIZED HELIUM |        |
|-------------|--------|-----------|--------|---------|--------|----------------|--------|
|             |        | 2WE (A)   | DE (A) | 2WI (A) | DI (A) | 2WI (A)        | DI (A) |
| 5P - 9S     | 2500.  | 2.63      | 1.83   |         |        |                |        |
| 12600.0A    | 5000.  | 2.90      | 2.01   |         |        |                |        |
| C= 0.46E+19 | 10000. | 3.32      | 1.89   | 0.669*  | 0.558* |                |        |
|             | 20000. | 3.89      | 1.33   | 0.751*  | 0.658* |                |        |
|             | 30000. | 4.36      | 1.09   | 0.803*  | 0.717* | 0.646*         | 0.568* |
|             | 80000. | 5.01      | 0.509  | 0.947*  | 0.869* | 0.761*         | 0.693* |
| 5P -10S     | 2500.  | 4.12      | 2.67   |         |        |                |        |
| 11761.0A    | 5000.  | 4.56      | 2.87   |         |        |                |        |
| C= 0.27E+19 | 10000. | 5.23      | 2.62   |         |        |                |        |
|             | 20000. | 6.35      | 1.72   |         |        |                |        |
|             | 30000. | 7.06      | 1.41   |         |        |                |        |
|             | 80000. | 7.94      | 0.557  | 1.47*   | 1.34*  |                |        |
| 5P -11S     | 2500.  | 6.39      | 4.14   |         |        |                |        |
| 11253.0A    | 5000.  | 7.02      | 4.02   |         |        |                |        |
| C= 0.18E+19 | 10000. | 8.17      | 3.48   |         |        |                |        |
|             | 20000. | 10.1      | 2.15   |         |        |                |        |
|             | 30000. | 11.2      | 1.84   |         |        |                |        |
|             | 80000. | 12.4      | 0.641  |         |        |                |        |
| 5P - 4D     | 2500.  | 2.01      | 1.35   | 0.504   | 0.340  | 0.448          | 0.267  |
| 37255.0A    | 5000.  | 2.32      | 1.34   | 0.542   | 0.395  | 0.476          | 0.313  |
| C= 0.10E+21 | 10000. | 2.71      | 1.01   | 0.587   | 0.453  | 0.509          | 0.361  |
|             | 20000. | 3.41      | 0.786  | 0.639   | 0.515  | 0.547          | 0.412  |
|             | 30000. | 3.79      | 0.673  | 0.673   | 0.554  | 0.573          | 0.444  |
|             | 80000. | 4.46      | 0.391  | 0.769   | 0.658  | 0.645          | 0.528  |
| 5P - 5D     | 2500.  | 1.61      | 1.11   | 0.391*  | 0.259* | 0.339*         | 0.198* |
| 18272.0A    | 5000.  | 1.76      | 1.19   | 0.425*  | 0.311* | 0.366*         | 0.243* |
| C= 0.14E+20 | 10000. | 1.95      | 1.05   | 0.464   | 0.363  | 0.396*         | 0.287* |
|             | 20000. | 2.27      | 0.790  | 0.509   | 0.418  | 0.430*         | 0.333* |
|             | 30000. | 2.47      | 0.670  | 0.539   | 0.452  | 0.452          | 0.360  |
|             | 80000. | 2.73      | 0.352  | 0.621   | 0.540  | 0.515          | 0.433  |
| 5P - 6D     | 2500.  | 2.38      | 1.61   |         |        |                |        |
| 14319.0A    | 5000.  | 2.60      | 1.66   | 0.628*  | 0.432* |                |        |
| C= 0.53E+19 | 10000. | 2.86      | 1.48   | 0.687*  | 0.518* |                |        |
|             | 20000. | 3.30      | 1.04   | 0.754*  | 0.605* | 0.636*         | 0.479* |
|             | 30000. | 3.54      | 0.836  | 0.797*  | 0.657* | 0.669*         | 0.522* |
|             | 80000. | 3.80      | 0.366  | 0.919   | 0.792  | 0.762*         | 0.633* |
| 5P - 7D     | 2500.  | 3.85      | 2.69   |         |        |                |        |
| 12679.0A    | 5000.  | 4.22      | 2.56   |         |        |                |        |
| C= 0.27E+19 | 10000. | 4.66      | 2.18   |         |        |                |        |
|             | 20000. | 5.37      | 1.39   |         |        |                |        |
|             | 30000. | 5.72      | 1.17   | 1.29*   | 1.04*  |                |        |
|             | 80000. | 6.03      | 0.424  | 1.48*   | 1.27*  |                |        |

| NE= 0.1E+16 |        |           |           |            |            |                |            |
|-------------|--------|-----------|-----------|------------|------------|----------------|------------|
| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|             |        | 2WE(A)    | DE(A)     | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 5P - 8D     | 2500.  | 6.20      | 3.99      |            |            |                |            |
| 11811.0A    | 5000.  | 6.81      | 4.11      |            |            |                |            |
| C= 0.16E+19 | 10000. | 7.60      | 3.21      |            |            |                |            |
|             | 20000. | 8.76      | 1.95      |            |            |                |            |
|             | 30000. | 9.25      | 1.75      |            |            |                |            |
|             | 80000. | 9.62      | 0.540     |            |            |                |            |
| 5P - 9D     | 2500.  | 9.67      | 5.77      |            |            |                |            |
| 11286.0A    | 5000.  | 10.7      | 5.96      |            |            |                |            |
| C= 0.10E+19 | 10000. | 12.1      | 4.48      |            |            |                |            |
|             | 20000. | 13.9      | 2.85      |            |            |                |            |
|             | 30000. | 14.6      | 2.48      |            |            |                |            |
|             | 80000. | 15.0      | 0.715     |            |            |                |            |
| NE= 0.1E+17 |        |           |           |            |            |                |            |
| 3D - 5P     | 2500.  | 5.73      | 3.20      | 2.06*      | 0.747*     | 1.96*          | 0.573*     |
| 31453.0A    | 5000.  | 6.55      | 3.90      | 2.13       | 0.897      | 2.04*          | 0.702*     |
| C= 0.27E+21 | 10000. | 7.69      | 4.02      | 2.19       | 1.05       | 2.10*          | 0.829*     |
|             | 20000. | 9.42      | 3.63      | 2.27       | 1.20       | 2.15           | 0.959      |
|             | 30000. | 10.7      | 3.11      | 2.32       | 1.30       | 2.18           | 1.04       |
|             | 80000. | 14.0      | 2.40      | 2.47       | 1.56       | 2.28           | 1.25       |
| 3D - 6P     | 2500.  | 3.52      | 2.13      |            |            |                |            |
| 13384.0A    | 5000.  | 4.10      | 2.59      | 1.32*      | 0.552*     |                |            |
| C= 0.21E+20 | 10000. | 4.80      | 2.57      | 1.38*      | 0.675*     |                |            |
|             | 20000. | 5.72      | 2.42      | 1.44*      | 0.797*     | 1.35*          | 0.628*     |
|             | 30000. | 6.40      | 2.18      | 1.48*      | 0.870*     | 1.38*          | 0.689*     |
|             | 80000. | 7.88      | 1.67      | 1.60       | 1.05       | 1.45*          | 0.842*     |
| 3D - 4F     | 2500.  | 2.64      | -1.03     | 0.583*     | -0.298*    | 0.527*         | -0.224*    |
| 15165.0A    | 5000.  | 2.95      | -0.658    | 0.623*     | -0.368*    | 0.563*         | -0.285*    |
| C= 0.17E+20 | 10000. | 3.55      | -0.334    | 0.665      | -0.437     | 0.595*         | -0.344*    |
|             | 20000. | 4.08      | -0.107    | 0.713      | -0.507     | 0.630*         | -0.402*    |
|             | 30000. | 4.39      | -0.111    | 0.745      | -0.550     | 0.653          | -0.438     |
|             | 80000. | 5.08      | 0.416E-01 | 0.837      | -0.661     | 0.719          | -0.529     |
| 4S - 4P     | 2500.  | 0.448E-01 | 0.334E-01 | 0.276E-01  | 0.881E-02  | 0.270E-01*     | 0.696E-02* |
| 7676.2A     | 5000.  | 0.509E-01 | 0.398E-01 | 0.280E-01  | 0.101E-01  | 0.274E-01*     | 0.808E-02* |
| C= 0.47E+20 | 10000. | 0.624E-01 | 0.453E-01 | 0.284E-01  | 0.116E-01  | 0.277E-01*     | 0.925E-02* |
|             | 20000. | 0.825E-01 | 0.461E-01 | 0.290E-01  | 0.131E-01  | 0.280E-01      | 0.105E-01  |
|             | 30000. | 0.973E-01 | 0.409E-01 | 0.294E-01  | 0.141E-01  | 0.283E-01      | 0.113E-01  |
|             | 80000. | 0.139     | 0.285E-01 | 0.306E-01  | 0.167E-01  | 0.291E-01      | 0.134E-01  |
| 4S - 5P     | 2500.  | 0.962E-01 | 0.580E-01 | 0.396E-01* | 0.138E-01* | 0.377E-01*     | 0.106E-01* |
| 4045.2A     | 5000.  | 0.110     | 0.704E-01 | 0.410E-01  | 0.167E-01  | 0.394E-01*     | 0.130E-01* |
| C= 0.44E+19 | 10000. | 0.126     | 0.768E-01 | 0.422E-01  | 0.195E-01  | 0.405E-01*     | 0.154E-01* |
|             | 20000. | 0.148     | 0.761E-01 | 0.436E-01  | 0.225E-01  | 0.414E-01      | 0.179E-01  |
|             | 30000. | 0.164     | 0.669E-01 | 0.445E-01  | 0.243E-01  | 0.420E-01      | 0.194E-01  |
|             | 80000. | 0.206     | 0.492E-01 | 0.472E-01  | 0.292E-01  | 0.438E-01      | 0.233E-01  |

# STARK BROADENING OF K I LINES

NE= 0.1E+17

| TRANSITION  | T(K)   | ELECTRONS |        | PROTONS    |            | IONIZED HELIUM |            |
|-------------|--------|-----------|--------|------------|------------|----------------|------------|
|             |        | 2WE(A)    | DE(A)  | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 4S - 6P     | 2500.  | 0.233     | 0.140  |            |            |                |            |
| 3446.7A     | 5000.  | 0.271     | 0.167  |            |            |                |            |
| C= 0.14E+19 | 10000. | 0.315     | 0.179  | 0.960E-01* | 0.456E-01* |                |            |
|             | 20000. | 0.373     | 0.169  | 0.100*     | 0.538E-01* |                |            |
|             | 30000. | 0.414     | 0.149  | 0.103*     | 0.587E-01* | 0.957E-01*     | 0.465E-01* |
|             | 80000. | 0.505     | 0.107  | 0.110      | 0.712E-01  | 0.101*         | 0.569E-01* |
| 4S - 7P     | 2500.  | 0.525     | 0.301  |            |            |                |            |
| 3217.3A     | 5000.  | 0.614     | 0.369  |            |            |                |            |
| C= 0.64E+18 | 10000. | 0.723     | 0.367  |            |            |                |            |
|             | 20000. | 0.864     | 0.326  |            |            |                |            |
|             | 30000. | 0.961     | 0.279  |            |            |                |            |
|             | 80000. | 1.14      | 0.184  | 0.237*     | 0.156*     |                |            |
| 4S - 8P     | 2500.  | 1.07      | 0.571  |            |            |                |            |
| 3101.9A     | 5000.  | 1.25      | 0.681  |            |            |                |            |
| C= 0.36E+18 | 10000. | 1.49      | 0.694  |            |            |                |            |
|             | 20000. | 1.80      | 0.559  |            |            |                |            |
|             | 30000. | 2.00      | 0.468  |            |            |                |            |
|             | 80000. | 2.32      | 0.277  |            |            |                |            |
| 4S - 9P     | 2500.  | 1.98*     | 0.945* |            |            |                |            |
| 3034.8A     | 5000.  | 2.34*     | 1.12*  |            |            |                |            |
| C= 0.22E+18 | 10000. | 2.82      | 1.12   |            |            |                |            |
|             | 20000. | 3.44      | 0.874  |            |            |                |            |
|             | 30000. | 3.80      | 0.732  |            |            |                |            |
|             | 80000. | 4.31      | 0.395  |            |            |                |            |
| 4P - 5S     | 2500.  | 0.583     | 0.397  | 0.136      | 0.980E-01  | 0.115          | 0.756E-01  |
| 12492.0A    | 5000.  | 0.672     | 0.481  | 0.149      | 0.117      | 0.126          | 0.916E-01  |
| C= 0.58E+20 | 10000. | 0.748     | 0.572  | 0.165      | 0.136      | 0.138          | 0.108      |
|             | 20000. | 0.844     | 0.566  | 0.182      | 0.156      | 0.151          | 0.124      |
|             | 30000. | 0.900     | 0.513  | 0.193      | 0.168      | 0.160          | 0.134      |
|             | 80000. | 1.15      | 0.361  | 0.224      | 0.201      | 0.184          | 0.161      |
| 4P - 6S     | 2500.  | 0.665     | 0.452  | 0.143*     | 0.969E-01* | 0.115*         | 0.706E-01* |
| 6929.5A     | 5000.  | 0.765     | 0.548  | 0.160*     | 0.124*     | 0.129*         | 0.948E-01* |
| C= 0.75E+19 | 10000. | 0.823     | 0.612  | 0.180*     | 0.151*     | 0.145*         | 0.117*     |
|             | 20000. | 0.916     | 0.615  | 0.202      | 0.177      | 0.163*         | 0.140*     |
|             | 30000. | 0.950     | 0.552  | 0.216      | 0.193      | 0.174*         | 0.153*     |
|             | 80000. | 1.17      | 0.413  | 0.254      | 0.233      | 0.204          | 0.186      |
| 4P - 7S     | 2500.  | 1.26      | 0.828  |            |            |                |            |
| 5795.3A     | 5000.  | 1.51      | 1.03   |            |            |                |            |
| C= 0.27E+19 | 10000. | 1.54      | 1.05   | 0.333*     | 0.258*     |                |            |
|             | 20000. | 1.70      | 1.02   | 0.374*     | 0.313*     |                |            |
|             | 30000. | 1.84      | 0.888  | 0.400*     | 0.346*     |                |            |
|             | 80000. | 2.24      | 0.642  | 0.471*     | 0.425*     | 0.379*         | 0.338*     |

| NE= 0.1E+17        |        |           |           |           |           |                |           |
|--------------------|--------|-----------|-----------|-----------|-----------|----------------|-----------|
| TRANSITION         | T(K)   | ELECTRONS |           | PROTONS   |           | IONIZED HELIUM |           |
|                    |        | 2WE(A)    | DE(A)     | 2WI(A)    | DI(A)     | 2WI(A)         | DI(A)     |
| 4P - 8S            | 2500.  | 2.32      | 1.40      |           |           |                |           |
| 5334.3A            | 5000.  | 2.60      | 1.72      |           |           |                |           |
| $\zeta = 0.13E+19$ | 10000. | 2.98      | 1.79      |           |           |                |           |
|                    | 20000. | 3.23      | 1.49      |           |           |                |           |
|                    | 30000. | 3.60      | 1.25      |           |           |                |           |
|                    | 80000. | 4.25      | 0.761     | 0.835*    | 0.738*    |                |           |
| 4P - 9S            | 2500.  | 4.30*     | 2.45*     |           |           |                |           |
| 5094.3A            | 5000.  | 4.75      | 3.00      |           |           |                |           |
| $\zeta = 0.76E+18$ | 10000. | 5.37      | 2.88      |           |           |                |           |
|                    | 20000. | 6.23      | 2.31      |           |           |                |           |
|                    | 30000. | 6.95      | 1.83      |           |           |                |           |
|                    | 80000. | 7.96      | 0.903     |           |           |                |           |
| 4P - 10S           | 2500.  | 7.21*     | 3.49*     |           |           |                |           |
| 4951.4A            | 5000.  | 8.03*     | 4.29*     |           |           |                |           |
| $\zeta = 0.48E+18$ | 10000. | 9.21      | 4.32      |           |           |                |           |
|                    | 20000. | 11.1      | 3.37      |           |           |                |           |
|                    | 30000. | 12.3      | 2.45      |           |           |                |           |
|                    | 80000. | 13.8      | 1.04      |           |           |                |           |
| 4P - 3D            | 2500.  | 0.253     | 0.128     | 0.867E-01 | 0.319E-01 | 0.843E-01      | 0.251E-01 |
| 11745.0A           | 5000.  | 0.271     | 0.142     | 0.886E-01 | 0.370E-01 | 0.859E-01      | 0.294E-01 |
| $\zeta = 0.44E+20$ | 10000. | 0.312     | 0.142     | 0.907E-01 | 0.424E-01 | 0.873E-01      | 0.338E-01 |
|                    | 20000. | 0.394     | 0.111     | 0.933E-01 | 0.483E-01 | 0.890E-01      | 0.386E-01 |
|                    | 30000. | 0.464     | 0.943E-01 | 0.952E-01 | 0.519E-01 | 0.901E-01      | 0.416E-01 |
|                    | 80000. | 0.639     | 0.673E-01 | 0.101     | 0.616E-01 | 0.937E-01      | 0.495E-01 |
| 4P - 4D            | 2500.  | 0.766     | 0.522     | 0.195*    | 0.105*    |                |           |
| 6955.2A            | 5000.  | 0.839     | 0.578     | 0.213*    | 0.136*    | 0.185*         | 0.103*    |
| $\zeta = 0.35E+19$ | 10000. | 0.914     | 0.567     | 0.232*    | 0.165*    | 0.200*         | 0.129*    |
|                    | 20000. | 1.01      | 0.453     | 0.253*    | 0.195*    | 0.216*         | 0.154*    |
|                    | 30000. | 1.09      | 0.403     | 0.267     | 0.212     | 0.227*         | 0.168*    |
|                    | 80000. | 1.20      | 0.282     | 0.305     | 0.257     | 0.256          | 0.205     |
| 4P - 5D            | 2500.  | 1.66      | 1.09      |           |           |                |           |
| 5825.3A            | 5000.  | 1.81      | 1.18      |           |           |                |           |
| $\zeta = 0.14E+19$ | 10000. | 1.97      | 1.17      |           |           |                |           |
|                    | 20000. | 2.21      | 0.903     |           |           |                |           |
|                    | 30000. | 2.36      | 0.763     | 0.569*    | 0.437*    |                |           |
|                    | 80000. | 2.54      | 0.452     | 0.653*    | 0.542*    |                |           |
| 4P - 6D            | 2500.  | 3.33      | 2.02      |           |           |                |           |
| 5354.1A            | 5000.  | 3.63      | 2.22      |           |           |                |           |
| $\zeta = 0.74E+18$ | 10000. | 3.98      | 2.07      |           |           |                |           |
|                    | 20000. | 4.52      | 1.58      |           |           |                |           |
|                    | 30000. | 4.83      | 1.25      |           |           |                |           |
|                    | 80000. | 5.12      | 0.578     |           |           |                |           |

# STARK BROADENING OF K I LINES

| NE= 0.1E+17 |        |           |        |         |            |                |            |
|-------------|--------|-----------|--------|---------|------------|----------------|------------|
| TRANSITION  | T(K)   | ELECTRONS |        | PROTONS |            | IONIZED HELIUM |            |
|             |        | 2WE (A)   | DE (A) | 2WI (A) | DI (A)     | 2WI (A)        | DI (A)     |
| 4P - 7D     | 2500.  | 6.16      | 3.41   |         |            |                |            |
| 5107.2A     | 5000.  | 6.78      | 3.54   |         |            |                |            |
| C= 0.43E+18 | 10000. | 7.49      | 3.32   |         |            |                |            |
|             | 20000. | 8.61      | 2.55   |         |            |                |            |
|             | 30000. | 9.15      | 1.93   |         |            |                |            |
|             | 80000. | 9.59      | 0.725  |         |            |                |            |
| 5S - 5P     | 2500.  | 3.50      | 1.23   | 1.70*   | 0.320*     | 1.65*          | 0.249*     |
| 27114.0A    | 5000.  | 4.16      | 1.17   | 1.73    | 0.377      | 1.71*          | 0.298*     |
| C= 0.20E+21 | 10000. | 5.50      | 0.756  | 1.75    | 0.436      | 1.73*          | 0.347*     |
|             | 20000. | 7.67      | 0.480  | 1.76    | 0.498      | 1.75           | 0.398      |
|             | 30000. | 9.13      | 0.401  | 1.77    | 0.537      | 1.75           | 0.429      |
|             | 80000. | 12.3      | 0.271  | 1.80    | 0.641      | 1.77           | 0.513      |
| 5S - 6P     | 2500.  | 3.02      | 1.76   |         |            |                |            |
| 12531.0A    | 5000.  | 3.52      | 2.06   |         |            |                |            |
| C= 0.19E+20 | 10000. | 4.20      | 2.12   | 1.24*   | 0.562*     |                |            |
|             | 20000. | 5.14      | 1.74   | 1.29*   | 0.663*     | 1.22*          | 0.522*     |
|             | 30000. | 5.85      | 1.52   | 1.32*   | 0.723*     | 1.24*          | 0.572*     |
|             | 80000. | 7.32      | 1.16   | 1.41    | 0.876      | 1.30*          | 0.699*     |
| 5S - 7P     | 2500.  | 5.02      | 2.87   |         |            |                |            |
| 9951.3A     | 5000.  | 5.88      | 3.40   |         |            |                |            |
| C= 0.62E+19 | 10000. | 6.99      | 3.55   |         |            |                |            |
|             | 20000. | 8.44      | 2.93   |         |            |                |            |
|             | 30000. | 9.46      | 2.43   |         |            |                |            |
|             | 80000. | 11.3      | 1.59   | 2.25*   | 1.47*      |                |            |
| NE= 0.1E+18 |        |           |        |         |            |                |            |
| 4S - 4P     | 2500.  | 0.448     | 0.320  | 0.263*  | 0.745E-01* | 0.246*         | 0.560E-01* |
| 7676.2A     | 5000.  | 0.509     | 0.388  | 0.275   | 0.919E-01  | 0.265*         | 0.711E-01* |
| C= 0.47E+20 | 10000. | 0.624     | 0.447  | 0.282   | 0.109      | 0.274*         | 0.857E-01* |
|             | 20000. | 0.825     | 0.459  | 0.289   | 0.126      | 0.279          | 0.100      |
|             | 30000. | 0.973     | 0.409  | 0.293   | 0.137      | 0.282          | 0.109      |
|             | 80000. | 1.39      | 0.285  | 0.306   | 0.165      | 0.290          | 0.132      |
| 4S - 5P     | 2500.  | 0.960     | 0.519  |         |            |                |            |
| 4045.2A     | 5000.  | 1.10      | 0.661  |         |            |                |            |
| C= 0.44E+19 | 10000. | 1.26      | 0.738  |         |            |                |            |
|             | 20000. | 1.48      | 0.743  | 0.432*  | 0.204*     |                |            |
|             | 30000. | 1.64      | 0.655  | 0.443*  | 0.226*     |                |            |
|             | 80000. | 2.06      | 0.491  | 0.472*  | 0.281*     | 0.437*         | 0.223*     |
| 4S - 6P     | 2500.  | 2.31      | 1.12   |         |            |                |            |
| 3446.7A     | 5000.  | 2.70      | 1.48   |         |            |                |            |
| C= 0.14E+19 | 10000. | 3.15      | 1.64   |         |            |                |            |
|             | 20000. | 3.73      | 1.60   |         |            |                |            |
|             | 30000. | 4.14      | 1.42   |         |            |                |            |
|             | 80000. | 5.04      | 1.06   |         |            |                |            |

| NE= 0.1E+18        |        | ELECTRONS |       | PROTONS |        | IONIZED HELIUM |        |
|--------------------|--------|-----------|-------|---------|--------|----------------|--------|
| TRANSITION         | T(K)   | 2WE(A)    | DE(A) | 2WI(A)  | DI(A)  | 2WI(A)         | DI(A)  |
| 4S - 7P            | 2500.  | 5.09*     | 1.97* |         |        |                |        |
| 3217.3A            | 5000.  | 6.08*     | 2.95* |         |        |                |        |
| $\approx 0.64E+18$ | 10000. | 7.20      | 3.15  |         |        |                |        |
|                    | 20000. | 8.62      | 2.96  |         |        |                |        |
|                    | 30000. | 9.60      | 2.55  |         |        |                |        |
|                    | 80000. | 11.4      | 1.81  |         |        |                |        |
| 4P - 5S            | 2500.  | 5.83      | 3.62  | 1.31*   | 0.627* |                |        |
| 12492.0A           | 5000.  | 6.72      | 4.57  | 1.48*   | 0.918* | 1.23*          | 0.667* |
| $\approx 0.58E+20$ | 10000. | 7.48      | 5.56  | 1.64*   | 1.18*  | 1.37*          | 0.900* |
|                    | 20000. | 8.44      | 5.59  | 1.82*   | 1.43*  | 1.51*          | 1.12*  |
|                    | 30000. | 9.00      | 5.08  | 1.93    | 1.58   | 1.60*          | 1.24*  |
|                    | 80000. | 11.5      | 3.60  | 2.24    | 1.95   | 1.84*          | 1.55*  |
| 4P - 6S            | 2500.  | 6.64      | 3.70  |         |        |                |        |
| 6929.5A            | 5000.  | 7.65      | 4.90  |         |        |                |        |
| $\approx 0.75E+19$ | 10000. | 8.23      | 5.72  |         |        |                |        |
|                    | 20000. | 9.16      | 5.91  |         |        |                |        |
|                    | 30000. | 9.50      | 5.40  |         |        |                |        |
|                    | 80000. | 11.7      | 4.11  | 2.54*   | 2.18*  |                |        |
| 4P - 3D            | 2500.  | 2.53      | 1.22  | 0.814*  | 0.256* | 0.742*         | 0.188* |
| 11745.0A           | 5000.  | 2.71      | 1.38  | 0.867*  | 0.326* | 0.823*         | 0.249* |
| $\approx 0.44E+20$ | 10000. | 3.12      | 1.41  | 0.900   | 0.393  | 0.860*         | 0.307* |
|                    | 20000. | 3.94      | 1.11  | 0.931   | 0.460  | 0.885*         | 0.364* |
|                    | 30000. | 4.64      | 0.940 | 0.950   | 0.501  | 0.899          | 0.397  |
|                    | 80000. | 6.39      | 0.673 | 1.01    | 0.605  | 0.936          | 0.483  |
| 4P - 4D            | 2500.  | 7.63      | 4.25  |         |        |                |        |
| 6955.2A            | 5000.  | 8.38      | 5.10  |         |        |                |        |
| $\approx 0.35E+19$ | 10000. | 9.13      | 5.19  |         |        |                |        |
|                    | 20000. | 10.1      | 4.25  |         |        |                |        |
|                    | 30000. | 10.9      | 3.89  |         |        |                |        |
|                    | 80000. | 12.0      | 2.80  | 3.05*   | 2.40*  |                |        |
| NE= 0.1E+19        |        |           |       |         |        |                |        |
| 4S - 4P            | 2500.  | 4.44      | 2.76  |         |        |                |        |
| 7676.2A            | 5000.  | 5.08      | 3.57  |         |        |                |        |
| $\approx 0.47E+20$ | 10000. | 6.24      | 4.25  | 2.66*   | 0.874* |                |        |
|                    | 20000. | 8.25      | 4.45  | 2.83*   | 1.11*  |                |        |
|                    | 30000. | 9.72      | 4.01  | 2.90*   | 1.25*  |                |        |
|                    | 80000. | 13.9      | 2.84  | 3.06*   | 1.57*  | 2.89*          | 1.24*  |



ШТАРКОВО ШИРЕЊЕ ЛИНИЈА К I

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Претходно саопштење

Користећи семикласичан прилаз, у раду су израчунате ширине и помаци за 51 мултиплет неутралног калијума, проузроковане сударима са електронима,

протонима и јонизованим хелијумом. Резултати су дати у функцији електронске температуре и густине.

## TABLES FOR Na I LINES STARK BROADENING PARAMETERS

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**SUMMARY:** A semiclassical approach has been used to evaluate electron–, proton–, and ionized–helium–impact line widths and shifts for 61 neutral sodium multiplets as a function of electron temperature and electron density.

Reliable Stark broadening parameters for Na I lines are useful for a number of problems in astrophysics (e. g. Caccin, Gomez and Roberti, 1980; Vince, Dimitrijević and Kršljanin, 1985), plasma diagnostics (Griem, 1974), technology of high pressure discharge lamps (Stormberg, 1980; Wharmby, 1980) etc. Using a semi-classical–perturbational approach (Sahal–Bréchet, 1969, a,b) we have calculated recently (Dimitrijević and Sahal–Bréchet, 1989) electron–, proton–, and ionized helium–impact broadening parameters for 46 neutral sodium multiplets with the principal quantum number ( $n$ ) of the upper state between 6 and 10, at perturber density  $N = 10^{13} \text{ cm}^{-3}$  and electron impact broadening parameters at  $N = 10^{16} \text{ cm}^{-3}$ . For higher densities the departure from the linear density law due to Debye screening influences on the accuracy of the method (this is especially serious in the case of the shift) making that extrapolation to higher densities is sometimes difficult and inaccurate.

In order to enable such extrapolation, we calculated Stark broadening data for 61 Na I multiplets for perturber densities  $10^{13} - 10^{19} \text{ cm}^{-3}$ , when validity conditions of the theory are satisfied. Data at  $10^{13}$  and  $10^{16} \text{ cm}^{-3}$  for  $n \geq 6$ , can be found in Dimitrijević and Sahal–Bréchet (1989), where all details of the calculations are given. For the discussion and the comparison with experimental data see also Dimitrijević and Sahal–Bréchet (1985). Energy level data were taken from Bashkin and Stoner (1975).

The calculated values are presented in Table 1. We checked that for each value given in the Table, the collision volume ( $V$ ) multiplied by the perturber density ( $NE$ ) is much less than one. In such a case the impact approximation is valid (Sahal–Bréchet, 1969). The values for which  $NE \cdot V > 0.5$  are not given in the Table, while values where  $0.1 < NE \cdot V \leq 0.5$  are denoted with an asterisk and are given in order to enable interpolation to lower densities. In the case when the impact approximation is not valid, the ion broadening contribution may be estimated by the quasistatic ion–broadening parameter (Griem, 1974).

Table 1. This table lists electron–, proton– and ionized helium–impact broadening parameters for Na I lines for perturber densities from  $10^{13}$  to  $10^{18} \text{ cm}^{-3}$  and temperatures from 2500 to 80,000 K. Transitions and averaged wavelengths for the multiplet (in Å) are also given. Under  $2W$  are given full halfwidths, while  $D$  denotes corresponding shifts. Using  $c$  (see Eq. (4) in the preceding article), we obtain an estimate for maximum perturber density for which the line may be treated as isolated and the tabulated values may be used. Asterisk denotes cases when the collision volume multiplied by the electron density (condition for the validity of the impact approximation) lies between 0.1 and 0.5.

| NE= 0.1E+14 |        |                     |            |                   |            |                          |            |
|-------------|--------|---------------------|------------|-------------------|------------|--------------------------|------------|
| TRANSITION  | T(K)   | ELECTRONS<br>2WE(A) | DE(A)      | PROTONS<br>2WI(A) | DI(A)      | IONIZED HELIUM<br>2WI(A) | DI(A)      |
| 3S - 3P     | 2500.  | 0.191E-04           | 0.132E-04  | 0.126E-04         | 0.372E-05  | 0.125E-04                | 0.301E-05  |
| 5291.8A     | 5000.  | 0.211E-04           | 0.155E-04  | 0.127E-04         | 0.417E-05  | 0.126E-04                | 0.338E-05  |
| c= 0.30E+20 | 10000. | 0.249E-04           | 0.178E-04  | 0.129E-04         | 0.469E-05  | 0.127E-04                | 0.380E-05  |
|             | 20000. | 0.322E-04           | 0.182E-04  | 0.130E-04         | 0.526E-05  | 0.128E-04                | 0.426E-05  |
|             | 30000. | 0.381E-04           | 0.183E-04  | 0.132E-04         | 0.563E-05  | 0.128E-04                | 0.456E-05  |
|             | 80000. | 0.551E-04           | 0.129E-04  | 0.136E-04         | 0.663E-05  | 0.131E-04                | 0.537E-05  |
| 3S - 4P     | 2500.  | 0.649E-04           | -0.241E-04 | 0.224E-04         | -0.797E-05 | 0.220E-04                | -0.645E-05 |
| 3302.6A     | 5000.  | 0.725E-04           | -0.148E-04 | 0.227E-04         | -0.896E-05 | 0.222E-04                | -0.725E-05 |
| c= 0.12E+19 | 10000. | 0.864E-04           | -0.448E-05 | 0.231E-04         | -0.101E-04 | 0.224E-04                | -0.815E-05 |
|             | 20000. | 0.100E-03           | 0.232E-05  | 0.236E-04         | -0.113E-04 | 0.227E-04                | -0.915E-05 |
|             | 30000. | 0.108E-03           | 0.579E-05  | 0.239E-04         | -0.121E-04 | 0.230E-04                | -0.979E-05 |
|             | 80000. | 0.126E-03           | 0.634E-05  | 0.251E-04         | -0.142E-04 | 0.237E-04                | -0.115E-04 |
| 3S - 5P     | 2500.  | 0.202E-03           | -0.114E-03 | 0.599E-04         | -0.341E-04 | 0.565E-04                | -0.276E-04 |
| 2352.8A     | 5000.  | 0.221E-03           | -0.100E-03 | 0.624E-04         | -0.384E-04 | 0.582E-04                | -0.310E-04 |
| c= 0.40E+18 | 10000. | 0.254E-03           | -0.668E-04 | 0.656E-04         | -0.432E-04 | 0.603E-04                | -0.349E-04 |
|             | 20000. | 0.295E-03           | -0.465E-04 | 0.695E-04         | -0.485E-04 | 0.630E-04                | -0.393E-04 |
|             | 30000. | 0.313E-03           | -0.344E-04 | 0.721E-04         | -0.520E-04 | 0.648E-04                | -0.421E-04 |
|             | 80000. | 0.347E-03           | -0.115E-04 | 0.799E-04         | -0.609E-04 | 0.703E-04                | -0.496E-04 |
| 3P - 4S     | 2500.  | 0.367E-03           | 0.262E-03  | 0.857E-04         | 0.708E-04  | 0.737E-04                | 0.573E-04  |
| 11397.0A    | 5000.  | 0.420E-03           | 0.301E-03  | 0.938E-04         | 0.795E-04  | 0.799E-04                | 0.644E-04  |
| c= 0.59E+20 | 10000. | 0.466E-03           | 0.356E-03  | 0.103E-03         | 0.893E-04  | 0.871E-04                | 0.724E-04  |
|             | 20000. | 0.515E-03           | 0.334E-03  | 0.114E-03         | 0.100E-03  | 0.954E-04                | 0.812E-04  |
|             | 30000. | 0.552E-03           | 0.329E-03  | 0.121E-03         | 0.107E-03  | 0.101E-03                | 0.869E-04  |
|             | 80000. | 0.702E-03           | 0.228E-03  | 0.140E-03         | 0.126E-03  | 0.116E-03                | 0.102E-03  |
| 3P - 5S     | 2500.  | 0.405E-03           | 0.294E-03  | 0.867E-04         | 0.807E-04  | 0.706E-04                | 0.653E-04  |
| 6158.6A     | 5000.  | 0.468E-03           | 0.351E-03  | 0.971E-04         | 0.908E-04  | 0.790E-04                | 0.735E-04  |
| c= 0.70E+19 | 10000. | 0.508E-03           | 0.383E-03  | 0.109E-03         | 0.102E-03  | 0.885E-04                | 0.827E-04  |
|             | 20000. | 0.563E-03           | 0.366E-03  | 0.122E-03         | 0.115E-03  | 0.991E-04                | 0.929E-04  |
|             | 30000. | 0.589E-03           | 0.339E-03  | 0.130E-03         | 0.123E-03  | 0.106E-03                | 0.995E-04  |
|             | 80000. | 0.732E-03           | 0.254E-03  | 0.154E-03         | 0.145E-03  | 0.125E-03                | 0.117E-03  |
| 3P - 3D     | 2500.  | 0.312E-03           | 0.228E-03  | 0.814E-04         | 0.617E-04  | 0.721E-04                | 0.500E-04  |
| 8191.1A     | 5000.  | 0.355E-03           | 0.247E-03  | 0.879E-04         | 0.694E-04  | 0.769E-04                | 0.562E-04  |
| c= 0.74E+19 | 10000. | 0.385E-03           | 0.247E-03  | 0.955E-04         | 0.780E-04  | 0.825E-04                | 0.632E-04  |
|             | 20000. | 0.413E-03           | 0.227E-03  | 0.104E-03         | 0.876E-04  | 0.892E-04                | 0.710E-04  |
|             | 30000. | 0.428E-03           | 0.201E-03  | 0.110E-03         | 0.937E-04  | 0.936E-04                | 0.759E-04  |
|             | 80000. | 0.474E-03           | 0.137E-03  | 0.126E-03         | 0.110E-03  | 0.106E-03                | 0.894E-04  |
| 3P - 4D     | 2500.  | 0.255E-02           | 0.126E-02  | 0.699E-03         | 0.638E-03  | 0.563E-03                | 0.514E-03  |
| 5686.4A     | 5000.  | 0.243E-02           | 0.107E-02  | 0.784E-03         | 0.723E-03  | 0.637E-03                | 0.584E-03  |
| c= 0.13E+18 | 10000. | 0.226E-02           | 0.836E-03  | 0.883E-03         | 0.816E-03  | 0.713E-03                | 0.661E-03  |
|             | 20000. | 0.208E-02           | 0.598E-03  | 0.100E-02         | 0.919E-03  | 0.800E-03                | 0.743E-03  |
|             | 30000. | 0.197E-02           | 0.479E-03  | 0.109E-02         | 0.986E-03  | 0.858E-03                | 0.797E-03  |
|             | 80000. | 0.170E-02           | 0.262E-03  | 0.130E-02         | 0.120E-02  | 0.103E-02                | 0.941E-03  |
| 3P - 5D     | 2500.  | 0.672E-02           | 0.321E-02  | 0.189E-02         | 0.170E-02  | 0.154E-02                | 0.136E-02  |
| 4981.4A     | 5000.  | 0.633E-02           | 0.249E-02  | 0.212E-02         | 0.194E-02  | 0.172E-02                | 0.156E-02  |
| c= 0.52E+17 | 10000. | 0.585E-02           | 0.189E-02  | 0.239E-02         | 0.220E-02  | 0.193E-02                | 0.177E-02  |
|             | 20000. | 0.532E-02           | 0.121E-02  | 0.272E-02         | 0.249E-02  | 0.217E-02                | 0.201E-02  |
|             | 30000. | 0.500E-02           | 0.945E-03  | 0.295E-02         | 0.267E-02  | 0.233E-02                | 0.216E-02  |
|             | 80000. | 0.419E-02           | 0.426E-03  | 0.354E-02         | 0.325E-02  | 0.279E-02                | 0.255E-02  |

# TABLES FOR NA I LINES STARK BROADENING PARAMETERS

NE= 0.1E+14

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS   |            | IONIZED HELIUM |            |
|-------------|--------|-----------|------------|-----------|------------|----------------|------------|
|             |        | 2WE(A)    | DE(A)      | 2WI(A)    | DI(A)      | 2WI(A)         | DI(A)      |
| 3D - 4P     | 2500.  | 0.734E-01 | -0.424E-01 | 0.169E-01 | -0.110E-01 | 0.156E-01      | -0.892E-02 |
| 91050.0A    | 5000.  | 0.814E-01 | -0.428E-01 | 0.179E-01 | -0.124E-01 | 0.162E-01      | -0.100E-01 |
| c= 0.91E+21 | 10000. | 0.901E-01 | -0.336E-01 | 0.191E-01 | -0.139E-01 | 0.171E-01      | -0.113E-01 |
|             | 20000. | 0.105     | -0.252E-01 | 0.205E-01 | -0.156E-01 | 0.181E-01      | -0.127E-01 |
|             | 30000. | 0.114     | -0.221E-01 | 0.214E-01 | -0.167E-01 | 0.188E-01      | -0.136E-01 |
|             | 80000. | 0.131     | -0.129E-01 | 0.241E-01 | -0.197E-01 | 0.207E-01      | -0.160E-01 |

|             |        |           |            |           |            |           |            |
|-------------|--------|-----------|------------|-----------|------------|-----------|------------|
| 3D - 5P     | 2500.  | 0.785E-02 | -0.463E-02 | 0.208E-02 | -0.130E-02 | 0.193E-02 | -0.105E-02 |
| 17038.7A    | 5000.  | 0.874E-02 | -0.441E-02 | 0.219E-02 | -0.146E-02 | 0.200E-02 | -0.118E-02 |
| c= 0.14E+20 | 10000. | 0.986E-02 | -0.328E-02 | 0.232E-02 | -0.165E-02 | 0.209E-02 | -0.133E-02 |
|             | 20000. | 0.115E-01 | -0.260E-02 | 0.248E-02 | -0.185E-02 | 0.221E-02 | -0.150E-02 |
|             | 30000. | 0.123E-01 | -0.226E-02 | 0.259E-02 | -0.198E-02 | 0.229E-02 | -0.160E-02 |
|             | 80000. | 0.136E-01 | -0.104E-02 | 0.290E-02 | -0.233E-02 | 0.251E-02 | -0.189E-02 |

|             |        |           |            |           |            |           |            |
|-------------|--------|-----------|------------|-----------|------------|-----------|------------|
| 3D - 4F     | 2500.  | 0.188E-01 | -0.586E-02 | 0.552E-02 | -0.508E-02 | 0.448E-02 | -0.410E-02 |
| 18465.3A    | 5000.  | 0.177E-01 | -0.359E-02 | 0.621E-02 | -0.576E-02 | 0.502E-02 | -0.465E-02 |
| c= 0.14E+19 | 10000. | 0.164E-01 | -0.180E-02 | 0.701E-02 | -0.648E-02 | 0.564E-02 | -0.525E-02 |
|             | 20000. | 0.149E-01 | -0.785E-03 | 0.801E-02 | -0.730E-02 | 0.634E-02 | -0.591E-02 |
|             | 30000. | 0.142E-01 | -0.445E-03 | 0.870E-02 | -0.787E-02 | 0.681E-02 | -0.633E-02 |
|             | 80000. | 0.126E-01 | 0.221E-03  | 0.103E-01 | -0.974E-02 | 0.821E-02 | -0.748E-02 |

|             |        |           |            |           |            |           |            |
|-------------|--------|-----------|------------|-----------|------------|-----------|------------|
| 4S - 4P     | 2500.  | 0.356E-02 | -0.189E-02 | 0.105E-02 | -0.504E-03 | 0.102E-02 | -0.408E-03 |
| 22070.0A    | 5000.  | 0.385E-02 | -0.189E-02 | 0.108E-02 | -0.567E-03 | 0.103E-02 | -0.459E-03 |
| c= 0.53E+20 | 10000. | 0.440E-02 | -0.165E-02 | 0.112E-02 | -0.637E-03 | 0.106E-02 | -0.516E-03 |
|             | 20000. | 0.529E-02 | -0.124E-02 | 0.117E-02 | -0.715E-03 | 0.109E-02 | -0.579E-03 |
|             | 30000. | 0.589E-02 | -0.105E-02 | 0.120E-02 | -0.765E-03 | 0.111E-02 | -0.620E-03 |
|             | 80000. | 0.723E-02 | -0.658E-03 | 0.130E-02 | -0.901E-03 | 0.118E-02 | -0.730E-03 |

|             |        |           |            |           |            |           |            |
|-------------|--------|-----------|------------|-----------|------------|-----------|------------|
| 4S - 5P     | 2500.  | 0.298E-02 | -0.171E-02 | 0.859E-03 | -0.499E-03 | 0.808E-03 | -0.404E-03 |
| 10747.0A    | 5000.  | 0.325E-02 | -0.162E-02 | 0.898E-03 | -0.562E-03 | 0.833E-03 | -0.455E-03 |
| c= 0.57E+19 | 10000. | 0.372E-02 | -0.124E-02 | 0.945E-03 | -0.633E-03 | 0.866E-03 | -0.512E-03 |
|             | 20000. | 0.438E-02 | -0.103E-02 | 0.100E-02 | -0.711E-03 | 0.906E-03 | -0.576E-03 |
|             | 30000. | 0.470E-02 | -0.800E-03 | 0.104E-02 | -0.762E-03 | 0.933E-03 | -0.617E-03 |
|             | 80000. | 0.531E-02 | -0.387E-03 | 0.116E-02 | -0.897E-03 | 0.101E-02 | -0.727E-03 |

|             |        |           |           |           |           |           |           |
|-------------|--------|-----------|-----------|-----------|-----------|-----------|-----------|
| 4P - 4D     | 2500.  | 0.451E-01 | 0.216E-01 | 0.118E-01 | 0.108E-01 | 0.961E-02 | 0.872E-02 |
| 23370.0A    | 5000.  | 0.433E-01 | 0.187E-01 | 0.133E-01 | 0.123E-01 | 0.108E-01 | 0.991E-02 |
| c= 0.22E+19 | 10000. | 0.408E-01 | 0.148E-01 | 0.149E-01 | 0.138E-01 | 0.121E-01 | 0.112E-01 |
|             | 20000. | 0.381E-01 | 0.105E-01 | 0.170E-01 | 0.156E-01 | 0.136E-01 | 0.126E-01 |
|             | 30000. | 0.367E-01 | 0.824E-02 | 0.184E-01 | 0.167E-01 | 0.145E-01 | 0.135E-01 |
|             | 80000. | 0.329E-01 | 0.432E-02 | 0.221E-01 | 0.203E-01 | 0.174E-01 | 0.160E-01 |

|             |        |           |           |           |           |           |           |
|-------------|--------|-----------|-----------|-----------|-----------|-----------|-----------|
| 4P - 5D     | 2500.  | 0.599E-01 | 0.282E-01 | 0.166E-01 | 0.149E-01 | 0.135E-01 | 0.120E-01 |
| 14776.0A    | 5000.  | 0.566E-01 | 0.229E-01 | 0.187E-01 | 0.171E-01 | 0.151E-01 | 0.137E-01 |
| c= 0.45E+18 | 10000. | 0.525E-01 | 0.174E-01 | 0.211E-01 | 0.194E-01 | 0.170E-01 | 0.156E-01 |
|             | 20000. | 0.481E-01 | 0.116E-01 | 0.239E-01 | 0.219E-01 | 0.191E-01 | 0.177E-01 |
|             | 30000. | 0.453E-01 | 0.893E-02 | 0.259E-01 | 0.235E-01 | 0.205E-01 | 0.190E-01 |
|             | 80000. | 0.385E-01 | 0.408E-02 | 0.311E-01 | 0.286E-01 | 0.245E-01 | 0.225E-01 |

|             |        |           |            |           |            |           |            |
|-------------|--------|-----------|------------|-----------|------------|-----------|------------|
| 5S - 5P     | 2500.  | 0.948E-01 | -0.576E-01 | 0.235E-01 | -0.152E-01 | 0.217E-01 | -0.123E-01 |
| 54318.3A    | 5000.  | 0.106     | -0.610E-01 | 0.249E-01 | -0.171E-01 | 0.226E-01 | -0.138E-01 |
| c= 0.15E+21 | 10000. | 0.120     | -0.572E-01 | 0.265E-01 | -0.192E-01 | 0.237E-01 | -0.156E-01 |
|             | 20000. | 0.139     | -0.463E-01 | 0.284E-01 | -0.216E-01 | 0.251E-01 | -0.175E-01 |
|             | 30000. | 0.152     | -0.389E-01 | 0.297E-01 | -0.232E-01 | 0.261E-01 | -0.188E-01 |
|             | 80000. | 0.176     | -0.255E-01 | 0.334E-01 | -0.273E-01 | 0.288E-01 | -0.221E-01 |

NE= 0.1E+15

|             |        |           |           |           |           |           |           |
|-------------|--------|-----------|-----------|-----------|-----------|-----------|-----------|
| 3S - 3P     | 2500.  | 0.191E-03 | 0.132E-03 | 0.126E-03 | 0.371E-04 | 0.125E-03 | 0.300E-04 |
| 5891.8A     | 5000.  | 0.211E-03 | 0.155E-03 | 0.127E-03 | 0.417E-04 | 0.126E-03 | 0.338E-04 |
| c= 0.30E+20 | 10000. | 0.249E-03 | 0.178E-03 | 0.129E-03 | 0.468E-04 | 0.127E-03 | 0.379E-04 |
|             | 20000. | 0.322E-03 | 0.182E-03 | 0.130E-03 | 0.526E-04 | 0.128E-03 | 0.426E-04 |
|             | 30000. | 0.381E-03 | 0.183E-03 | 0.132E-03 | 0.563E-04 | 0.128E-03 | 0.456E-04 |
|             | 80000. | 0.551E-03 | 0.129E-03 | 0.136E-03 | 0.663E-04 | 0.131E-03 | 0.537E-04 |

| NE= 0.1E+15 |        |           |            |            |             |                |             |
|-------------|--------|-----------|------------|------------|-------------|----------------|-------------|
| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS    |             | IONIZED HELIUM |             |
|             |        | 2WE(A)    | FJ(A)      | 2WI(A)     | DI(A)       | 2WI(A)         | DI(A)       |
| 3S - 4P     | 2500.  | 0.649E-03 | -0.241E-03 | 0.224E-03  | -0.790E-04  | 0.220E-03      | -0.637E-04  |
| 3302.6A     | 5000.  | 0.725E-03 | -0.148E-03 | 0.227E-03  | -0.890E-04  | 0.222E-03      | -0.721E-04  |
| c= 0.12E+19 | 10000. | 0.864E-03 | -0.448E-04 | 0.231E-03  | -0.100E-03  | 0.224E-03      | -0.811E-04  |
|             | 20000. | 0.100E-02 | 0.232E-04  | 0.236E-03  | -0.113E-03  | 0.227E-03      | -0.913E-04  |
|             | 30000. | 0.108E-02 | 0.579E-04  | 0.239E-03  | -0.121E-03  | 0.230E-03      | -0.978E-04  |
|             | 80000. | 0.126E-02 | 0.634E-04  | 0.251E-03  | -0.142E-03  | 0.237E-03      | -0.115E-03  |
| 3S - 5P     | 2500.  | 0.202E-02 | -0.113E-02 | 0.598E-03  | -0.332E-03  | 0.564E-03      | -0.267E-03  |
| 2852.8A     | 5000.  | 0.221E-02 | -0.998E-03 | 0.624E-03  | -0.378E-03  | 0.581E-03      | -0.305E-03  |
| c= 0.40E+18 | 10000. | 0.254E-02 | -0.668E-03 | 0.656E-03  | -0.428E-03  | 0.603E-03      | -0.346E-03  |
|             | 20000. | 0.295E-02 | -0.465E-03 | 0.695E-03  | -0.483E-03  | 0.630E-03      | -0.391E-03  |
|             | 30000. | 0.313E-02 | -0.344E-03 | 0.721E-03  | -0.517E-03  | 0.648E-03      | -0.419E-03  |
|             | 80000. | 0.347E-02 | -0.115E-03 | 0.799E-03  | -0.608E-03  | 0.703E-03      | -0.495E-03  |
| 3S - 6P     | 2500.  | 0.528E-02 | -0.337E-02 | 0.143E-02  | -0.909E-03  | 0.131E-02      | -0.726E-03  |
| 2680.4A     | 5000.  | 0.573E-02 | -0.286E-02 | 0.152E-02  | -0.105E-02  | 0.137E-02      | -0.839E-03  |
| c= 0.19E+18 | 10000. | 0.653E-02 | -0.206E-02 | 0.163E-02  | -0.119E-02  | 0.145E-02      | -0.959E-03  |
|             | 20000. | 0.749E-02 | -0.145E-02 | 0.176E-02  | -0.135E-02  | 0.154E-02      | -0.109E-02  |
|             | 30000. | 0.785E-02 | -0.110E-02 | 0.184E-02  | -0.145E-02  | 0.160E-02      | -0.117E-02  |
|             | 80000. | 0.843E-02 | -0.366E-03 | 0.208E-02  | -0.172E-02  | 0.178E-02      | -0.139E-02  |
| 3S - 7P     | 2500.  | 0.118E-01 | -0.732E-02 | 0.304E-02* | -0.202E-02* | 0.272E-02*     | -0.160E-02* |
| 2593.9A     | 5000.  | 0.127E-01 | -0.662E-02 | 0.327E-02  | -0.236E-02  | 0.289E-02*     | -0.188E-02* |
| c= 0.10E+18 | 10000. | 0.145E-01 | -0.470E-02 | 0.354E-02  | -0.271E-02  | 0.308E-02*     | -0.218E-02* |
|             | 20000. | 0.164E-01 | -0.334E-02 | 0.385E-02  | -0.309E-02  | 0.332E-02      | -0.249E-02  |
|             | 30000. | 0.170E-01 | -0.247E-02 | 0.406E-02  | -0.332E-02  | 0.347E-02      | -0.268E-02  |
|             | 80000. | 0.178E-01 | -0.749E-03 | 0.464E-02  | -0.395E-02  | 0.391E-02      | -0.320E-02  |
| 3S - 8P     | 2500.  | 0.235E-01 | -0.153E-01 | 0.588E-02* | -0.393E-02* |                |             |
| 2542.8A     | 5000.  | 0.252E-01 | -0.125E-01 | 0.638E-02* | -0.468E-02* | 0.554E-02*     | -0.371E-02* |
| c= 0.63E+17 | 10000. | 0.288E-01 | -0.913E-02 | 0.695E-02* | -0.544E-02* | 0.598E-02*     | -0.435E-02* |
|             | 20000. | 0.321E-01 | -0.675E-02 | 0.761E-02* | -0.624E-02* | 0.648E-02*     | -0.501E-02* |
|             | 30000. | 0.331E-01 | -0.455E-02 | 0.805E-02  | -0.673E-02  | 0.681E-02*     | -0.542E-02* |
|             | 80000. | 0.340E-01 | -0.126E-02 | 0.929E-02  | -0.804E-02  | 0.775E-02*     | -0.649E-02* |
| 3S - 9P     | 2500.  | 0.431E-01 | -0.262E-01 |            |             |                |             |
| 2512.1A     | 5000.  | 0.461E-01 | -0.227E-01 |            |             |                |             |
| c= 0.42E+17 | 10000. | 0.526E-01 | -0.144E-01 | 0.126E-01* | -0.991E-02* |                |             |
|             | 20000. | 0.578E-01 | -0.104E-01 | 0.139E-01* | -0.115E-01* |                |             |
|             | 30000. | 0.593E-01 | -0.743E-02 | 0.147E-01* | -0.124E-01* | 0.124E-01*     | -0.997E-02* |
|             | 80000. | 0.600E-01 | -0.234E-02 | 0.171E-01* | -0.149E-01* | 0.141E-01*     | -0.120E-01* |
| 3S - 10P    | 2500.  | 0.739E-01 | -0.445E-01 |            |             |                |             |
| 2490.7A     | 5000.  | 0.789E-01 | -0.372E-01 |            |             |                |             |
| c= 0.29E+17 | 10000. | 0.898E-01 | -0.257E-01 |            |             |                |             |
|             | 20000. | 0.974E-01 | -0.161E-01 |            |             |                |             |
|             | 30000. | 0.994E-01 | -0.113E-01 |            |             |                |             |
|             | 80000. | 0.990E-01 | -0.270E-02 | 0.294E-01* | -0.257E-01* |                |             |
| 3P - 4S     | 2500.  | 0.367E-02 | 0.262E-02  | 0.857E-03  | 0.703E-03   | 0.737E-03      | 0.567E-03   |
| 11397.0A    | 5000.  | 0.420E-02 | 0.301E-02  | 0.938E-03  | 0.791E-03   | 0.799E-03      | 0.640E-03   |
| c= 0.59E+20 | 10000. | 0.466E-02 | 0.356E-02  | 0.103E-02  | 0.891E-03   | 0.871E-03      | 0.721E-03   |
|             | 20000. | 0.515E-02 | 0.334E-02  | 0.114E-02  | 0.100E-02   | 0.954E-03      | 0.811E-03   |
|             | 30000. | 0.552E-02 | 0.329E-02  | 0.121E-02  | 0.107E-02   | 0.101E-02      | 0.868E-03   |
|             | 80000. | 0.702E-02 | 0.228E-02  | 0.140E-02  | 0.126E-02   | 0.116E-02      | 0.102E-02   |
| 3P - 5S     | 2500.  | 0.405E-02 | 0.293E-02  | 0.867E-03  | 0.793E-03   | 0.706E-03      | 0.639E-03   |
| 6158.6A     | 5000.  | 0.468E-02 | 0.350E-02  | 0.971E-03  | 0.899E-03   | 0.790E-03      | 0.726E-03   |
| c= 0.70E+19 | 10000. | 0.508E-02 | 0.383E-02  | 0.109E-02  | 0.101E-02   | 0.885E-03      | 0.822E-03   |
|             | 20000. | 0.563E-02 | 0.366E-02  | 0.122E-02  | 0.114E-02   | 0.991E-03      | 0.925E-03   |
|             | 30000. | 0.589E-02 | 0.339E-02  | 0.130E-02  | 0.122E-02   | 0.106E-02      | 0.991E-03   |
|             | 80000. | 0.732E-02 | 0.254E-02  | 0.154E-02  | 0.145E-02   | 0.125E-02      | 0.117E-02   |



## TABLES FOR Na I LINES STARK BROADENING PARAMETERS

NE= 0.1E+15

| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS    |            | IONIZED HELIUM |            |
|-------------|--------|-----------|-----------|------------|------------|----------------|------------|
|             |        | 2WE(A)    | DE(A)     | 2WI(A)     | DI(A)      | 2WI(A)         | DI(A)      |
| 3P - 6S     | 2500.  | 0.780E-02 | 0.571E-02 | 0.162E-02  | 0.147E-02  | 0.131E-02      | 0.118E-02  |
| 5151.9A     | 5000.  | 0.892E-02 | 0.648E-02 | 0.182E-02  | 0.168E-02  | 0.147E-02      | 0.135E-02  |
| c= 0.25E+19 | 10000. | 0.974E-02 | 0.676E-02 | 0.204E-02  | 0.190E-02  | 0.165E-02      | 0.153E-02  |
|             | 20000. | 0.110E-01 | 0.640E-02 | 0.229E-02  | 0.215E-02  | 0.186E-02      | 0.174E-02  |
|             | 30000. | 0.119E-01 | 0.546E-02 | 0.245E-02  | 0.230E-02  | 0.199E-02      | 0.186E-02  |
|             | 80000. | 0.146E-01 | 0.375E-02 | 0.289E-02  | 0.272E-02  | 0.234E-02      | 0.220E-02  |
| 3P - 7S     | 2500.  | 0.152E-01 | 0.107E-01 | 0.302E-02  | 0.269E-02  | 0.245E-02      | 0.215E-02  |
| 4750.6A     | 5000.  | 0.173E-01 | 0.122E-01 | 0.339E-02  | 0.309E-02  | 0.275E-02      | 0.248E-02  |
| c= 0.12E+19 | 10000. | 0.190E-01 | 0.118E-01 | 0.381E-02  | 0.352E-02  | 0.309E-02      | 0.284E-02  |
|             | 20000. | 0.219E-01 | 0.101E-01 | 0.428E-02  | 0.399E-02  | 0.347E-02      | 0.322E-02  |
|             | 30000. | 0.245E-01 | 0.844E-02 | 0.458E-02  | 0.429E-02  | 0.371E-02      | 0.347E-02  |
|             | 80000. | 0.293E-01 | 0.528E-02 | 0.540E-02  | 0.507E-02  | 0.437E-02      | 0.410E-02  |
| 3P - 8S     | 2500.  | 0.271E-01 | 0.189E-01 | 0.533E-02  | 0.464E-02  | 0.432E-02      | 0.368E-02  |
| 4544.2A     | 5000.  | 0.307E-01 | 0.206E-01 | 0.599E-02  | 0.538E-02  | 0.485E-02      | 0.430E-02  |
| c= 0.68E+18 | 10000. | 0.361E-01 | 0.198E-01 | 0.672E-02  | 0.616E-02  | 0.544E-02      | 0.495E-02  |
|             | 20000. | 0.423E-01 | 0.151E-01 | 0.755E-02  | 0.700E-02  | 0.611E-02      | 0.564E-02  |
|             | 30000. | 0.475E-01 | 0.126E-01 | 0.808E-02  | 0.753E-02  | 0.654E-02      | 0.608E-02  |
|             | 80000. | 0.555E-01 | 0.692E-02 | 0.952E-02  | 0.893E-02  | 0.771E-02      | 0.723E-02  |
| 3P - 9S     | 2500.  | 0.460E-01 | 0.310E-01 | 0.886E-02* | 0.748E-02* | 0.718E-02*     | 0.589E-02* |
| 4423.5A     | 5000.  | 0.526E-01 | 0.325E-01 | 0.995E-02  | 0.878E-02  | 0.806E-02*     | 0.699E-02* |
| c= 0.43E+18 | 10000. | 0.627E-01 | 0.299E-01 | 0.112E-01  | 0.101E-01  | 0.905E-02*     | 0.811E-02* |
|             | 20000. | 0.770E-01 | 0.218E-01 | 0.125E-01  | 0.115E-01  | 0.102E-01      | 0.930E-02  |
|             | 30000. | 0.861E-01 | 0.178E-01 | 0.134E-01  | 0.124E-01  | 0.109E-01      | 0.100E-01  |
|             | 80000. | 0.986E-01 | 0.694E-02 | 0.158E-01  | 0.148E-01  | 0.128E-01      | 0.120E-01  |
| 3P - 3D     | 2500.  | 0.312E-02 | 0.228E-02 | 0.814E-03  | 0.611E-03  | 0.721E-03      | 0.493E-03  |
| 8191.1A     | 5000.  | 0.355E-02 | 0.247E-02 | 0.879E-03  | 0.691E-03  | 0.768E-03      | 0.558E-03  |
| c= 0.74E+19 | 10000. | 0.385E-02 | 0.247E-02 | 0.955E-03  | 0.777E-03  | 0.825E-03      | 0.629E-03  |
|             | 20000. | 0.413E-02 | 0.227E-02 | 0.104E-02  | 0.874E-03  | 0.892E-03      | 0.708E-03  |
|             | 30000. | 0.428E-02 | 0.201E-02 | 0.110E-02  | 0.936E-03  | 0.936E-03      | 0.758E-03  |
|             | 80000. | 0.474E-02 | 0.137E-02 | 0.126E-02  | 0.110E-02  | 0.106E-02      | 0.894E-03  |
| 3P - 4D     | 2500.  | 0.255E-01 | 0.123E-01 | 0.698E-02  | 0.605E-02  | 0.569E-02      | 0.481E-02  |
| 5686.4A     | 5000.  | 0.243E-01 | 0.106E-01 | 0.784E-02  | 0.699E-02  | 0.636E-02      | 0.560E-02  |
| c= 0.13E+18 | 10000. | 0.226E-01 | 0.833E-02 | 0.882E-02  | 0.799E-02  | 0.713E-02      | 0.643E-02  |
|             | 20000. | 0.208E-01 | 0.597E-02 | 0.100E-01  | 0.907E-02  | 0.800E-02      | 0.732E-02  |
|             | 30000. | 0.197E-01 | 0.479E-02 | 0.109E-01  | 0.978E-02  | 0.858E-02      | 0.788E-02  |
|             | 80000. | 0.170E-01 | 0.262E-02 | 0.130E-01  | 0.119E-01  | 0.103E-01      | 0.936E-02  |
| 3P - 5D     | 2500.  | 0.672E-01 | 0.304E-01 | 0.189E-01* | 0.153E-01* |                |            |
| 4981.4A     | 5000.  | 0.633E-01 | 0.243E-01 | 0.212E-01* | 0.182E-01* | 0.172E-01*     | 0.144E-01* |
| c= 0.52E+17 | 10000. | 0.585E-01 | 0.187E-01 | 0.239E-01* | 0.211E-01* | 0.193E-01*     | 0.169E-01* |
|             | 20000. | 0.532E-01 | 0.120E-01 | 0.272E-01  | 0.242E-01  | 0.217E-01*     | 0.195E-01* |
|             | 30000. | 0.500E-01 | 0.942E-02 | 0.295E-01  | 0.262E-01  | 0.232E-01*     | 0.210E-01* |
|             | 80000. | 0.419E-01 | 0.426E-02 | 0.354E-01  | 0.322E-01  | 0.279E-01      | 0.252E-01  |
| 3P - 6D     | 2500.  | 0.144     | 0.601E-01 |            |            |                |            |
| 4667.5A     | 5000.  | 0.135     | 0.472E-01 |            |            |                |            |
| c= 0.28E+17 | 10000. | 0.124     | 0.316E-01 |            |            |                |            |
|             | 20000. | 0.113     | 0.213E-01 | 0.598E-01* | 0.521E-01* |                |            |
|             | 30000. | 0.106     | 0.166E-01 | 0.648E-01* | 0.566E-01* |                |            |
|             | 80000. | 0.875E-01 | 0.630E-02 | 0.776E-01* | 0.703E-01* | 0.612E-01*     | 0.547E-01* |
| 3P - 7D     | 2500.  | 0.272     | 0.999E-01 |            |            |                |            |
| 4496.6A     | 5000.  | 0.255     | 0.812E-01 |            |            |                |            |
| c= 0.17E+17 | 10000. | 0.236     | 0.455E-01 |            |            |                |            |
|             | 20000. | 0.213     | 0.347E-01 |            |            |                |            |
|             | 30000. | 0.199     | 0.265E-01 |            |            |                |            |
|             | 80000. | 0.164     | 0.851E-02 |            |            |                |            |



| NE= 0.1E+15 |        |                     |            |                   |             |                          |             |
|-------------|--------|---------------------|------------|-------------------|-------------|--------------------------|-------------|
| TRANSITION  | T(K)   | ELECTRONS<br>2WE(A) | DE(A)      | PROTONS<br>2WI(A) | DI(A)       | IONIZED HELIUM<br>2WI(A) | DI(A)       |
| 3P - 8D     | 2500.  | 0.477               | 0.160      |                   |             |                          |             |
| 4392.3A     | 5000.  | 0.448               | 0.125      |                   |             |                          |             |
| c= 0.96E+16 | 10000. | 0.414               | 0.789E-01  |                   |             |                          |             |
|             | 20000. | 0.374               | 0.428E-01  |                   |             |                          |             |
|             | 30000. | 0.348               | 0.395E-01  |                   |             |                          |             |
|             | 80000. | 0.284               | 0.108E-01  |                   |             |                          |             |
| 3P - 9D     | 2500.  | 0.739               | 0.230      |                   |             |                          |             |
| 4323.5A     | 5000.  | 0.705               | 0.176      |                   |             |                          |             |
| c= 0.67E+16 | 10000. | 0.658               | 0.116      |                   |             |                          |             |
|             | 20000. | 0.596               | 0.651E-01  |                   |             |                          |             |
|             | 30000. | 0.555               | 0.454E-01  |                   |             |                          |             |
|             | 80000. | 0.454               | 0.138E-01  |                   |             |                          |             |
| 3D - 4P     | 2500.  | 0.734               | -0.423     | 0.169             | -0.109      | 0.156                    | -0.877E-01  |
| 91050.0A    | 5000.  | 0.814               | -0.428     | 0.179             | -0.123      | 0.162                    | -0.994E-01  |
| c= 0.91E+21 | 10000. | 0.901               | -0.336     | 0.191             | -0.139      | 0.171                    | -0.112      |
|             | 20000. | 1.05                | -0.252     | 0.205             | -0.156      | 0.181                    | -0.126      |
|             | 30000. | 1.14                | -0.221     | 0.214             | -0.167      | 0.188                    | -0.135      |
|             | 80000. | 1.31                | -0.129     | 0.241             | -0.197      | 0.207                    | -0.160      |
| 3D - 5P     | 2500.  | 0.785E-01           | -0.462E-01 | 0.207E-01         | -0.127E-01  | 0.192E-01                | -0.102E-01  |
| 17038.7A    | 5000.  | 0.874E-01           | -0.441E-01 | 0.219E-01         | -0.144E-01  | 0.200E-01                | -0.116E-01  |
| c= 0.14E+20 | 10000. | 0.986E-01           | -0.328E-01 | 0.232E-01         | -0.163E-01  | 0.209E-01                | -0.132E-01  |
|             | 20000. | 0.115               | -0.260E-01 | 0.248E-01         | -0.184E-01  | 0.221E-01                | -0.149E-01  |
|             | 30000. | 0.123               | -0.226E-01 | 0.259E-01         | -0.197E-01  | 0.229E-01                | -0.160E-01  |
|             | 80000. | 0.136               | -0.104E-01 | 0.290E-01         | -0.233E-01  | 0.251E-01                | -0.189E-01  |
| 3D - 6P     | 2500.  | 0.114               | -0.696E-01 | 0.299E-01         | -0.194E-01  | 0.271E-01                | -0.155E-01  |
| 12309.2A    | 5000.  | 0.125               | -0.638E-01 | 0.318E-01         | -0.223E-01  | 0.285E-01                | -0.179E-01  |
| c= 0.39E+19 | 10000. | 0.142               | -0.447E-01 | 0.341E-01         | -0.254E-01  | 0.302E-01                | -0.205E-01  |
|             | 20000. | 0.163               | -0.309E-01 | 0.369E-01         | -0.288E-01  | 0.322E-01                | -0.233E-01  |
|             | 30000. | 0.171               | -0.229E-01 | 0.387E-01         | -0.310E-01  | 0.336E-01                | -0.250E-01  |
|             | 80000. | 0.184               | -0.564E-02 | 0.439E-01         | -0.366E-01  | 0.374E-01                | -0.296E-01  |
| 3D - 7P     | 2500.  | 0.201               | -0.125     | 0.512E-01*        | -0.344E-01* | 0.456E-01*               | -0.271E-01* |
| 10674.6A    | 5000.  | 0.218               | -0.112     | 0.552E-01         | -0.401E-01  | 0.486E-01*               | -0.320E-01* |
| c= 0.18E+19 | 10000. | 0.248               | -0.752E-01 | 0.597E-01         | -0.461E-01  | 0.520E-01*               | -0.370E-01* |
|             | 20000. | 0.281               | -0.471E-01 | 0.650E-01         | -0.525E-01  | 0.560E-01                | -0.423E-01  |
|             | 30000. | 0.292               | -0.359E-01 | 0.686E-01         | -0.565E-01  | 0.586E-01                | -0.455E-01  |
|             | 80000. | 0.307               | -0.537E-02 | 0.786E-01         | -0.669E-01  | 0.661E-01                | -0.543E-01  |
| 3D - 8P     | 2500.  | 0.356               | -0.232     | 0.883E-01*        | -0.593E-01* |                          |             |
| 9875.6A     | 5000.  | 0.382               | -0.193     | 0.959E-01*        | -0.706E-01* | 0.833E-01*               | -0.559E-01* |
| c= 0.96E+18 | 10000. | 0.436               | -0.127     | 0.105*            | -0.820E-01* | 0.899E-01*               | -0.656E-01* |
|             | 20000. | 0.487               | -0.762E-01 | 0.115*            | -0.941E-01* | 0.975E-01*               | -0.756E-01* |
|             | 30000. | 0.503               | -0.592E-01 | 0.121             | -0.102      | 0.103*                   | -0.817E-01* |
|             | 80000. | 0.517               | -0.881E-02 | 0.140             | -0.121      | 0.117*                   | -0.979E-01* |
| 3D - 9P     | 2500.  | 0.607               | -0.363     |                   |             |                          |             |
| 9414.4A     | 5000.  | 0.649               | -0.322     |                   |             |                          |             |
| c= 0.58E+18 | 10000. | 0.741               | -0.218     | 0.177*            | -0.139*     |                          |             |
|             | 20000. | 0.815               | -0.125     | 0.195*            | -0.161*     |                          |             |
|             | 30000. | 0.836               | -0.975E-01 | 0.207*            | -0.174*     | 0.173*                   | -0.140*     |
|             | 80000. | 0.846               | -0.175E-01 | 0.240*            | -0.209*     | 0.198*                   | -0.169*     |
| 3D -10P     | 2500.  | 0.992               | -0.627     |                   |             |                          |             |
| 9120.8A     | 5000.  | 1.06                | -0.480     |                   |             |                          |             |
| c= 0.39E+18 | 10000. | 1.21                | -0.355     |                   |             |                          |             |
|             | 20000. | 1.31                | -0.200     |                   |             |                          |             |
|             | 30000. | 1.34                | -0.155     |                   |             |                          |             |
|             | 80000. | 1.33                | -0.332E-01 | 0.394*            | -0.344*     |                          |             |

# TABLES FOR NA I LINES STARK BROADENING PARAMETERS

NE= 0.1E+15

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS    |             | IONIZED HELIUM |             |
|-------------|--------|-----------|------------|------------|-------------|----------------|-------------|
|             |        | 2WE(A)    | DE(A)      | 2WI(A)     | DI(A)       | 2WI(A)         | DI(A)       |
| 3D - 4F     | 2500.  | 0.188     | -0.571E-01 | 0.552E-01  | -0.485E-01  | 0.448E-01      | -0.387E-01  |
| 18465.3A    | 5000.  | 0.177     | -0.355E-01 | 0.620E-01  | -0.558E-01  | 0.502E-01      | -0.448E-01  |
| c= 0.14E+19 | 10000. | 0.164     | -0.180E-01 | 0.701E-01  | -0.636E-01  | 0.563E-01      | -0.513E-01  |
|             | 20000. | 0.149     | -0.785E-02 | 0.801E-01  | -0.723E-01  | 0.634E-01      | -0.583E-01  |
|             | 30000. | 0.142     | -0.445E-02 | 0.870E-01  | -0.783E-01  | 0.681E-01      | -0.627E-01  |
|             | 80000. | 0.126     | 0.221E-02  | 0.103      | -0.971E-01  | 0.821E-01      | -0.744E-01  |
| 4S - 4P     | 2500.  | 0.356E-01 | -0.188E-01 | 0.105E-01  | -0.498E-02  | 0.101E-01      | -0.402E-02  |
| 22070.0A    | 5000.  | 0.385E-01 | -0.189E-01 | 0.108E-01  | -0.563E-02  | 0.103E-01      | -0.455E-02  |
| c= 0.53E+20 | 10000. | 0.440E-01 | -0.165E-01 | 0.112E-01  | -0.634E-02  | 0.106E-01      | -0.513E-02  |
|             | 20000. | 0.529E-01 | -0.124E-01 | 0.117E-01  | -0.713E-02  | 0.109E-01      | -0.577E-02  |
|             | 30000. | 0.589E-01 | -0.105E-01 | 0.120E-01  | -0.764E-02  | 0.111E-01      | -0.619E-02  |
|             | 80000. | 0.723E-01 | -0.658E-02 | 0.130E-01  | -0.901E-02  | 0.118E-01      | -0.730E-02  |
| 4S - 5P     | 2500.  | 0.298E-01 | -0.170E-01 | 0.859E-02  | -0.487E-02  | 0.807E-02      | -0.391E-02  |
| 10747.0A    | 5000.  | 0.325E-01 | -0.161E-01 | 0.898E-02  | -0.554E-02  | 0.833E-02      | -0.446E-02  |
| c= 0.57E+19 | 10000. | 0.372E-01 | -0.124E-01 | 0.945E-02  | -0.628E-02  | 0.865E-02      | -0.507E-02  |
|             | 20000. | 0.438E-01 | -0.103E-01 | 0.100E-01  | -0.707E-02  | 0.906E-02      | -0.573E-02  |
|             | 30000. | 0.470E-01 | -0.800E-02 | 0.104E-01  | -0.758E-02  | 0.933E-02      | -0.614E-02  |
|             | 80000. | 0.531E-01 | -0.387E-02 | 0.116E-01  | -0.896E-02  | 0.101E-01      | -0.725E-02  |
| 4S - 6P     | 2500.  | 0.556E-01 | -0.353E-01 | 0.150E-01  | -0.952E-02  | 0.137E-01      | -0.760E-02  |
| 8650.3A     | 5000.  | 0.604E-01 | -0.310E-01 | 0.159E-01  | -0.109E-01  | 0.143E-01      | -0.879E-02  |
| c= 0.19E+19 | 10000. | 0.687E-01 | -0.217E-01 | 0.170E-01  | -0.125E-01  | 0.151E-01      | -0.100E-01  |
|             | 20000. | 0.793E-01 | -0.156E-01 | 0.184E-01  | -0.141E-01  | 0.161E-01      | -0.114E-01  |
|             | 30000. | 0.834E-01 | -0.116E-01 | 0.192E-01  | -0.152E-01  | 0.168E-01      | -0.123E-01  |
|             | 80000. | 0.902E-01 | -0.292E-02 | 0.218E-01  | -0.180E-01  | 0.186E-01      | -0.145E-01  |
| 4S - 7P     | 2500.  | 0.107     | -0.664E-01 | 0.276E-01* | -0.184E-01* | 0.246E-01*     | -0.145E-01* |
| 7810.0A     | 5000.  | 0.116     | -0.598E-01 | 0.297E-01  | -0.214E-01  | 0.262E-01*     | -0.171E-01* |
| c= 0.94E+18 | 10000. | 0.132     | -0.423E-01 | 0.321E-01  | -0.246E-01  | 0.280E-01*     | -0.198E-01* |
|             | 20000. | 0.150     | -0.301E-01 | 0.349E-01  | -0.280E-01  | 0.301E-01      | -0.226E-01  |
|             | 30000. | 0.156     | -0.197E-01 | 0.368E-01  | -0.302E-01  | 0.315E-01      | -0.243E-01  |
|             | 80000. | 0.164     | -0.312E-02 | 0.421E-01  | -0.358E-01  | 0.355E-01      | -0.290E-01  |
| 4S - 8P     | 2500.  | 0.198     | -0.129     | 0.494E-01* | -0.330E-01* |                |             |
| 7373.3A     | 5000.  | 0.213     | -0.110     | 0.536E-01* | -0.393E-01* | 0.466E-01*     | -0.311E-01* |
| c= 0.53E+18 | 10000. | 0.242     | -0.781E-01 | 0.584E-01* | -0.457E-01* | 0.502E-01*     | -0.365E-01* |
|             | 20000. | 0.271     | -0.523E-01 | 0.640E-01* | -0.524E-01* | 0.545E-01*     | -0.421E-01* |
|             | 30000. | 0.280     | -0.340E-01 | 0.677E-01  | -0.566E-01  | 0.573E-01*     | -0.455E-01* |
|             | 80000. | 0.288     | -0.523E-02 | 0.781E-01  | -0.676E-01  | 0.651E-01*     | -0.545E-01* |
| 4S - 9P     | 2500.  | 0.346     | -0.210     |            |             |                |             |
| 7113.0A     | 5000.  | 0.370     | -0.177     |            |             |                |             |
| c= 0.33E+18 | 10000. | 0.422     | -0.132     | 0.101*     | -0.794E-01* |                |             |
|             | 20000. | 0.465     | -0.853E-01 | 0.111*     | -0.919E-01* |                |             |
|             | 30000. | 0.477     | -0.548E-01 | 0.118*     | -0.995E-01* | 0.990E-01*     | -0.779E-01* |
|             | 80000. | 0.483     | -0.103E-01 | 0.137*     | -0.119*     | 0.113*         | -0.963E-01* |
| 4S -10P     | 2500.  | 0.575     | -0.364     |            |             |                |             |
| 6944.0A     | 5000.  | 0.614     | -0.290     |            |             |                |             |
| c= 0.22E+18 | 10000. | 0.698     | -0.202     |            |             |                |             |
|             | 20000. | 0.758     | -0.130     |            |             |                |             |
|             | 30000. | 0.774     | -0.918E-01 |            |             |                |             |
|             | 80000. | 0.771     | -0.197E-01 | 0.229*     | -0.200*     |                |             |
| 4P - 6S     | 2500.  | 0.890E-01 | 0.582E-01  | 0.175E-01  | 0.153E-01   | 0.145E-01      | 0.123E-01   |
| 16384.0A    | 5000.  | 0.103     | 0.672E-01  | 0.195E-01  | 0.175E-01   | 0.160E-01      | 0.141E-01   |
| c= 0.25E+20 | 10000. | 0.114     | 0.691E-01  | 0.218E-01  | 0.198E-01   | 0.179E-01      | 0.160E-01   |
|             | 20000. | 0.129     | 0.634E-01  | 0.243E-01  | 0.224E-01   | 0.199E-01      | 0.181E-01   |
|             | 30000. | 0.142     | 0.544E-01  | 0.260E-01  | 0.240E-01   | 0.212E-01      | 0.194E-01   |
|             | 80000. | 0.174     | 0.382E-01  | 0.305E-01  | 0.284E-01   | 0.248E-01      | 0.230E-01   |

| NE= 0.1E+15 |        |                      |           |                    |            |                           |            |
|-------------|--------|----------------------|-----------|--------------------|------------|---------------------------|------------|
| TRANSITION  | T (K)  | ELECTRONS<br>2WE (A) | DE (A)    | PROTONS<br>2WI (A) | DI (A)     | IONIZED HELIUM<br>2WI (A) | DI (A)     |
| 4P - 7S     | 2500.  | 0.117                | 0.801E-01 | 0.227E-01          | 0.201E-01  | 0.185E-01                 | 0.160E-01  |
| 12915.0A    | 5000.  | 0.133                | 0.935E-01 | 0.255E-01          | 0.231E-01  | 0.207E-01                 | 0.185E-01  |
| c= 0.88E+19 | 10000. | 0.151                | 0.877E-01 | 0.286E-01          | 0.263E-01  | 0.232E-01                 | 0.212E-01  |
|             | 20000. | 0.174                | 0.751E-01 | 0.321E-01          | 0.298E-01  | 0.260E-01                 | 0.240E-01  |
|             | 30000. | 0.195                | 0.629E-01 | 0.343E-01          | 0.320E-01  | 0.278E-01                 | 0.259E-01  |
|             | 80000. | 0.233                | 0.394E-01 | 0.404E-01          | 0.379E-01  | 0.327E-01                 | 0.306E-01  |
| 4P - 8S     | 2500.  | 0.178                | 0.121     | 0.343E-01          | 0.298E-01  | 0.278E-01*                | 0.236E-01* |
| 11495.0A    | 5000.  | 0.203                | 0.133     | 0.385E-01          | 0.345E-01  | 0.312E-01                 | 0.276E-01  |
| c= 0.44E+19 | 10000. | 0.235                | 0.129     | 0.432E-01          | 0.395E-01  | 0.350E-01                 | 0.318E-01  |
|             | 20000. | 0.281                | 0.100     | 0.485E-01          | 0.449E-01  | 0.393E-01                 | 0.362E-01  |
|             | 30000. | 0.315                | 0.825E-01 | 0.519E-01          | 0.484E-01  | 0.421E-01                 | 0.390E-01  |
|             | 80000. | 0.368                | 0.465E-01 | 0.612E-01          | 0.573E-01  | 0.495E-01                 | 0.464E-01  |
| 4P - 9S     | 2500.  | 0.277                | 0.185     | 0.528E-01*         | 0.445E-01* | 0.428E-01*                | 0.351E-01* |
| 10745.0A    | 5000.  | 0.317                | 0.195     | 0.593E-01          | 0.523E-01  | 0.481E-01*                | 0.416E-01* |
| c= 0.25E+19 | 10000. | 0.379                | 0.181     | 0.666E-01          | 0.603E-01  | 0.539E-01*                | 0.483E-01* |
|             | 20000. | 0.464                | 0.136     | 0.747E-01          | 0.688E-01  | 0.605E-01                 | 0.554E-01  |
|             | 30000. | 0.519                | 0.111     | 0.800E-01          | 0.741E-01  | 0.648E-01                 | 0.597E-01  |
|             | 80000. | 0.594                | 0.572E-01 | 0.944E-01          | 0.882E-01  | 0.763E-01                 | 0.714E-01  |
| 4P - 4D     | 2500.  | 0.451                | 0.213     | 0.118              | 0.103      | 0.961E-01                 | 0.816E-01  |
| 23370.0A    | 5000.  | 0.433                | 0.185     | 0.133              | 0.119      | 0.108                     | 0.950E-01  |
| c= 0.22E+19 | 10000. | 0.408                | 0.147     | 0.149              | 0.136      | 0.121                     | 0.109      |
|             | 20000. | 0.381                | 0.105     | 0.170              | 0.154      | 0.136                     | 0.124      |
|             | 30000. | 0.367                | 0.824E-01 | 0.184              | 0.166      | 0.145                     | 0.134      |
|             | 80000. | 0.329                | 0.432E-01 | 0.221              | 0.202      | 0.174                     | 0.159      |
| 4P - 5D     | 2500.  | 0.599                | 0.269     | 0.166*             | 0.134*     |                           |            |
| 14776.0A    | 5000.  | 0.566                | 0.224     | 0.187*             | 0.160*     | 0.151*                    | 0.127*     |
| c= 0.45E+18 | 10000. | 0.525                | 0.171     | 0.210*             | 0.186*     | 0.170*                    | 0.149*     |
|             | 20000. | 0.481                | 0.115     | 0.239              | 0.213      | 0.191*                    | 0.171*     |
|             | 30000. | 0.453                | 0.891E-01 | 0.259              | 0.231      | 0.204*                    | 0.185*     |
|             | 80000. | 0.385                | 0.408E-01 | 0.311              | 0.283      | 0.245                     | 0.222      |
| 4P - 6D     | 2500.  | 0.998                | 0.423     |                    |            |                           |            |
| 12318.0A    | 5000.  | 0.939                | 0.341     |                    |            |                           |            |
| c= 0.20E+18 | 10000. | 0.869                | 0.236     |                    |            |                           |            |
|             | 20000. | 0.791                | 0.144     | 0.410*             | 0.358*     |                           |            |
|             | 30000. | 0.742                | 0.111     | 0.444*             | 0.389*     |                           |            |
|             | 80000. | 0.618                | 0.414E-01 | 0.533*             | 0.482*     | 0.420*                    | 0.376*     |
| 4P - 7D     | 2500.  | 1.69                 | 0.654     |                    |            |                           |            |
| 11195.0A    | 5000.  | 1.59                 | 0.522     |                    |            |                           |            |
| c= 0.10E+18 | 10000. | 1.47                 | 0.349     |                    |            |                           |            |
|             | 20000. | 1.33                 | 0.220     |                    |            |                           |            |
|             | 30000. | 1.24                 | 0.158     |                    |            |                           |            |
|             | 80000. | 1.02                 | 0.493E-01 |                    |            |                           |            |
| 4P - 8D     | 2500.  | 2.76                 | 0.938     |                    |            |                           |            |
| 10570.0A    | 5000.  | 2.60                 | 0.743     |                    |            |                           |            |
| c= 0.56E+17 | 10000. | 2.40                 | 0.437     |                    |            |                           |            |
|             | 20000. | 2.17                 | 0.301     |                    |            |                           |            |
|             | 30000. | 2.02                 | 0.185     |                    |            |                           |            |
|             | 80000. | 1.65                 | 0.587E-01 |                    |            |                           |            |
| 4D - 6P     | 2500.  | 1.95                 | -0.997    | 0.410              | -0.327     | 0.345*                    | -0.259*    |
| 36390.1A    | 5000.  | 1.99                 | -0.921    | 0.454              | -0.380     | 0.379                     | -0.304     |
| c= 0.52E+19 | 10000. | 2.03                 | -0.673    | 0.504              | -0.436     | 0.418                     | -0.350     |
|             | 20000. | 2.14                 | -0.443    | 0.564              | -0.496     | 0.462                     | -0.400     |
|             | 30000. | 2.17                 | -0.347    | 0.604              | -0.534     | 0.492                     | -0.431     |
|             | 80000. | 2.15                 | -0.129    | 0.718              | -0.641     | 0.575                     | -0.513     |

# TABLES FOR NA I LINES STARK BROADENING PARAMETERS

| NE= 0.1E+15 |        |           |            |         |            |                |             |
|-------------|--------|-----------|------------|---------|------------|----------------|-------------|
| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS |            | IONIZED HELIUM |             |
|             |        | 2WE(A)    | DE(A)      | 2WI(A)  | DI(A)      | 2WI(A)         | DI(A)       |
| 4D - 7P     | 2500.  | 1.55      | -0.861     | 0.330*  | -0.241*    | 0.284*         | -0.190*     |
| 25050.1A    | 5000.  | 1.62      | -0.758     | 0.361*  | -0.283*    | 0.308*         | -0.225*     |
| c= 0.25E+19 | 10000. | 1.74      | -0.507     | 0.396   | -0.326     | 0.335*         | -0.261*     |
|             | 20000. | 1.88      | -0.287     | 0.438   | -0.372     | 0.367          | -0.300      |
|             | 30000. | 1.93      | -0.217     | 0.465   | -0.401     | 0.388          | -0.323      |
|             | 80000. | 1.95      | -0.626E-01 | 0.544   | -0.479     | 0.446          | -0.386      |
| 4D - 8P     | 2500.  | 1.93      | -1.05      | 0.425*  | -0.294*    |                |             |
| 21052.6A    | 5000.  | 2.03      | -0.854     | 0.464*  | -0.351*    |                |             |
| c= 0.18E+19 | 10000. | 2.24      | -0.471     | 0.509*  | -0.409*    | 0.433*         | -0.326*     |
|             | 20000. | 2.45      | -0.294     | 0.560*  | -0.469*    | 0.472*         | -0.377*     |
|             | 30000. | 2.51      | -0.206     | 0.594   | -0.506     | 0.498*         | -0.408*     |
|             | 80000. | 2.53      | -0.297E-01 | 0.691   | -0.606     | 0.571*         | -0.488*     |
| 4D - 9P     | 2500.  | 2.74      | -1.50      |         |            |                |             |
| 19062.1A    | 5000.  | 2.90      | -1.24      |         |            |                |             |
| c= 0.14E+19 | 10000. | 3.25      | -0.693     | 0.746*  | -0.591*    |                |             |
|             | 20000. | 3.54      | -0.320     | 0.823*  | -0.685*    |                |             |
|             | 30000. | 3.61      | -0.204     | 0.873*  | -0.741*    | 0.730*         | -0.595*     |
|             | 80000. | 3.62      | -0.853E-02 | 1.02*   | -0.890*    | 0.838*         | -0.717*     |
| 4D -10P     | 2500.  | 4.04      | -2.43      |         |            |                |             |
| 17895.5A    | 5000.  | 4.29      | -1.84      |         |            |                |             |
| c= 0.13E+19 | 10000. | 4.83      | -0.981     |         |            |                |             |
|             | 20000. | 5.21      | -0.375     |         |            |                |             |
|             | 30000. | 5.30      | -0.279     |         |            |                |             |
|             | 80000. | 5.25      | -0.136     | 1.54*   | -1.35*     |                |             |
| 5S - 5P     | 2500.  | 0.948     | -0.573     | 0.235   | -0.148     | 0.217          | -0.118      |
| 54318.3A    | 5000.  | 1.06      | -0.608     | 0.249   | -0.168     | 0.226          | -0.135      |
| c= 0.15E+21 | 10000. | 1.20      | -0.572     | 0.265   | -0.191     | 0.237          | -0.154      |
|             | 20000. | 1.39      | -0.463     | 0.284   | -0.215     | 0.251          | -0.174      |
|             | 30000. | 1.52      | -0.389     | 0.297   | -0.230     | 0.261          | -0.186      |
|             | 80000. | 1.76      | -0.255     | 0.334   | -0.272     | 0.288          | -0.220      |
| 5S - 6P     | 2500.  | 0.470     | -0.301     | 0.121   | -0.785E-01 | 0.110          | -0.626E-01  |
| 24414.1A    | 5000.  | 0.515     | -0.291     | 0.129   | -0.903E-01 | 0.116          | -0.725E-01  |
| c= 0.15E+20 | 10000. | 0.584     | -0.223     | 0.139   | -0.103     | 0.123          | -0.829E-01  |
|             | 20000. | 0.680     | -0.162     | 0.150   | -0.117     | 0.131          | -0.941E-01  |
|             | 30000. | 0.725     | -0.128     | 0.157   | -0.125     | 0.136          | -0.101      |
|             | 80000. | 0.796     | -0.560E-01 | 0.178   | -0.148     | 0.152          | -0.120      |
| 5S - 7P     | 2500.  | 0.628     | -0.406     | 0.160*  | -0.107*    | 0.142*         | -0.842E-01* |
| 18726.6A    | 5000.  | 0.681     | -0.349     | 0.172   | -0.124     | 0.151*         | -0.992E-01* |
| c= 0.54E+19 | 10000. | 0.776     | -0.228     | 0.186   | -0.143     | 0.162*         | -0.115*     |
|             | 20000. | 0.887     | -0.158     | 0.202   | -0.163     | 0.174          | -0.131      |
|             | 30000. | 0.929     | -0.102     | 0.213   | -0.175     | 0.182          | -0.141      |
|             | 80000. | 0.986     | -0.329E-01 | 0.244   | -0.208     | 0.206          | -0.169      |
| 5S - 8P     | 2500.  | 0.987     | -0.642     | 0.245*  | -0.164*    |                |             |
| 16398.8A    | 5000.  | 1.06      | -0.534     | 0.266*  | -0.195*    | 0.231*         | -0.155*     |
| c= 0.26E+19 | 10000. | 1.21      | -0.348     | 0.290*  | -0.227*    | 0.249*         | -0.181*     |
|             | 20000. | 1.36      | -0.220     | 0.317*  | -0.260*    | 0.270*         | -0.209*     |
|             | 30000. | 1.41      | -0.102     | 0.335   | -0.281     | 0.284*         | -0.226*     |
|             | 80000. | 1.46      | -0.369E-01 | 0.387   | -0.336     | 0.323*         | -0.271*     |
| 5S - 9P     | 2500.  | 1.58      | -0.956     |         |            |                |             |
| 15165.3A    | 5000.  | 1.69      | -0.821     |         |            |                |             |
| c= 0.15E+19 | 10000. | 1.93      | -0.546     | 0.460*  | -0.361*    |                |             |
|             | 20000. | 2.13      | -0.335     | 0.507*  | -0.418*    |                |             |
|             | 30000. | 2.19      | -0.124     | 0.537*  | -0.453*    | 0.451*         | -0.364*     |
|             | 80000. | 2.22      | -0.587E-01 | 0.623*  | -0.543*    | 0.516*         | -0.438*     |

| NE= 0.1E+15 |        |           |            |           |            |                |            |
|-------------|--------|-----------|------------|-----------|------------|----------------|------------|
| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS   |            | IONIZED HELIUM |            |
|             |        | 2WE(A)    | DE(A)      | 2WI(A)    | DI(A)      | 2WI(A)         | DI(A)      |
| 5S - 10P    | 2500.  | 2.48      | -1.57      |           |            |                |            |
| 14417.5A    | 5000.  | 2.65      | -1.26      |           |            |                |            |
| c= 0.97E+18 | 10000. | 3.02      | -0.850     |           |            |                |            |
|             | 20000. | 3.28      | -0.515     |           |            |                |            |
|             | 30000. | 3.36      | -0.348     |           |            |                |            |
|             | 80000. | 3.35      | -0.986E-01 | 0.986*    | -0.861*    |                |            |
| 5P - 6S     | 2500.  | 2.80      | 1.73       | 0.574     | 0.430      | 0.502          | 0.345      |
| 75075.1A    | 5000.  | 3.24      | 1.95       | 0.623     | 0.492      | 0.539          | 0.396      |
| c= 0.28E+21 | 10000. | 3.67      | 1.96       | 0.680     | 0.558      | 0.582          | 0.450      |
|             | 20000. | 4.17      | 1.67       | 0.745     | 0.632      | 0.632          | 0.511      |
|             | 30000. | 4.58      | 1.42       | 0.788     | 0.677      | 0.665          | 0.548      |
|             | 80000. | 5.38      | 0.986      | 0.908     | 0.801      | 0.758          | 0.648      |
| 5P - 7S     | 2500.  | 0.969     | 0.605      | 0.182     | 0.152      | 0.152          | 0.121      |
| 33658.7A    | 5000.  | 1.13      | 0.694      | 0.202     | 0.174      | 0.168          | 0.140      |
| c= 0.56E+20 | 10000. | 1.29      | 0.702      | 0.224     | 0.199      | 0.186          | 0.160      |
|             | 20000. | 1.48      | 0.569      | 0.250     | 0.225      | 0.206          | 0.182      |
|             | 30000. | 1.64      | 0.467      | 0.266     | 0.242      | 0.219          | 0.196      |
|             | 80000. | 1.93      | 0.288      | 0.311     | 0.286      | 0.255          | 0.232      |
| 5D - 7P     | 2500.  | 11.5      | -3.51      | 3.37*     | -2.62*     |                |            |
| 66489.4A    | 5000.  | 11.0      | -2.39      | 3.76*     | -3.11*     | 3.10*          | -2.4*      |
| c= 0.91E+19 | 10000. | 10.3      | -1.41      | 4.21*     | -3.61*     | 3.44*          | -2.8*      |
|             | 20000. | 9.47      | -0.584     | 4.76      | -4.14      | 3.83*          | -3.3*      |
|             | 30000. | 8.92      | -0.267     | 5.15      | -4.48      | 4.09*          | -3.6*      |
|             | 80000. | 7.56      | 0.174      | 6.14      | -5.53      | 4.88           | -4.31      |
| 5D - 8P     | 2500.  | 12.1      | -5.79      |           |            |                |            |
| 44208.7A    | 5000.  | 12.5      | -4.35      | 2.78*     | -2.21*     |                |            |
| c= 0.40E+19 | 10000. | 13.0      | -2.23      | 3.09*     | -2.59*     |                |            |
|             | 20000. | 13.6      | -1.63      | 3.45*     | -2.99*     | 2.83*          | -2.40*     |
|             | 30000. | 13.7      | -1.01      | 3.69*     | -3.23*     | 3.01*          | -2.60*     |
|             | 80000. | 13.2      | -0.113     | 4.39*     | -3.91*     | 3.52*          | -3.12*     |
| 5D - 9P     | 2500.  | 12.4      | -6.45      |           |            |                |            |
| 36258.2A    | 5000.  | 12.8      | -4.36      |           |            |                |            |
| c= 0.27E+19 | 10000. | 13.8      | -2.31      |           |            |                |            |
|             | 20000. | 14.7      | -1.20      | 3.48*     | -2.96*     |                |            |
|             | 30000. | 14.8      | -0.914     | 3.71*     | -3.20*     |                |            |
|             | 80000. | 14.5      | -0.299E-01 | 4.37*     | -3.86*     | 3.55*          | -3.10*     |
| 3S - 3P     | 2500.  | 0.191E-02 | 0.132E-02  | 0.126E-02 | 0.366E-03  | 0.125E-02      | 0.296E-03  |
| 5891.8A     | 5000.  | 0.211E-02 | 0.155E-02  | 0.127E-02 | 0.414E-03  | 0.126E-02      | 0.335E-03  |
| c= 0.30E+20 | 10000. | 0.249E-02 | 0.178E-02  | 0.129E-02 | 0.466E-03  | 0.127E-02      | 0.377E-03  |
|             | 20000. | 0.322E-02 | 0.182E-02  | 0.130E-02 | 0.525E-03  | 0.128E-02      | 0.425E-03  |
|             | 30000. | 0.381E-02 | 0.183E-02  | 0.132E-02 | 0.562E-03  | 0.128E-02      | 0.455E-03  |
|             | 80000. | 0.551E-02 | 0.129E-02  | 0.136E-02 | 0.663E-03  | 0.131E-02      | 0.537E-03  |
| 3S - 4P     | 2500.  | 0.649E-02 | -0.239E-02 | 0.223E-02 | -0.764E-03 | 0.219E-02      | -0.612E-03 |
| 3302.6A     | 5000.  | 0.725E-02 | -0.146E-02 | 0.226E-02 | -0.873E-03 | 0.222E-02      | -0.702E-03 |
| c= 0.12E+19 | 10000. | 0.864E-02 | -0.442E-03 | 0.230E-02 | -0.991E-03 | 0.224E-02      | -0.799E-03 |
|             | 20000. | 0.100E-01 | 0.234E-03  | 0.236E-02 | -0.112E-02 | 0.227E-02      | -0.906E-03 |
|             | 30000. | 0.108E-01 | 0.579E-03  | 0.239E-02 | -0.120E-02 | 0.230E-02      | -0.972E-03 |
|             | 80000. | 0.126E-01 | 0.634E-03  | 0.251E-02 | -0.142E-02 | 0.237E-02      | -0.115E-02 |
| 3S - 5P     | 2500.  | 0.202E-01 | -0.110E-01 | 0.595E-02 | -0.307E-02 | 0.558E-02*     | -0.242E-02 |
| 2852.8A     | 5000.  | 0.221E-01 | -0.983E-02 | 0.623E-02 | -0.360E-02 | 0.579E-02*     | -0.287E-02 |
| c= 0.40E+18 | 10000. | 0.254E-01 | -0.662E-02 | 0.655E-02 | -0.415E-02 | 0.602E-02      | -0.333E-02 |
|             | 20000. | 0.295E-01 | -0.464E-02 | 0.695E-02 | -0.474E-02 | 0.629E-02      | -0.381E-02 |
|             | 30000. | 0.313E-01 | -0.344E-02 | 0.721E-02 | -0.510E-02 | 0.648E-02      | -0.411E-02 |
|             | 80000. | 0.347E-01 | -0.115E-02 | 0.799E-02 | -0.605E-02 | 0.703E-02      | -0.491E-02 |

# TABLES FOR NA I LINES STARK BROADENING PARAMETERS

NE= 0.1E+16

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS    |             | IONIZED HELIUM |             |
|-------------|--------|-----------|------------|------------|-------------|----------------|-------------|
|             |        | 2WE(A)    | DE(A)      | 2WI(A)     | DI(A)       | 2WI(A)         | DI(A)       |
| 3S - 6P     | 2500.  | 0.528E-01 | -0.325E-01 | 0.141E-01* | -0.782E-02* |                |             |
| 2680.4A     | 5000.  | 0.573E-01 | -0.281E-01 | 0.152E-01* | -0.955E-02* |                |             |
| c= 0.19E+18 | 10000. | 0.653E-01 | -0.202E-01 | 0.163E-01* | -0.113E-01* | 0.145E-01*     | -0.895E-02* |
|             | 20000. | 0.749E-01 | -0.145E-01 | 0.175E-01* | -0.130E-01* | 0.154E-01*     | -0.104E-01* |
|             | 30000. | 0.785E-01 | -0.109E-01 | 0.184E-01  | -0.141E-01  | 0.160E-01*     | -0.113E-01* |
|             | 80000. | 0.843E-01 | -0.365E-02 | 0.208E-01  | -0.169E-01  | 0.178E-01*     | -0.137E-01* |
| 3S - 7P     | 2500.  | 0.118     | -0.687E-01 |            |             |                |             |
| 2593.9A     | 5000.  | 0.127     | -0.634E-01 |            |             |                |             |
| c= 0.10E+18 | 10000. | 0.145     | -0.458E-01 |            |             |                |             |
|             | 20000. | 0.164     | -0.332E-01 | 0.384E-01* | -0.292E-01* |                |             |
|             | 30000. | 0.170     | -0.245E-01 | 0.405E-01* | -0.319E-01* |                |             |
|             | 80000. | 0.178     | -0.749E-02 | 0.464E-01* | -0.387E-01* | 0.391E-01*     | -0.311E-01* |
| 3S - 8P     | 2500.  | 0.235     | -0.141     |            |             |                |             |
| 2543.8A     | 5000.  | 0.252     | -0.119     |            |             |                |             |
| c= 0.63E+17 | 10000. | 0.288     | -0.877E-01 |            |             |                |             |
|             | 20000. | 0.321     | -0.656E-01 |            |             |                |             |
|             | 30000. | 0.331     | -0.450E-01 |            |             |                |             |
|             | 80000. | 0.340     | -0.126E-01 |            |             |                |             |
| 3S - 9P     | 2500.  | 0.430     | -0.225     |            |             |                |             |
| 2512.1A     | 5000.  | 0.460     | -0.205     |            |             |                |             |
| c= 0.42E+17 | 10000. | 0.525     | -0.142     |            |             |                |             |
|             | 20000. | 0.578     | -0.103     |            |             |                |             |
|             | 30000. | 0.593     | -0.730E-01 |            |             |                |             |
|             | 80000. | 0.600     | -0.230E-01 |            |             |                |             |
| 3S -10P     | 2500.  | 0.730*    | -0.388*    |            |             |                |             |
| 2490.7A     | 5000.  | 0.783     | -0.320     |            |             |                |             |
| c= 0.29E+17 | 10000. | 0.894     | -0.235     |            |             |                |             |
|             | 20000. | 0.971     | -0.158     |            |             |                |             |
|             | 30000. | 0.992     | -0.110     |            |             |                |             |
|             | 80000. | 0.989     | -0.270E-01 |            |             |                |             |
| 3P - 4S     | 2500.  | 0.367E-01 | 0.262E-01  | 0.856E-02  | 0.683E-02   | 0.736E-02      | 0.548E-02   |
| 11397.0A    | 5000.  | 0.420E-01 | 0.300E-01  | 0.938E-02  | 0.778E-02   | 0.798E-02      | 0.626E-02   |
| c= 0.59E+20 | 10000. | 0.466E-01 | 0.356E-01  | 0.103E-01  | 0.882E-02   | 0.871E-02      | 0.712E-02   |
|             | 20000. | 0.515E-01 | 0.334E-01  | 0.114E-01  | 0.995E-02   | 0.954E-02      | 0.806E-02   |
|             | 30000. | 0.552E-01 | 0.329E-01  | 0.121E-01  | 0.107E-01   | 0.101E-01      | 0.863E-02   |
|             | 80000. | 0.702E-01 | 0.228E-01  | 0.140E-01  | 0.126E-01   | 0.116E-01      | 0.102E-01   |
| 3P - 5S     | 2500.  | 0.405E-01 | 0.289E-01  | 0.866E-02  | 0.750E-02   | 0.705E-02      | 0.596E-02   |
| 6158.6A     | 5000.  | 0.468E-01 | 0.349E-01  | 0.971E-02  | 0.868E-02   | 0.790E-02      | 0.695E-02   |
| c= 0.70E+19 | 10000. | 0.508E-01 | 0.382E-01  | 0.109E-01  | 0.993E-02   | 0.884E-02      | 0.799E-02   |
|             | 20000. | 0.563E-01 | 0.365E-01  | 0.122E-01  | 0.113E-01   | 0.991E-02      | 0.910E-02   |
|             | 30000. | 0.589E-01 | 0.339E-01  | 0.130E-01  | 0.121E-01   | 0.106E-01      | 0.979E-02   |
|             | 80000. | 0.732E-01 | 0.254E-01  | 0.154E-01  | 0.144E-01   | 0.125E-01      | 0.116E-01   |
| 3P - 6S     | 2500.  | 0.780E-01 | 0.562E-01  | 0.162E-01  | 0.134E-01   | 0.131E-01*     | 0.105E-01*  |
| 5151.9A     | 5000.  | 0.892E-01 | 0.640E-01  | 0.182E-01  | 0.158E-01   | 0.147E-01      | 0.126E-01   |
| c= 0.25E+19 | 10000. | 0.974E-01 | 0.673E-01  | 0.204E-01  | 0.183E-01   | 0.165E-01      | 0.147E-01   |
|             | 20000. | 0.110     | 0.640E-01  | 0.229E-01  | 0.210E-01   | 0.186E-01      | 0.169E-01   |
|             | 30000. | 0.119     | 0.545E-01  | 0.245E-01  | 0.226E-01   | 0.199E-01      | 0.182E-01   |
|             | 80000. | 0.146     | 0.375E-01  | 0.289E-01  | 0.270E-01   | 0.234E-01      | 0.218E-01   |
| 3P - 7S     | 2500.  | 0.152     | 0.104      | 0.302E-01* | 0.233E-01*  | 0.245E-01*     | 0.178E-01*  |
| 4750.6A     | 5000.  | 0.173     | 0.121      | 0.339E-01* | 0.284E-01*  | 0.275E-01*     | 0.223E-01*  |
| c= 0.12E+19 | 10000. | 0.190     | 0.117      | 0.381E-01  | 0.334E-01   | 0.309E-01*     | 0.266E-01*  |
|             | 20000. | 0.219     | 0.101      | 0.428E-01  | 0.386E-01   | 0.347E-01*     | 0.309E-01*  |
|             | 30000. | 0.245     | 0.843E-01  | 0.458E-01  | 0.418E-01   | 0.371E-01*     | 0.336E-01*  |
|             | 80000. | 0.293     | 0.528E-01  | 0.540E-01  | 0.501E-01   | 0.437E-01      | 0.404E-01   |



| NE= 0.1E+16 |        |                     |           |                   |            |                          |            |
|-------------|--------|---------------------|-----------|-------------------|------------|--------------------------|------------|
| TRANSITION  | T(K)   | ELECTRONS<br>2WE(A) | DE(A)     | PROTONS<br>2WI(A) | DI(A)      | IONIZED HELIUM<br>2WI(A) | DI(A)      |
| 3P - 8S     | 2500.  | 0.271               | 0.180     |                   |            |                          |            |
| 4544.2A     | 5000.  | 0.307               | 0.202     | 0.598E-01*        | 0.474E-01* |                          |            |
| c= 0.68E+18 | 10000. | 0.361               | 0.198     | 0.672E-01*        | 0.571E-01* | 0.544E-01*               | 0.450E-01* |
|             | 20000. | 0.423               | 0.151     | 0.754E-01*        | 0.668E-01* | 0.611E-01*               | 0.532E-01* |
|             | 30000. | 0.475               | 0.125     | 0.807E-01*        | 0.726E-01* | 0.654E-01*               | 0.581E-01* |
|             | 80000. | 0.555               | 0.692E-01 | 0.952E-01         | 0.877E-01  | 0.770E-01*               | 0.706E-01* |
| 3P - 9S     | 2500.  | 0.460               | 0.291     |                   |            |                          |            |
| 4423.5A     | 5000.  | 0.526               | 0.315     |                   |            |                          |            |
| c= 0.43E+18 | 10000. | 0.627               | 0.298     |                   |            |                          |            |
|             | 20000. | 0.770               | 0.217     | 0.125*            | 0.108*     |                          |            |
|             | 30000. | 0.861               | 0.177     | 0.134*            | 0.119*     |                          |            |
|             | 80000. | 0.986               | 0.694E-01 | 0.158*            | 0.144*     | 0.128*                   | 0.116*     |
| 3P - 3D     | 2500.  | 0.312E-01           | 0.226E-01 | 0.814E-02         | 0.589E-02  | 0.720E-02                | 0.472E-02  |
| 8191.1A     | 5000.  | 0.355E-01           | 0.246E-01 | 0.879E-02         | 0.674E-02  | 0.768E-02                | 0.542E-02  |
| c= 0.74E+19 | 10000. | 0.385E-01           | 0.246E-01 | 0.955E-02         | 0.766E-02  | 0.825E-02                | 0.618E-02  |
|             | 20000. | 0.413E-01           | 0.227E-01 | 0.104E-01         | 0.868E-02  | 0.892E-02                | 0.701E-02  |
|             | 30000. | 0.428E-01           | 0.201E-01 | 0.110E-01         | 0.930E-02  | 0.936E-02                | 0.753E-02  |
|             | 80000. | 0.474E-01           | 0.137E-01 | 0.126E-01         | 0.110E-01  | 0.106E-01                | 0.891E-02  |
| 3P - 4D     | 2500.  | 0.253               | 0.112     | 0.697E-01*        | 0.499E-01* |                          |            |
| 5686.4A     | 5000.  | 0.242               | 0.993E-01 | 0.783E-01*        | 0.624E-01* |                          |            |
| c= 0.13E+18 | 10000. | 0.225               | 0.804E-01 | 0.882E-01*        | 0.746E-01* | 0.713E-01*               | 0.590E-01* |
|             | 20000. | 0.207               | 0.593E-01 | 0.100*            | 0.869E-01* | 0.800E-01*               | 0.694E-01* |
|             | 30000. | 0.196               | 0.475E-01 | 0.108*            | 0.945E-01* | 0.857E-01*               | 0.757E-01* |
|             | 80000. | 0.170               | 0.262E-01 | 0.130             | 0.117      | 0.103*                   | 0.916E-01* |
| 3P - 5D     | 2500.  | 0.644               | 0.246     |                   |            |                          |            |
| 4981.4A     | 5000.  | 0.613               | 0.221     |                   |            |                          |            |
| c= 0.52E+17 | 10000. | 0.571               | 0.171     |                   |            |                          |            |
|             | 20000. | 0.523               | 0.117     |                   |            |                          |            |
|             | 30000. | 0.492               | 0.922E-01 |                   |            |                          |            |
|             | 80000. | 0.414               | 0.426E-01 |                   |            |                          |            |
| 3P - 6D     | 2500.  | 1.27                | 0.434     |                   |            |                          |            |
| 4667.5A     | 5000.  | 1.23                | 0.387     |                   |            |                          |            |
| c= 0.28E+17 | 10000. | 1.16                | 0.302     |                   |            |                          |            |
|             | 20000. | 1.07                | 0.204     |                   |            |                          |            |
|             | 30000. | 1.01                | 0.158     |                   |            |                          |            |
|             | 80000. | 0.846               | 0.630E-01 |                   |            |                          |            |
| 3P - 7D     | 2500.  | 2.15                | 0.670     |                   |            |                          |            |
| 4496.6A     | 5000.  | 2.15                | 0.602     |                   |            |                          |            |
| c= 0.17E+17 | 10000. | 2.07                | 0.455     |                   |            |                          |            |
|             | 20000. | 1.93                | 0.319     |                   |            |                          |            |
|             | 30000. | 1.83                | 0.242     |                   |            |                          |            |
|             | 80000. | 1.54                | 0.851E-01 |                   |            |                          |            |
| 3P - 8D     | 2500.  | 3.20                | 0.910     |                   |            |                          |            |
| 4392.3A     | 5000.  | 3.39                | 0.833     |                   |            |                          |            |
| c= 0.96E+16 | 10000. | 3.37                | 0.663     |                   |            |                          |            |
|             | 20000. | 3.19                | 0.428     |                   |            |                          |            |
|             | 30000. | 3.03                | 0.336     |                   |            |                          |            |
|             | 80000. | 2.57                | 0.108     |                   |            |                          |            |
| 3P - 9D     | 2500.  | 4.30*               | 1.21*     |                   |            |                          |            |
| 4323.5A     | 5000.  | 4.89                | 1.14      |                   |            |                          |            |
| c= 0.67E+16 | 10000. | 5.05                | 0.901     |                   |            |                          |            |
|             | 20000. | 4.88                | 0.624     |                   |            |                          |            |
|             | 30000. | 4.67                | 0.454     |                   |            |                          |            |
|             | 80000. | 4.00                | 0.138     |                   |            |                          |            |

## TABLES FOR NA I LINES STARK BROADENING PARAMETERS

| NE= 0.1E+16 |        |           |            |         |            |                |             |
|-------------|--------|-----------|------------|---------|------------|----------------|-------------|
| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS |            | IONIZED HELIUM |             |
|             |        | 2WE(A)    | DE(A)      | 2WI(A)  | DI(A)      | 2WI(A)         | DI(A)       |
| 3D - 4P     | 2500.  | 7.34      | -4.19      | 1.69    | -1.04      | 1.55           | -0.831      |
| 91050.0A    | 5000.  | 8.14      | -4.26      | 1.79    | -1.20      | 1.62           | -0.960      |
| c= 0.91E+21 | 10000. | 9.01      | -3.35      | 1.91    | -1.36      | 1.71           | -1.10       |
|             | 20000. | 10.5      | -2.52      | 2.05    | -1.55      | 1.81           | -1.25       |
|             | 30000. | 11.4      | -2.21      | 2.14    | -1.66      | 1.88           | -1.34       |
|             | 80000. | 13.1      | -1.29      | 2.41    | -1.96      | 2.07           | -1.59       |
| 3D - 5P     | 2500.  | 0.785     | -0.457     | 0.206   | -0.117     | 0.190*         | -0.917E-01* |
| 17038.7A    | 5000.  | 0.874     | -0.440     | 0.218   | -0.137     | 0.199*         | -0.109*     |
| c= 0.14E+20 | 10000. | 0.986     | -0.327     | 0.232   | -0.158     | 0.209          | -0.127      |
|             | 20000. | 1.15      | -0.260     | 0.248   | -0.180     | 0.221          | -0.145      |
|             | 30000. | 1.23      | -0.226     | 0.259   | -0.194     | 0.229          | -0.157      |
|             | 80000. | 1.36      | -0.104     | 0.290   | -0.231     | 0.251          | -0.187      |
| 3D - 6P     | 2500.  | 1.14      | -0.670     | 0.295*  | -0.167*    |                |             |
| 12309.2A    | 5000.  | 1.25      | -0.627     | 0.317*  | -0.204*    |                |             |
| c= 0.39E+19 | 10000. | 1.42      | -0.446     | 0.341*  | -0.240*    | 0.301*         | -0.191*     |
|             | 20000. | 1.63      | -0.309     | 0.369*  | -0.278*    | 0.322*         | -0.223*     |
|             | 30000. | 1.71      | -0.229     | 0.387   | -0.301     | 0.336*         | -0.242*     |
|             | 80000. | 1.84      | -0.564E-01 | 0.439   | -0.361     | 0.374          | -0.291      |
| 3D - 7P     | 2500.  | 2.01      | -1.17      |         |            |                |             |
| 10674.6A    | 5000.  | 2.18      | -1.09      |         |            |                |             |
| c= 0.18E+19 | 10000. | 2.48      | -0.747     |         |            |                |             |
|             | 20000. | 2.81      | -0.467     | 0.650*  | -0.497*    |                |             |
|             | 30000. | 2.92      | -0.356     | 0.685*  | -0.542*    |                |             |
|             | 80000. | 3.07      | -0.537E-01 | 0.786*  | -0.656*    | 0.661*         | -0.528*     |
| 3D - 8P     | 2500.  | 3.56      | -2.12      |         |            |                |             |
| 9875.6A     | 5000.  | 3.82      | -1.82      |         |            |                |             |
| c= 0.96E+18 | 10000. | 4.36      | -1.26      |         |            |                |             |
|             | 20000. | 4.87      | -0.752     |         |            |                |             |
|             | 30000. | 5.03      | -0.584     |         |            |                |             |
|             | 80000. | 5.17      | -0.881E-01 |         |            |                |             |
| 3D - 9P     | 2500.  | 6.05      | -3.16      |         |            |                |             |
| 9414.4A     | 5000.  | 6.48      | -2.89      |         |            |                |             |
| c= 0.58E+18 | 10000. | 7.40      | -2.05      |         |            |                |             |
|             | 20000. | 8.15      | -1.23      |         |            |                |             |
|             | 30000. | 8.36      | -0.957     |         |            |                |             |
|             | 80000. | 8.46      | -0.175     |         |            |                |             |
| 3D -10P     | 2500.  | 9.80*     | -5.10*     |         |            |                |             |
| 9120.8A     | 5000.  | 10.5      | -4.27      |         |            |                |             |
| c= 0.39E+18 | 10000. | 12.0      | -3.21      |         |            |                |             |
|             | 20000. | 13.0      | -1.95      |         |            |                |             |
|             | 30000. | 13.3      | -1.51      |         |            |                |             |
|             | 80000. | 13.3      | -0.332     |         |            |                |             |
| 3D - 4F     | 2500.  | 1.86      | -0.496     | 0.551*  | -0.412*    | 0.447*         | -0.314*     |
| 18465.3A    | 5000.  | 1.77      | -0.317     | 0.620*  | -0.507*    | 0.502*         | -0.397*     |
| c= 0.14E+19 | 10000. | 1.64      | -0.176     | 0.701*  | -0.600*    | 0.563*         | -0.476*     |
|             | 20000. | 1.49      | -0.755E-01 | 0.800   | -0.701     | 0.634*         | -0.557*     |
|             | 30000. | 1.41      | -0.425E-01 | 0.870   | -0.759     | 0.681*         | -0.605*     |
|             | 80000. | 1.26      | 0.221E-01  | 1.03    | -0.960     | 0.821          | -0.731      |
| 4S - 4P     | 2500.  | 0.356     | -0.186     | 0.105   | -0.479E-01 | 0.101          | -0.383E-01  |
| 22070.0A    | 5000.  | 0.385     | -0.188     | 0.108   | -0.549E-01 | 0.103          | -0.441E-01  |
| c= 0.53E+20 | 10000. | 0.440     | -0.165     | 0.112   | -0.625E-01 | 0.106          | -0.504E-01  |
|             | 20000. | 0.529     | -0.124     | 0.117   | -0.708E-01 | 0.109          | -0.571E-01  |
|             | 30000. | 0.589     | -0.105     | 0.120   | -0.760E-01 | 0.111          | -0.614E-01  |
|             | 80000. | 0.723     | -0.658E-01 | 0.130   | -0.898E-01 | 0.118          | -0.727E-01  |

| NE= 0.1E+16 |        |           |            |           |             |                |             |  |
|-------------|--------|-----------|------------|-----------|-------------|----------------|-------------|--|
| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS   |             | IONIZED HELIUM |             |  |
|             |        | 2WE(A)    | DE(A)      | 2WI(A)    | DI(A)       | 2WI(A)         | DI(A)       |  |
| 4S - 5P     | 2500.  | 0.298     | -0.167     | 0.854E-01 | -0.449E-01  | 0.798E-01*     | -0.353E-01* |  |
| 10747.0A    | 5000.  | 0.325     | -0.160     | 0.896E-01 | -0.527E-01  | 0.830E-01*     | -0.420E-01* |  |
| c= 0.57E+19 | 10000. | 0.372     | -0.124     | 0.944E-01 | -0.608E-01  | 0.864E-01      | -0.487E-01  |  |
|             | 20000. | 0.438     | -0.103     | 0.100     | -0.694E-01  | 0.905E-01      | -0.558E-01  |  |
|             | 30000. | 0.470     | -0.800E-01 | 0.104     | -0.747E-01  | 0.933E-01      | -0.602E-01  |  |
|             | 80000. | 0.531     | -0.387E-01 | 0.116     | -0.890E-01  | 0.101          | -0.720E-01  |  |
| 4S - 6P     | 2500.  | 0.556     | -0.340     | 0.148*    | -0.818E-01* |                |             |  |
| 8650.3A     | 5000.  | 0.604     | -0.303     | 0.158*    | -0.100*     |                |             |  |
| c= 0.19E+19 | 10000. | 0.687     | -0.217     | 0.170*    | -0.118*     | 0.151*         | -0.938E-01* |  |
|             | 20000. | 0.793     | -0.155     | 0.183*    | -0.137*     | 0.161*         | -0.109*     |  |
|             | 30000. | 0.834     | -0.116     | 0.192     | -0.148      | 0.167*         | -0.119*     |  |
|             | 80000. | 0.902     | -0.292E-01 | 0.218     | -0.177      | 0.186          | -0.143      |  |
| 4S - 7P     | 2500.  | 1.07      | -0.623     |           |             |                |             |  |
| 7810.0A     | 5000.  | 1.16      | -0.576     |           |             |                |             |  |
| c= 0.94E+18 | 10000. | 1.32      | -0.420     |           |             |                |             |  |
|             | 20000. | 1.50      | -0.299     | 0.349*    | -0.265*     |                |             |  |
|             | 30000. | 1.56      | -0.195     | 0.368*    | -0.289*     |                |             |  |
|             | 80000. | 1.64      | -0.312E-01 | 0.421*    | -0.351*     | 0.355*         | -0.282*     |  |
| 4S - 8P     | 2500.  | 1.98      | -1.18      |           |             |                |             |  |
| 7373.3A     | 5000.  | 2.12      | -1.02      |           |             |                |             |  |
| c= 0.53E+18 | 10000. | 2.42      | -0.751     |           |             |                |             |  |
|             | 20000. | 2.71      | -0.517     |           |             |                |             |  |
|             | 30000. | 2.80      | -0.336     |           |             |                |             |  |
|             | 80000. | 2.88      | -0.523E-01 |           |             |                |             |  |
| 4S - 9P     | 2500.  | 3.45      | -1.81      |           |             |                |             |  |
| 7113.0A     | 5000.  | 3.70      | -1.64      |           |             |                |             |  |
| c= 0.33E+18 | 10000. | 4.22      | -1.23      |           |             |                |             |  |
|             | 20000. | 4.64      | -0.840     |           |             |                |             |  |
|             | 30000. | 4.77      | -0.548     |           |             |                |             |  |
|             | 80000. | 4.82      | -0.103     |           |             |                |             |  |
| 4S - 10P    | 2500.  | 5.68*     | -2.96*     |           |             |                |             |  |
| 6944.0A     | 5000.  | 6.09      | -2.48      |           |             |                |             |  |
| c= 0.22E+18 | 10000. | 6.95      | -1.88      |           |             |                |             |  |
|             | 20000. | 7.56      | -1.30      |           |             |                |             |  |
|             | 30000. | 7.72      | -0.894     |           |             |                |             |  |
|             | 80000. | 7.70      | -0.197     |           |             |                |             |  |
| 4P - 6S     | 2500.  | 0.890     | 0.568      | 0.175     | 0.139       | 0.144*         | 0.109*      |  |
| 16384.0A    | 5000.  | 1.03      | 0.663      | 0.195     | 0.165       | 0.160          | 0.131       |  |
| c= 0.25E+20 | 10000. | 1.14      | 0.686      | 0.218     | 0.191       | 0.179          | 0.153       |  |
|             | 20000. | 1.29      | 0.634      | 0.243     | 0.219       | 0.199          | 0.176       |  |
|             | 30000. | 1.42      | 0.543      | 0.260     | 0.236       | 0.212          | 0.190       |  |
|             | 80000. | 1.74      | 0.382      | 0.305     | 0.282       | 0.248          | 0.227       |  |
| 4P - 7S     | 2500.  | 1.17      | 0.773      | 0.227*    | 0.173*      | 0.185*         | 0.133*      |  |
| 12915.0A    | 5000.  | 1.33      | 0.922      | 0.255*    | 0.211*      | 0.207*         | 0.166*      |  |
| c= 0.88E+19 | 10000. | 1.51      | 0.868      | 0.286*    | 0.249*      | 0.232*         | 0.198*      |  |
|             | 20000. | 1.74      | 0.750      | 0.320     | 0.288       | 0.260*         | 0.231*      |  |
|             | 30000. | 1.95      | 0.628      | 0.343     | 0.312       | 0.278*         | 0.250*      |  |
|             | 80000. | 2.33      | 0.394      | 0.404     | 0.374       | 0.327          | 0.301       |  |
| 4P - 8S     | 2500.  | 1.78      | 1.15       |           |             |                |             |  |
| 11495.0A    | 5000.  | 2.03      | 1.29       | 0.385*    | 0.304*      |                |             |  |
| c= 0.44E+19 | 10000. | 2.35      | 1.28       | 0.432*    | 0.366*      |                |             |  |
|             | 20000. | 2.81      | 0.997      | 0.485*    | 0.429*      | 0.393*         | 0.342*      |  |
|             | 30000. | 3.15      | 0.823      | 0.519*    | 0.466*      | 0.421*         | 0.373*      |  |
|             | 80000. | 3.68      | 0.465      | 0.612     | 0.563       | 0.495*         | 0.453*      |  |

## TABLES FOR NA I LINES STARK BROADENING PARAMETERS

| NE= 0.1E+16 |        |           |           |           |           |                |           |
|-------------|--------|-----------|-----------|-----------|-----------|----------------|-----------|
| TRANSITION  | T(K)   | ELECTRONS |           | PROTONS   |           | IONIZED HELIUM |           |
|             |        | 2WE(A)    | DE(A)     | 2WI(A)    | DI(A)     | 2WI(A)         | DI(A)     |
| 4P - 9S     | 2500.  | 2.77      | 1.73      |           |           |                |           |
| 10745.0A    | 5000.  | 3.17      | 1.88      |           |           |                |           |
| c= 0.25E+19 | 10000. | 3.79      | 1.78      |           |           |                |           |
|             | 20000. | 4.64      | 1.35      | 0.747*    | 0.646*    |                |           |
|             | 30000. | 5.19      | 1.11      | 0.800*    | 0.707*    |                |           |
|             | 80000. | 5.94      | 0.572     | 0.943*    | 0.860*    | 0.763*         | 0.691*    |
| 4P - 4D     | 2500.  | 4.49      | 1.95      | 1.18*     | 0.847*    |                |           |
| 23370.0A    | 5000.  | 4.32      | 1.74      | 1.33*     | 1.06*     |                |           |
| c= 0.22E+19 | 10000. | 4.07      | 1.42      | 1.49*     | 1.27*     | 1.21*          | 1.00*     |
|             | 20000. | 3.80      | 1.04      | 1.70*     | 1.48*     | 1.35*          | 1.18*     |
|             | 30000. | 3.66      | 0.824     | 1.84*     | 1.60*     | 1.45*          | 1.28*     |
|             | 80000. | 3.29      | 0.432     | 2.21      | 1.99      | 1.74*          | 1.56*     |
| 4P - 5D     | 2500.  | 5.75      | 2.18      |           |           |                |           |
| 14776.0A    | 5000.  | 5.49      | 1.93      |           |           |                |           |
| c= 0.45E+18 | 10000. | 5.13      | 1.55      |           |           |                |           |
|             | 20000. | 4.72      | 1.13      |           |           |                |           |
|             | 30000. | 4.46      | 0.873     |           |           |                |           |
|             | 80000. | 3.80      | 0.408     |           |           |                |           |
| 4P - 6D     | 2500.  | 8.88      | 3.04      |           |           |                |           |
| 12318.0A    | 5000.  | 8.62      | 2.71      |           |           |                |           |
| c= 0.20E+18 | 10000. | 8.14      | 2.18      |           |           |                |           |
|             | 20000. | 7.52      | 1.44      |           |           |                |           |
|             | 30000. | 7.10      | 1.06      |           |           |                |           |
|             | 80000. | 5.99      | 0.414     |           |           |                |           |
| 5S - 5P     | 2500.  | 9.48      | -5.62     | 2.34      | -1.35     | 2.14*          | -1.06*    |
| 54318.3A    | 5000.  | 10.6      | -6.04     | 2.48      | -1.59     | 2.25*          | -1.27*    |
| c= 0.15E+21 | 10000. | 12.0      | -5.71     | 2.65      | -1.84     | 2.37           | -1.47     |
|             | 20000. | 13.9      | -4.63     | 2.84      | -2.10     | 2.51           | -1.69     |
|             | 30000. | 15.2      | -3.88     | 2.97      | -2.27     | 2.61           | -1.83     |
|             | 80000. | 17.6      | -2.55     | 3.34      | -2.71     | 2.88           | -2.19     |
| 5S - 6P     | 2500.  | 4.70      | -2.96     | 1.20*     | -0.672*   |                |           |
| 24414.1A    | 5000.  | 5.15      | -2.90     | 1.29*     | -0.823*   |                |           |
| c= 0.15E+20 | 10000. | 5.84      | -2.23     | 1.38*     | -0.973*   | 1.22*          | -0.772*   |
|             | 20000. | 6.80      | -1.62     | 1.50*     | -1.13*    | 1.31*          | -0.901*   |
|             | 30000. | 7.25      | -1.28     | 1.57      | -1.22     | 1.36*          | -0.979*   |
|             | 80000. | 7.96      | -0.560    | 1.78      | -1.46     | 1.52           | -1.18     |
| 5S - 7P     | 2500.  | 6.28      | -3.85     |           |           |                |           |
| 18726.6A    | 5000.  | 6.81      | -3.42     |           |           |                |           |
| c= 0.54E+19 | 10000. | 7.75      | -2.26     |           |           |                |           |
|             | 20000. | 8.87      | -1.58     | 2.02*     | -1.54*    |                |           |
|             | 30000. | 9.29      | -1.02     | 2.13*     | -1.68*    |                |           |
|             | 80000. | 9.86      | -0.329    | 2.44*     | -2.04*    | 2.05*          | -1.64*    |
| 5S - 8P     | 2500.  | 9.87      | -5.87     |           |           |                |           |
| 16398.8A    | 5000.  | 10.6      | -5.06     |           |           |                |           |
| c= 0.26E+19 | 10000. | 12.1      | -3.45     |           |           |                |           |
|             | 20000. | 13.6      | -2.17     |           |           |                |           |
|             | 30000. | 14.1      | -1.02     |           |           |                |           |
|             | 80000. | 14.6      | -0.369    |           |           |                |           |
| NE= 0.1E+17 |        |           |           |           |           |                |           |
| 3S - 3P     | 2500.  | 0.191E-01 | 0.130E-01 | 0.126E-01 | 0.352E-02 | 0.124E-01      | 0.282E-02 |
| 5891.8A     | 5000.  | 0.211E-01 | 0.154E-01 | 0.127E-01 | 0.404E-02 | 0.126E-01      | 0.325E-02 |
| c= 0.30E+20 | 10000. | 0.249E-01 | 0.177E-01 | 0.129E-01 | 0.459E-02 | 0.127E-01      | 0.370E-02 |
|             | 20000. | 0.322E-01 | 0.181E-01 | 0.130E-01 | 0.521E-02 | 0.128E-01      | 0.420E-02 |
|             | 30000. | 0.381E-01 | 0.183E-01 | 0.132E-01 | 0.559E-02 | 0.128E-01      | 0.452E-02 |
|             | 80000. | 0.551E-01 | 0.129E-01 | 0.136E-01 | 0.660E-02 | 0.131E-01      | 0.534E-02 |

| NE= 0.1E+17 |        | ELECTRONS |            | PROTONS    |             | IONIZED HELIUM |             |
|-------------|--------|-----------|------------|------------|-------------|----------------|-------------|
| TRANSITION  | T(K)   | 2WE(A)    | DE(A)      | 2WI(A)     | DI(A)       | 2WI(A)         | DI(A)       |
| 3S - 4P     | 2500.  | 0.649E-01 | -0.231E-01 | 0.219E-01* | -0.686E-02* | 0.211E-01*     | -0.535E-02* |
| 3302.6A     | 5000.  | 0.725E-01 | -0.141E-01 | 0.225E-01  | -0.818E-02  | 0.219E-01*     | -0.647E-02* |
| c= 0.12E+19 | 10000. | 0.864E-01 | -0.422E-02 | 0.230E-01  | -0.951E-02  | 0.223E-01*     | -0.760E-02* |
|             | 20000. | 0.100     | 0.248E-02  | 0.235E-01  | -0.109E-01  | 0.227E-01      | -0.877E-02  |
|             | 30000. | 0.108     | 0.582E-02  | 0.239E-01  | -0.118E-01  | 0.229E-01      | -0.948E-02  |
|             | 80000. | 0.126     | 0.635E-02  | 0.251E-01  | -0.141E-01  | 0.237E-01      | -0.114E-01  |
| 3S - 5P     | 2500.  | 0.202     | -0.102     |            |             |                |             |
| 2852.8A     | 5000.  | 0.221     | -0.928E-01 | 0.611E-01* | -0.303E-01* |                |             |
| c= 0.40E+18 | 10000. | 0.254     | -0.631E-01 | 0.651E-01* | -0.375E-01* |                |             |
|             | 20000. | 0.295     | -0.460E-01 | 0.693E-01* | -0.445E-01* | 0.626E-01*     | -0.353E-01* |
|             | 30000. | 0.313     | -0.340E-01 | 0.720E-01* | -0.487E-01* | 0.646E-01*     | -0.388E-01* |
|             | 80000. | 0.347     | -0.114E-01 | 0.798E-01  | -0.590E-01  | 0.702E-01*     | -0.476E-01* |
| 3S - 6P     | 2500.  | 0.527     | -0.283     |            |             |                |             |
| 2680.4A     | 5000.  | 0.573     | -0.257     |            |             |                |             |
| c= 0.19E+18 | 10000. | 0.653     | -0.186     |            |             |                |             |
|             | 20000. | 0.749     | -0.143     |            |             |                |             |
|             | 30000. | 0.785     | -0.108     |            |             |                |             |
|             | 80000. | 0.842     | -0.356E-01 | 0.208*     | -0.162*     |                |             |
| 3P - 4S     | 2500.  | 0.367     | 0.258      | 0.855E-01  | 0.623E-01   | 0.733E-01      | 0.488E-01   |
| 11397.0A    | 5000.  | 0.420     | 0.296      | 0.937E-01  | 0.735E-01   | 0.797E-01      | 0.584E-01   |
| c= 0.59E+20 | 10000. | 0.466     | 0.355      | 0.103      | 0.851E-01   | 0.870E-01      | 0.681E-01   |
|             | 20000. | 0.515     | 0.333      | 0.114      | 0.974E-01   | 0.953E-01      | 0.783E-01   |
|             | 30000. | 0.552     | 0.329      | 0.121      | 0.105       | 0.101          | 0.846E-01   |
|             | 80000. | 0.702     | 0.228      | 0.140      | 0.125       | 0.116          | 0.101       |
| 3P - 5S     | 2500.  | 0.405     | 0.276      | 0.865E-01* | 0.615E-01*  | 0.702E-01*     | 0.461E-01*  |
| 6158.6A     | 5000.  | 0.468     | 0.339      | 0.970E-01  | 0.773E-01   | 0.789E-01*     | 0.600E-01*  |
| c= 0.70E+19 | 10000. | 0.508     | 0.376      | 0.109      | 0.925E-01   | 0.884E-01*     | 0.731E-01*  |
|             | 20000. | 0.563     | 0.363      | 0.122      | 0.108       | 0.991E-01      | 0.862E-01   |
|             | 30000. | 0.589     | 0.339      | 0.130      | 0.117       | 0.106          | 0.940E-01   |
|             | 80000. | 0.732     | 0.254      | 0.154      | 0.141       | 0.125          | 0.114       |
| 3P - 6S     | 2500.  | 0.780     | 0.519      |            |             |                |             |
| 5151.9A     | 5000.  | 0.891     | 0.611      | 0.181*     | 0.129*      |                |             |
| c= 0.25E+19 | 10000. | 0.974     | 0.654      | 0.204*     | 0.162*      |                |             |
|             | 20000. | 1.10      | 0.634      | 0.229*     | 0.195*      | 0.186*         | 0.154*      |
|             | 30000. | 1.19      | 0.542      | 0.245*     | 0.214*      | 0.198*         | 0.170*      |
|             | 80000. | 1.46      | 0.374      | 0.289*     | 0.262*      | 0.234*         | 0.210*      |
| 3P - 7S     | 2500.  | 1.52      | 0.920      |            |             |                |             |
| 4750.6A     | 5000.  | 1.73      | 1.12       |            |             |                |             |
| c= 0.12E+19 | 10000. | 1.90      | 1.12       |            |             |                |             |
|             | 20000. | 2.19      | 0.986      |            |             |                |             |
|             | 30000. | 2.45      | 0.832      |            |             |                |             |
|             | 80000. | 2.93      | 0.528      | 0.539*     | 0.480*      |                |             |
| 3P - 3D     | 2500.  | 0.312     | 0.219      | 0.809E-01  | 0.521E-01   | 0.711E-01*     | 0.404E-01*  |
| 8191.1A     | 5000.  | 0.355     | 0.241      | 0.877E-01  | 0.626E-01   | 0.765E-01      | 0.494E-01   |
| c= 0.74E+19 | 10000. | 0.385     | 0.244      | 0.954E-01  | 0.732E-01   | 0.824E-01      | 0.584E-01   |
|             | 20000. | 0.413     | 0.227      | 0.104      | 0.843E-01   | 0.891E-01      | 0.676E-01   |
|             | 30000. | 0.428     | 0.200      | 0.110      | 0.910E-01   | 0.936E-01      | 0.732E-01   |
|             | 80000. | 0.474     | 0.136      | 0.126      | 0.109       | 0.106          | 0.879E-01   |
| 3P - 4D     | 2500.  | 2.25      | 0.809      |            |             |                |             |
| 5686.4A     | 5000.  | 2.22      | 0.772      |            |             |                |             |
| c= 0.13E+18 | 10000. | 2.11      | 0.669      |            |             |                |             |
|             | 20000. | 1.97      | 0.550      |            |             |                |             |
|             | 30000. | 1.88      | 0.450      |            |             |                |             |
|             | 80000. | 1.65      | 0.254      |            |             |                |             |

TABLES FOR NA I LINES STARK BROADENING PARAMETERS

NE= 0.1E+17

| TRANSITION  | T(K)   | ELECTRONS |            | PROTONS |             | IONIZED HELIUM |             |
|-------------|--------|-----------|------------|---------|-------------|----------------|-------------|
|             |        | 2WE(A)    | DE(A)      | 2WI(A)  | DI(A)       | 2WI(A)         | DI(A)       |
| 3P - 5D     | 2500.  | 4.62      | 1.43       |         |             |                |             |
| 4981.4A     | 5000.  | 4.86      | 1.45       |         |             |                |             |
| c= 0.52E+17 | 10000. | 4.81      | 1.24       |         |             |                |             |
|             | 20000. | 4.59      | 0.993      |         |             |                |             |
|             | 30000. | 4.40      | 0.808      |         |             |                |             |
|             | 80000. | 3.82      | 0.426      |         |             |                |             |
| 3D - 5P     | 2500.  | 7.85      | -4.29      |         |             |                |             |
| 17038.7A    | 5000.  | 8.74      | -4.29      | 2.14*   | -1.14*      |                |             |
| c= 0.14E+20 | 10000. | 9.86      | -3.25      | 2.31*   | -1.42*      |                |             |
|             | 20000. | 11.5      | -2.58      | 2.48*   | -1.69*      | 2.20*          | -1.34*      |
|             | 30000. | 12.3      | -2.26      | 2.59*   | -1.85*      | 2.28*          | -1.47*      |
|             | 80000. | 13.6      | -1.04      | 2.90    | -2.26       | 2.51*          | -1.81*      |
| 3D - 6P     | 2500.  | 11.4      | -5.81      |         |             |                |             |
| 12309.2A    | 5000.  | 12.5      | -5.67      |         |             |                |             |
| c= 0.39E+19 | 10000. | 14.2      | -4.25      |         |             |                |             |
|             | 20000. | 16.3      | -3.01      |         |             |                |             |
|             | 30000. | 17.1      | -2.25      |         |             |                |             |
|             | 80000. | 18.4      | -0.564     | 4.39*   | -3.46*      |                |             |
| 4S - 4P     | 2500.  | 3.56      | -1.81      | 1.03*   | -0.421*     | 0.974*         | -0.325*     |
| 22070.0A    | 5000.  | 3.86      | -1.84      | 1.07    | -0.508      | 1.02*          | -0.400*     |
| c= 0.53E+20 | 10000. | 4.40      | -1.62      | 1.12    | -0.595      | 1.05*          | -0.474*     |
|             | 20000. | 5.29      | -1.23      | 1.16    | -0.686      | 1.09           | -0.550      |
|             | 30000. | 5.89      | -1.05      | 1.20    | -0.742      | 1.11           | -0.596      |
|             | 80000. | 7.23      | -0.658     | 1.30    | -0.888      | 1.18           | -0.716      |
| 4S - 5P     | 2500.  | 2.98      | -1.55      |         |             |                |             |
| 10747.0A    | 5000.  | 3.25      | -1.52      |         |             |                |             |
| c= 0.57E+19 | 10000. | 3.72      | -1.21      | 0.938*  | -0.548*     |                |             |
|             | 20000. | 4.38      | -1.02      | 1.00*   | -0.651*     | 0.901*         | -0.516*     |
|             | 30000. | 4.70      | -0.797     | 1.04*   | -0.713*     | 0.931*         | -0.568*     |
|             | 80000. | 5.31      | -0.387     | 1.16    | -0.868      | 1.01*          | -0.697*     |
| 4S - 6P     | 2500.  | 5.55      | -2.97      |         |             |                |             |
| 8650.3A     | 5000.  | 6.04      | -2.74      |         |             |                |             |
| c= 0.19E+19 | 10000. | 6.87      | -2.00      |         |             |                |             |
|             | 20000. | 7.92      | -1.49      |         |             |                |             |
|             | 30000. | 8.34      | -1.15      |         |             |                |             |
|             | 80000. | 9.02      | -0.292     | 2.17*   | -1.70*      |                |             |
| NE= 0.1E+18 |        |           |            |         |             |                |             |
| 3S - 3F     | 2500.  | 0.191     | 0.126      | 0.121   | 0.308E-01   | 0.116*         | 0.238E-01*  |
| 5891.8A     | 5000.  | 0.211     | 0.150      | 0.126   | 0.373E-01   | 0.123*         | 0.294E-01*  |
| c= 0.30E+20 | 10000. | 0.249     | 0.176      | 0.128   | 0.437E-01   | 0.125          | 0.348E-01   |
|             | 20000. | 0.322     | 0.160      | 0.130   | 0.504E-01   | 0.127          | 0.404E-01   |
|             | 30000. | 0.381     | 0.182      | 0.132   | 0.545E-01   | 0.128          | 0.438E-01   |
|             | 80000. | 0.551     | 0.129      | 0.136   | 0.653E-01   | 0.131          | 0.527E-01   |
| 3S - 4P     | 2500.  | 0.648     | -0.206     |         |             |                |             |
| 3302.6A     | 5000.  | 0.724     | -0.124     |         |             |                |             |
| c= 0.12E+19 | 10000. | 0.863     | -0.359E-01 | 0.224*  | -0.828E-01* |                |             |
|             | 20000. | 1.00      | 0.293E-01  | 0.233*  | -0.100*     |                |             |
|             | 30000. | 1.08      | 0.591E-01  | 0.238*  | -0.111*     | 0.227*         | -0.877E-01* |
|             | 80000. | 1.26      | 0.641E-01  | 0.251*  | -0.136*     | 0.236*         | -0.109*     |
| 3S - 5P     | 2500.  | 1.98      | -0.749     |         |             |                |             |
| 2852.8A     | 5000.  | 2.19      | -0.734     |         |             |                |             |
| c= 0.40E+18 | 10000. | 2.53      | -0.494     |         |             |                |             |
|             | 20000. | 2.95      | -0.378     |         |             |                |             |
|             | 30000. | 3.12      | -0.281     |         |             |                |             |
|             | 80000. | 3.47      | -0.108     |         |             |                |             |



| NE= 0.1E+18 |        | ELECTRONS |        | PROTONS |        | IONIZED HELIUM |        |
|-------------|--------|-----------|--------|---------|--------|----------------|--------|
| TRANSITION  | T(K)   | 2WE(A)    | DE(A)  | 2WI(A)  | DI(A)  | 2WI(A)         | DI(A)  |
| 3S - 6P     | 2500.  | 4.39*     | -1.41* |         |        |                |        |
| 2620.4A     | 5000.  | 5.24*     | -1.55* |         |        |                |        |
| c= 0.19E+18 | 10000. | 6.21      | -1.14  |         |        |                |        |
|             | 20000. | 7.28      | -0.921 |         |        |                |        |
|             | 30000. | 7.68      | -0.748 |         |        |                |        |
|             | 80000. | 8.32      | -0.326 |         |        |                |        |
| 3P - 4S     | 2500.  | 3.67      | 2.37   | 0.831*  | 0.434* | 0.689*         | 0.300* |
| 11397.0A    | 5000.  | 4.20      | 2.83   | 0.930*  | 0.602* | 0.784*         | 0.451* |
| c= 0.59E+20 | 10000. | 4.66      | 3.45   | 1.03*   | 0.757* | 0.865*         | 0.587* |
|             | 20000. | 5.15      | 3.28   | 1.14    | 0.907  | 0.952*         | 0.716* |
|             | 30000. | 5.52      | 3.26   | 1.21    | 0.995  | 1.01*          | 0.791* |
|             | 80000. | 7.02      | 2.27   | 1.40    | 1.22   | 1.16           | 0.977  |
| 3P - 5S     | 2500.  | 4.04      | 2.33   |         |        |                |        |
| 6158.6A     | 5000.  | 4.68      | 3.09   |         |        |                |        |
| c= 0.70E+19 | 10000. | 5.08      | 3.55   |         |        |                |        |
|             | 20000. | 5.63      | 3.50   | 1.22*   | 0.929* |                |        |
|             | 30000. | 5.89      | 3.32   | 1.30*   | 1.05*  |                |        |
|             | 80000. | 7.32      | 2.54   | 1.53*   | 1.34*  | 1.24*          | 1.06*  |
| 3P - 6S     | 2500.  | 7.76*     | 3.84*  |         |        |                |        |
| 5151.9A     | 5000.  | 8.90      | 5.15   |         |        |                |        |
| c= 0.25E+19 | 10000. | 9.74      | 5.87   |         |        |                |        |
|             | 20000. | 11.0      | 5.92   |         |        |                |        |
|             | 30000. | 11.9      | 5.12   |         |        |                |        |
|             | 80000. | 14.6      | 3.71   |         |        |                |        |
| 3P - 3D     | 2500.  | 3.12      | 1.97   | 0.749*  | 0.308* |                |        |
| 8191.1A     | 5000.  | 3.55      | 2.26   | 0.859*  | 0.475* |                |        |
| c= 0.74E+19 | 10000. | 3.85      | 2.34   | 0.948*  | 0.625* | 0.812*         | 0.477* |
|             | 20000. | 4.13      | 2.20   | 1.04*   | 0.767* | 0.887*         | 0.600* |
|             | 30000. | 4.28      | 1.97   | 1.10*   | 0.848* | 0.934*         | 0.670* |
|             | 80000. | 4.74      | 1.36   | 1.26    | 1.05   | 1.06*          | 0.841* |
| 3P - 4D     | 2500.  | 12.8      | 4.00   |         |        |                |        |
| 5686.4A     | 5000.  | 15.3      | 4.81   |         |        |                |        |
| c= 0.13E+18 | 10000. | 16.3      | 4.63   |         |        |                |        |
|             | 20000. | 16.3      | 4.08   |         |        |                |        |
|             | 30000. | 16.0      | 3.50   |         |        |                |        |
|             | 80000. | 14.8      | 2.32   |         |        |                |        |
| NE= 0.1E+19 |        |           |        |         |        |                |        |
| 3S - 3P     | 2500.  | 1.90      | 1.12   | 0.796*  | 0.170* |                |        |
| 5891.3A     | 5000.  | 2.11      | 1.41   | 1.09*   | 0.275* |                |        |
| c= 0.30E+20 | 10000. | 2.49      | 1.70   | 1.22*   | 0.368* |                |        |
|             | 20000. | 3.22      | 1.78   | 1.28*   | 0.455* | 1.23*          | 0.355* |
|             | 30000. | 3.81      | 1.82   | 1.31*   | 0.505* | 1.26*          | 0.398* |
|             | 80000. | 5.51      | 1.29   | 1.36    | 0.628  | 1.30*          | 0.502* |
| 3S - 4P     | 2500.  | 5.62      | -1.15  |         |        |                |        |
| 3302.6A     | 5000.  | 6.89      | -0.586 |         |        |                |        |
| c= 0.12E+19 | 10000. | 8.45      | 0.146  |         |        |                |        |
|             | 20000. | 9.91      | 0.593  |         |        |                |        |
|             | 30000. | 10.7      | 0.739  |         |        |                |        |
|             | 80000. | 12.5      | 0.659  |         |        |                |        |

## ACKNOWLEDGEMENTS

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## ТАБЛИЦЕ ЗА ПАРАМЕТРЕ ШТАРКОВОГ ШИРЕЊА ЛИНИЈА NaI

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УДК 52-355,3

Претходно саопштење

У оквиру семикласичне теорије израчунате су ширине и помаци услед судара са електронима, протонима и јонизованим хелијумом за спектралне линије у

оквиру 61 мултиплета неутралног натријума. Резултати су дати у функцији електронске температуре и густине.

BEHAVIOUR OF LEVELS IN THE CONDITIONS OF  
ASYMMETRICAL HEATING

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**SUMMARY:** The subject of the paper is the earlier and present importance of second level examinations. The data of a general analysis are presented. They indicate not only some problems of second levels, but also give informations on level triers whose properties are weakly known at present.

For levels it is very important that the temperature difference at some parts of the tube is not large. According to Drodofski (Drodofski, 1956) in the case of a tube 150 mm long a temperature difference greater than 0.009 °C already causes a measurable effect in the position of the bubble. It is difficult to satisfy this requirement. Sardy (Sardy, 1965) measured temperature differences, equal to 0.25 °C on the average, on the outer sides of levels in the field conditions and for the levels examined by him a change of 2" in the geographic latitude determined by use of Talcot's method due to a temperature difference of 1 °C at the level ends was found. Drodofski's datum concerns the hydrostatic influences only, whereas Sardy's effect corresponds to a sum of influences both of hydrostatic and mechanical character. The thermomechanical influence is a function of properties of the level-tube housing. The housing can produce a change in the tube's curvature already at a uniform temperature distribution. In the case of a nonuniform temperature distribution its influence is significantly larger and more complicated (Tarczy-Hornoch, A., 1964).

The hydrostatic effects may have a more general character, whereas the mechanical influences are practically different for different levels. This means that one should carefully examine the level behaviour within an inhomogeneous temperature field. This behaviour is

usually not taken into account because it is thought that the tube is well isolated from outer influences, but unfortunately this statement is not true.

a) At the geodetico-geophysical Institute in Sopron, in 1964, two levels (in further text level A and level B) were examined with a photo-automatical trier. One level was put on a trier (Tarczy-Hornoch, 1959) and then its ends were heated by lamps. Between the lamps and the levels was a glass wall 10 mm thick. A lamp was at the distance of 1 m from the level's body (position I), i. e. shifted by 40° with respect to position I (position II). The heating was carried out with an infrared lamp (power 250 W), or with a normal lamp (power 300 W). The beam was directed to the part of the level's end containing the correction screws ( $\leftrightarrow$ ), i. e. to the opposite end ( $\leftarrow \rightarrow$ ). The level was read every minute. The cooling interval between two successive groups of measurements was 4 minutes. When the position of the bubble's middle was determined (expressed in parts of the level constant), a significant difference in heating, between the two kinds of lamps, as well as a prominent influence caused by the heating of the level's ends containing the correction screws, were established. Practically, there was no difference in the effects for positions I and II. After the heating was finished the bubble would come back to its rest position along a logarithmic spiral trajectory. Since the major part of the normal

lamp effects was absorbed by the glass, the shifting of the bubble was in this case about three times smaller.

On the basis of these examinations one can conclude that it is desirable to put a level within a protective shell in such a way that the correction screws should be covered and a glass slab situated in front of the level in order to protect it from the direct influence of observer who radiates like a normal lamp whose power is 100 W (Teleki, 1965).

b) Level A was heated along its length with electric heaters. The heaters (each one having 0.5 kW power) were at the distance of 170 cm from level B. A 0.5 kW heater changed the position of the bubble's middle by a very small amount (0.2 level constants) and the bubble came back to its rest position within 5 minutes. A heater of 1 kW shifted the bubble by 1 level constant and to come back to the rest position the bubble needed 25 minutes.

Level A was permanently under heating and the change in the bubble's position was observed from the moment of turning the heating source off. The time interval necessary to the middle of the bubble to come back to its original position was one hour. Later on, during the cooling process, the level ends were two times, the first time for 5 minutes, the second time for 10 minutes, heated with infralamps. This caused an uncertainty in the bubble's position and a long time interval was necessary for the bubble to come back in the state of equilibrium.

The levels A and B were heated under the conditions mentioned above with electric heaters of 1 kW power. After the bubble had reached its rest position, the positions of the levels were changed by 180°. The position of the bubble of level A had a change of 1.8 level constants after rotation and to reach the state of rest it needed 24 minutes. In the case of level B the rest state of its bubble was already reached after 16 minutes and the change in the bubble's middle position was 1.8 level constants.

The results of these measurements also indicate the different character of the levels on the one side and the necessity of level protection on the other side; in the case of existence of temperature gradients the position of the bubble had significant and long-lasting changes. This fact is especially important for those observations where instruments are rotated and there is no time enough to wait for the bubble to reach its rest state again.

c) The determinations of the constants for level A and level B in the presence of a temperature gradient were performed on a classical level trier of the type „Bamberg” No 5023 which belongs to the Geodetical Institute of Faculty of Civil Engineering of Belgrade University. The levels were heated along their lengths from the distance of 170 cm with an electric heater whose power was 1 kW. The trier was covered so that it suffered no direct radiation. The bubble length for both levels was 25 level constants and the mean external

temperature was + 18 C. Wanach's method was used. The examinations began only after the bubble had reached its state of rest.

The levels were examined by two observers in two positions (of the levels). In the first position (I) the screws were opposite the heater and in the second one (II) they were closer to the heater.

Table 1

| level | I       |       |       | II      |       |       |
|-------|---------|-------|-------|---------|-------|-------|
|       | N       | M     | F     | N       | M     | F     |
| A     | 1.12136 | 0.050 | 0.056 | 1.12123 | 0.060 | 0.067 |
|       | 1.12276 | 0.065 | 0.073 | 1.11410 | 0.060 | 0.068 |
| B     | 0.80636 | 0.057 | 0.046 | 0.81505 | 0.096 | 0.079 |
|       | 0.80949 | 0.116 | 0.096 | 0.81160 | 0.109 | 0.087 |

It is seen from Table 1 that there is a systematic difference in the level constant value depending on the rectification screw position. For level A from the mean values of the data concerning both observers one obtains a difference of 0.00438; for level B the difference is -0.01040.

All our examinations concerning the asymmetrical level heating point out that the problem is serious. Since it is very difficult, or perhaps impossible, to satisfy completely Drodofski's condition concerning the temperature difference at the tube's ends (Drodofski, 1956), a better level isolation becomes necessary. If we carry out the isolation, and especially if we do not, it is necessary for any level to know also the characteristics in the case that the level is within a variable temperature field. The results of these examinations indicate that the level constant at almost the same mean temperature has different values. According to Drodofski as level characteristics in addition to the constant one should also assume the durations of oscillations and damping and the highest possible accuracy of measurements with a given level. These data in Drodofski's opinion sufficiently characterise a level in the course of its using.

It is true that our instruments, including the levels as well, are seldom within a homogeneous temperature field. Knowing this and also that mentioned above one concludes that Drodofski's characteristics give no real picture of a level. Drodofski's opinion should be, certainly, taken into account, however the data proposed by him neither characterise a level sufficiently, nor give a real picture of it and therefore as a level characteristic one should assume the datum concerning its behaviour within an inhomogeneous temperature field. In astrometrical and astrogeodetical praxis these data are necessary, whereas the data concerning the durations of oscillations and damping are of no practical importance because there is time enough for the bubble to reach its rest state.

On the basis of the results obtained from the examinations of levels A and B and of other ones (Sadzakov, 1989) one can point out the following.

i) Any level is a problem for itself requiring thus a special examination.

ii) Levels are not sufficiently isolated from temperature influences. The correction screws are the main source of trouble. For this reason it is necessary to put a level within a protective shell and to separate it from the observer with a glass slab.

iii) For every level one should specify the datum describing its behaviour within an inhomogeneous temperature field. This characteristic is necessary to any astrometric and astrogeodetic measurement.

iv) Levels should be thoroughly examined at all temperatures at which they are used. A special attention should be paid to the level behaviour at low temperatures.

v) One should verify the constant of the disc belonging to the trier serving for the purpose of level examining. The trier should be well isolated from external effects.

All the examinations and analyses indicate that the levels are very large sources of errors of different kinds. For this reason levels should be examined in detail, comprehensively and with a special care, so that a prior knowledge of them is required.

### ПОНАШАЊЕ ЛИБЕЛА ПРИ АСИМЕТРИЧНОМ ГРЕЈАЊУ

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УДК 528.541

*Претходно саопштење*

Говори се о значају испитивања секундних либела пре и сада. Дати су подаци анализе општег карактера, који указују не само на неке проблеме секундних

либела, него дају информацију и о испитивању либела, чије су особине за сада мало познате.

## VALUES OF BELGRADE LATITUDE OBTAINED IN THE PERIOD 1969.0–1975.0

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**SUMMARY:** The values of Belgrade latitude obtained in the period 1969.0–1975.0 are presented here.

The latitude values presented here (Table 1) are subject of the analysis of the variations in the latitude of Belgrade given in the paper by Grujić, Djokić and Jovanović (1989). The observations comprehend a period within which the conditions of deriving the latitude values were the most favourable with regard to the programme characteristics and the number of observations. For this reason the mentioned period has been chosen for the purpose of examining the fine change of the Belgrade latitude and the other nonpolar changes (Z term). The six-year period has been taken in order to obtain the value of the Belgrade mean latitude and

its change by applying Orlov's formula which eliminates the Chandlerian annual and semi-annual periods. The latitudes are reduced to the FK4 system. No explanations of the designations appearing in the title are given because they are usual.

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## ВРЕДНОСТИ ШИРИНА БЕОГРАДА ДОБИЈЕНИХ ИЗ ПОСМАТРАЧКОГ ПЕРИОДА 1969.0–1975.0

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УДК 521.936/938  
Претходно саопштење

Дате су вредности ширина коришћене код анализе промена ширине Београда у раду Грујић, Ђокић и Јовановић /1989/.



## Prilog I

|      |    | Date | Julian<br>days | Observer | Group | Subgroup<br>$\varphi_a$ $\varphi_b$ |        |
|------|----|------|----------------|----------|-------|-------------------------------------|--------|
| 1969 |    |      | 2440000+       |          |       |                                     |        |
| I    | 7  |      | 229.250        | MD       | I     | -                                   | 10.194 |
|      | 7  |      | 229.395        | MD       | II    | 10.176                              | 10.316 |
|      | 10 |      | 232.220        | MD       | I     | 10.008                              | 10.290 |
|      | 10 |      | 232.385        | MD       | II    | 10.411                              | 10.493 |
|      | 14 |      | 236.350        | RG       | II    | 10.411                              | -      |
|      | 21 |      | 243.355        | RG       | II    | 10.250                              | 10.390 |
|      | 22 |      | 244.355        | MD       | II    | 10.241                              | 10.279 |
|      | 27 |      | 249.360        | MD       | II    | -                                   | 10.177 |
|      | 27 |      | 249.480        | MD       | III   | 10.283                              | -      |
|      | 31 |      | 253.325        | MD       | II    | 10.018                              | 10.214 |
| II   | 8  |      | 261.305        | RG       | II    | 10.155                              | 10.234 |
|      | 14 |      | 267.285        | MD       | II    | 10.310                              | 10.324 |
|      | 15 |      | 268.310        | RG       | II    | -                                   | 10.313 |
|      | 18 |      | 271.300        | RG       | II    | -                                   | 10.191 |
| III  | 18 |      | 271.420        | RG       | III   | 10.312                              | -      |
|      | 9  |      | 290.250        | RG       | II    | -                                   | 10.370 |
|      | 9  |      | 290.395        | RG       | III   | 10.368                              | 10.160 |
|      | 9  |      | 290.565        | RG       | IV    | 10.290                              | 10.302 |
| IV   | 22 |      | 303.355        | RG       | III   | 10.470                              | 10.151 |
|      | 5  |      | 317.325        | RG       | III   | 10.474                              | 10.242 |
|      | 5  |      | 317.490        | MD       | IV    | 10.315                              | 10.259 |
|      | 7  |      | 319.340        | MD       | III   | -                                   | 10.308 |
|      | 8  |      | 320.315        | RG       | III   | 10.518                              | 10.274 |
|      | 9  |      | 321.310        | MD       | III   | 10.590                              | 10.238 |
|      | 10 |      | 322.315        | RG       | III   | 10.558                              | 10.293 |
|      | 10 |      | 322.450        | RG       | IV    | 10.182                              | -      |
|      | 11 |      | 323.315        | MD       | III   | 10.674                              | 10.570 |
|      | 11 |      | 323.450        | MD       | IV    | 10.272                              | -      |
| V    | 12 |      | 324.305        | RG       | III   | 10.482                              | 10.303 |
|      | 12 |      | 324.450        | RG       | IV    | 10.236                              | -      |
|      | 25 |      | 337.435        | MD       | IV    | 10.268                              | 10.311 |
|      | 26 |      | 338.435        | RG       | IV    | 10.305                              | 10.262 |
|      | 27 |      | 339.400        | RG       | IV    | 10.274                              | -      |
|      | 28 |      | 340.425        | MD       | IV    | 10.345                              | 10.295 |
|      | 29 |      | 341.590        | RG       | V     | 10.304                              | 10.247 |
|      | 3  |      | 345.390        | RG       | IV    | 10.321                              | -      |
|      | 12 |      | 354.385        | MD       | IV    | 10.355                              | 10.419 |
|      | 14 |      | 356.385        | MD       | IV    | 10.317                              | 10.409 |
| VI   | 15 |      | 357.385        | RG       | IV    | 10.509                              | 10.543 |
|      | 15 |      | 357.545        | VM       | V     | 10.588                              | 10.519 |
|      | 16 |      | 358.375        | MD       | IV    | 10.443                              | 10.216 |
|      | 16 |      | 358.545        | VM       | V     | 10.456                              | 10.467 |
|      | 22 |      | 364.360        | RG       | IV    | 10.316                              | 10.411 |
|      | 22 |      | 364.525        | RG       | V     | 10.283                              | 10.398 |
|      | 23 |      | 365.380        | MD       | IV    | -                                   | 10.556 |
|      | 24 |      | 366.355        | RG       | IV    | 10.401                              | 10.341 |
|      | 24 |      | 366.520        | VM       | V     | 10.519                              | 10.474 |
|      | 29 |      | 371.480        | RG       | V     | 10.479                              | -      |
| VI   | 5  |      | 378.350        | RG       | IV    | -                                   | 10.369 |
|      | 10 |      | 383.475        | RG       | V     | 10.380                              | 10.316 |
|      | 12 |      | 385.330        | RG       | IV    | -                                   | 10.462 |
|      | 12 |      | 385.470        | RG       | V     | 10.448                              | 10.447 |
|      | 18 |      | 389.460        | MD       | V     | 10.496                              | 10.537 |
|      | 18 |      | 391.455        | MD       | V     | 10.461                              | 10.301 |
|      | 23 |      | 396.440        | RG       | V     | 10.353                              | 10.377 |
|      | 28 |      | 401.425        | RG       | V     | 10.375                              | 10.471 |

VALUES OF BELGRADE LATITUDE OBTAINED IN THE PERIOD 1969.0-1975.0

|      |    |         |    |    |        |        |
|------|----|---------|----|----|--------|--------|
| VII  | 2  | 405.515 | VM | V  | 10.551 | 10.461 |
|      | 2  | 405.560 | VM | VI | 10.421 | -      |
|      | 3  | 406.415 | RG | V  | 10.357 | 10.359 |
|      | 3  | 406.550 | RG | VI | 10.491 | -      |
|      | 4  | 407.410 | VM | V  | 10.538 | 10.448 |
|      | 4  | 407.550 | VM | VI | 10.560 | -      |
|      | 5  | 408.405 | RG | V  | 10.509 | 10.487 |
|      | 7  | 410.400 | VM | V  | 10.458 | 10.474 |
|      | 7  | 410.550 | VM | VI | 10.361 | -      |
|      | 15 | 418.380 | RG | V  | 10.515 | 10.488 |
|      | 15 | 418.545 | RG | VI | 10.535 | 10.595 |
|      | 16 | 419.380 | VM | V  | 10.558 | 10.494 |
|      | 16 | 419.545 | VM | VI | 10.499 | 10.491 |
|      | 17 | 420.375 | RG | V  | 10.458 | 10.518 |
|      | 17 | 420.535 | RG | VI | 10.347 | 10.378 |
|      | 20 | 423.390 | RG | V  | -      | 10.529 |
|      | 22 | 425.340 | RG | V  | 10.534 | -      |
|      | 23 | 426.340 | VM | V  | 10.551 | -      |
|      | 23 | 426.525 | VM | VI | 10.571 | 10.320 |
|      | 24 | 427.355 | RG | V  | 10.497 | 10.619 |
|      | 24 | 427.520 | RG | VI | 10.461 | 10.459 |
|      | 25 | 428.380 | VM | V  | -      | 10.474 |
|      | 25 | 428.515 | VM | VI | 10.542 | 10.520 |
| VIII | 1  | 435.360 | MD | V  | -      | 10.581 |
|      | 2  | 436.330 | VM | V  | 10.464 | 10.544 |
|      | 2  | 436.470 | VM | VI | 10.599 | -      |
|      | 3  | 437.350 | MD | V  | -      | 10.658 |
|      | 3  | 437.470 | MD | VI | 10.503 | -      |
|      | 5  | 439.325 | MD | V  | 10.423 | 10.359 |
|      | 7  | 441.340 | MD | V  | -      | 10.419 |
|      | 11 | 445.305 | MD | V  | 10.469 | 10.387 |
|      | 11 | 445.450 | MD | VI | 10.521 | -      |
|      | 13 | 447.340 | MD | V  | -      | 10.637 |
|      | 20 | 454.445 | MD | VI | 10.494 | 10.529 |
|      | 29 | 463.450 | MD | VI | -      | 10.526 |
|      | 30 | 464.400 | VM | VI | 10.541 | -      |
| IX   | 1  | 466.415 | MD | VI | 10.625 | 10.484 |
|      | 1  | 466.550 | MD | I  | 10.666 | -      |
|      | 2  | 467.390 | VM | VI | 10.513 | -      |
|      | 2  | 467.520 | VM | I  | -      | 10.542 |
|      | 8  | 473.395 | MD | VI | 10.414 | 10.532 |
|      | 9  | 474.395 | VM | VI | 10.479 | 10.439 |
|      | 9  | 474.555 | VM | I  | 10.580 | 10.455 |
|      | 10 | 475.360 | RG | VI | 10.663 | -      |
|      | 16 | 481.350 | VM | VI | 10.589 | -      |
|      | 21 | 486.355 | VM | VI | 10.562 | 10.626 |
|      | 21 | 486.525 | VM | I  | 10.518 | 10.589 |
|      | 23 | 488.355 | VM | VI | 10.490 | 10.576 |
|      | 23 | 488.515 | VM | I  | 10.589 | 10.564 |
|      | 24 | 489.355 | RG | VI | 10.650 | 10.696 |
|      | 24 | 489.515 | RG | I  | 10.431 | 10.429 |
|      | 25 | 490.355 | MD | VI | 10.438 | 10.489 |
|      | 25 | 490.515 | MD | I  | 10.429 | 10.605 |
|      | 27 | 492.345 | RG | VI | 10.596 | 10.599 |
|      | 27 | 492.505 | RG | I  | 10.551 | 10.539 |
|      | 29 | 494.335 | MD | VI | 10.575 | 10.502 |
|      | 29 | 494.530 | MD | I  | -      | 10.681 |
| X    | 1  | 496.310 | RG | VI | 10.642 | -      |
|      | 3  | 498.300 | VM | VI | 10.579 | -      |
|      | 4  | 499.325 | RG | VI | 10.462 | 10.614 |
|      | 4  | 499.465 | RG | I  | 10.595 | 10.430 |
|      | 4  | 499.630 | RG | II | 10.464 | -      |

|      |    |         |    |     |        |        |
|------|----|---------|----|-----|--------|--------|
| X    | 6  | 501.315 | MD | VI  | 10.424 | 10.411 |
|      | 6  | 501.490 | MD | I   | 10.437 | -      |
|      | 6  | 501.620 | MD | II  | 10.428 | -      |
|      | 9  | 504.475 | MD | I   | 10.415 | 10.446 |
|      | 11 | 506.465 | RG | I   | 10.713 | 10.465 |
|      | 11 | 506.635 | RG | II  | 10.425 | 10.451 |
|      | 13 | 508.440 | MD | I   | -      | 10.418 |
|      | 13 | 508.490 | MD | II  | 10.614 | -      |
|      | 16 | 511.455 | MD | I   | 10.499 | 10.607 |
|      | 16 | 511.620 | MD | II  | 10.587 | 10.544 |
|      | 17 | 512.455 | VM | I   | 10.560 | 10.588 |
|      | 17 | 512.515 | VM | II  | 10.480 | 10.555 |
|      | 20 | 515.445 | MD | I   | 10.265 | 10.387 |
|      | 21 | 516.445 | VM | I   | 10.513 | 10.503 |
|      | 21 | 516.605 | VM | II  | 10.529 | 10.438 |
|      | 22 | 517.410 | RG | I   | 10.548 | -      |
|      | 23 | 518.435 | MD | I   | 10.575 | 10.464 |
|      | 28 | 523.425 | VM | I   | 10.387 | 10.315 |
|      | 28 | 523.585 | VM | II  | 10.551 | 10.445 |
|      | 29 | 524.390 | RG | I   | 10.500 | -      |
| XI   | 1  | 527.415 | RG | I   | 10.444 | 10.402 |
|      | 2  | 528.410 | VM | I   | 10.435 | 10.512 |
|      | 2  | 528.600 | VM | II  | -      | 10.392 |
|      | 3  | 529.405 | MD | I   | 10.462 | 10.505 |
|      | 4  | 530.405 | RG | I   | 10.451 | 10.375 |
|      | 4  | 530.565 | RG | II  | 10.441 | 10.397 |
|      | 7  | 533.395 | VM | I   | 10.430 | 10.347 |
|      | 11 | 537.410 | VM | I   | -      | 10.459 |
|      | 11 | 537.545 | VM | II  | 10.591 | 10.479 |
|      | 16 | 542.560 | MD | II  | -      | 10.404 |
|      | 17 | 543.340 | VM | I   | 10.369 | -      |
|      | 19 | 545.365 | RG | I   | 10.342 | 10.422 |
|      | 20 | 546.365 | VM | I   | 10.386 | 10.393 |
|      | 28 | 554.335 | VM | I   | 10.303 | 10.321 |
|      | 28 | 554.505 | VM | II  | 10.199 | 10.440 |
| 1970 |    |         |    |     |        |        |
| I    | 3  | 590.270 | RG | I   | 10.217 | -      |
|      | 8  | 595.285 | RG | I   | 10.122 | 10.166 |
|      | 8  | 595.445 | MD | II  | 10.166 | 10.097 |
|      | 8  | 595.615 | MD | III | 10.269 | 10.325 |
|      | 21 | 608.440 | RG | II  | -      | 10.095 |
|      | 21 | 608.560 | RG | III | 10.316 | -      |
|      | 24 | 611.405 | VM | II  | 10.212 | 10.244 |
|      | 29 | 616.395 | MD | II  | 10.144 | 10.348 |
|      | 30 | 617.385 | VM | II  | 10.426 | 10.271 |
|      | 2  | 620.520 | MD | III | 10.306 | -      |
| II   | 12 | 630.380 | MD | II  | -      | 10.260 |
|      | 17 | 635.335 | VM | II  | 10.036 | 10.258 |
|      | 17 | 635.480 | VM | III | 10.163 | -      |
| III  | 2  | 648.330 | MD | II  | -      | 10.321 |
|      | 6  | 652.440 | VM | III | 10.248 | -      |
|      | 7  | 653.625 | RG | IV  | 10.173 | 10.127 |
|      | 8  | 654.310 | VM | II  | -      | 10.218 |
|      | 8  | 654.455 | VM | III | 10.226 | 10.177 |
|      | 9  | 655.310 | MD | II  | -      | 10.281 |
|      | 18 | 664.400 | RG | III | 10.325 | -      |
|      | 20 | 666.425 | VM | III | 10.098 | 10.235 |
|      | 20 | 666.590 | VM | IV  | 10.229 | 10.091 |
|      | 21 | 667.450 | RG | III | -      | 10.301 |
|      | 24 | 670.415 | VM | III | 10.114 | 10.191 |
|      | 24 | 670.575 | VM | IV  | 10.205 | 10.302 |
|      | 29 | 675.370 | MD | III | 10.247 | -      |

VALUES OF BELGRADE LATITUDE OBTAINED IN THE PERIOD 1969.0 - 1975.0

|     |    |         |    |     |        |        |
|-----|----|---------|----|-----|--------|--------|
| IV  | 19 | 675.565 | MD | IV  | 10.347 | 10.256 |
|     | 30 | 676.420 | MD | III | -      | 10.244 |
|     | 30 | 676.535 | RG | IV  | 10.089 | 10.219 |
|     | 4  | 681.585 | RG | III | 10.181 | 10.137 |
|     | 4  | 681.545 | RG | IV  | 10.202 | 10.080 |
|     | 5  | 682.375 | VM | III | 10.256 | 10.114 |
|     | 6  | 683.545 | MD | IV  | 10.287 | 10.235 |
|     | 9  | 686.535 | RG | IV  | 10.078 | 10.213 |
|     | 10 | 687.535 | MD | IV  | 10.168 | 10.262 |
|     | 12 | 689.525 | RG | IV  | 10.150 | 10.037 |
|     | 15 | 692.380 | RG | III | -      | 10.167 |
|     | 15 | 692.515 | RG | IV  | 10.084 | 10.177 |
|     | 17 | 694.345 | MD | III | 10.178 | 10.254 |
|     | 19 | 696.535 | VM | III | 10.156 | 10.183 |
|     | 19 | 696.505 | VM | IV  | 10.300 | 10.281 |
|     | 20 | 697.360 | MD | III | -      | 10.237 |
|     | 22 | 699.500 | RG | IV  | 10.171 | 10.174 |
|     | 23 | 700.495 | MD | IV  | 10.091 | 10.126 |
|     | 29 | 706.475 | RG | IV  | 10.265 | 10.236 |
| V   | 6  | 713.465 | RG | IV  | 10.164 | 10.185 |
|     | 8  | 715.430 | VM | IV  | 10.239 | -      |
|     | 10 | 717.455 | MD | IV  | 10.146 | 10.217 |
|     | 14 | 721.445 | MD | IV  | 10.141 | 10.299 |
|     | 15 | 722.420 | RG | IV  | 9.905  | -      |
|     | 16 | 723.470 | RG | IV  | -      | 10.280 |
|     | 25 | 732.430 | MD | IV  | -      | 10.268 |
|     | 25 | 732.575 | MD | V   | 10.424 | 10.247 |
|     | 26 | 733.405 | VM | IV  | 10.202 | 10.274 |
|     | 26 | 733.550 | VM | V   | 10.308 | -      |
| VI  | 29 | 736.395 | VM | IV  | 10.302 | 10.256 |
|     | 29 | 736.565 | VM | V   | 10.244 | 10.254 |
|     | 5  | 743.400 | MD | IV  | -      | 10.436 |
|     | 6  | 744.400 | RG | IV  | -      | 10.270 |
|     | 6  | 744.545 | RG | V   | 10.297 | 10.261 |
|     | 15 | 753.520 | MD | V   | 10.391 | 10.306 |
|     | 17 | 755.490 | RG | V   | 10.463 | -      |
|     | 20 | 758.480 | RG | V   | 10.378 | -      |
|     | 21 | 759.505 | MD | V   | 10.385 | 10.433 |
|     | 25 | 763.520 | MD | V   | -      | 10.327 |
| VII | 27 | 765.485 | RG | V   | 10.361 | 10.323 |
|     | 27 | 765.630 | RG | VI  | 10.402 | -      |
|     | 28 | 766.435 | VM | V   | 10.309 | 10.453 |
|     | 1  | 769.450 | RG | V   | 10.398 | -      |
|     | 8  | 776.455 | RG | V   | 10.361 | 10.405 |
|     | 8  | 776.525 | RG | VI  | 10.380 | 10.378 |
|     | 9  | 777.455 | MD | V   | 10.463 | 10.352 |
|     | 9  | 777.650 | MD | VI  | -      | 10.365 |
|     | 10 | 778.445 | VM | V   | 10.463 | 10.329 |
|     | 10 | 778.615 | VM | VI  | 10.405 | 10.409 |
|     | 11 | 779.435 | RG | V   | 10.484 | 10.536 |
|     | 11 | 779.615 | RG | VI  | 10.416 | 10.378 |
|     | 12 | 780.435 | MD | V   | 10.453 | 10.364 |
|     | 12 | 780.605 | MD | VI  | 10.481 | 10.304 |
|     | 15 | 783.450 | RG | V   | -      | 10.375 |
|     | 19 | 787.415 | VM | V   | 10.462 | 10.419 |
|     | 19 | 787.585 | VM | VI  | 10.474 | 10.465 |
|     | 20 | 788.585 | MD | VI  | 10.414 | 10.533 |
|     | 21 | 789.415 | VM | V   | 10.390 | 10.474 |
|     | 21 | 789.565 | VM | VI  | 10.515 | 10.416 |
|     | 22 | 790.415 | RG | V   | 10.420 | 10.474 |
|     | 22 | 790.565 | RG | VI  | 10.464 | 10.434 |

|      |    |         |    |    |        |        |
|------|----|---------|----|----|--------|--------|
|      | 23 | 791.415 | MD | V  | 10.537 | 10.561 |
|      | 23 | 791.585 | MD | VI | 10.544 | 10.566 |
|      | 24 | 792.415 | VM | V  | 10.555 | 10.497 |
|      | 24 | 792.575 | VM | VI | 10.577 | 10.594 |
|      | 26 | 794.405 | MD | V  | 10.441 | 10.440 |
|      | 26 | 794.575 | MD | VI | 10.402 | 10.461 |
|      | 27 | 795.405 | VM | V  | 10.470 | 10.463 |
|      | 27 | 795.575 | VM | VI | 10.586 | 10.443 |
|      | 29 | 797.395 | MD | V  | 10.559 | 10.518 |
|      | 29 | 797.565 | MD | VI | 10.575 | 10.551 |
| VIII | 3  | 802.400 | MD | V  | -      | 10.504 |
|      | 4  | 803.400 | VM | V  | -      | 10.488 |
|      | 6  | 805.365 | MD | V  | 10.551 | 10.491 |
|      | 7  | 806.365 | VM | V  | 10.529 | 10.531 |
|      | 18 | 817.505 | RG | VI | 10.564 | 10.627 |
|      | 20 | 819.530 | RG | VI | -      | 10.654 |
|      | 26 | 825.510 | MD | VI | -      | 10.625 |
|      | 27 | 826.485 | RG | VI | 10.511 | 10.540 |
|      | 27 | 826.645 | RG | I  | 10.517 | 10.610 |
| IX   | 2  | 832.465 | MD | VI | 10.626 | 10.647 |
|      | 2  | 832.600 | MD | I  | 10.796 | -      |
|      | 3  | 833.465 | RG | VI | 10.558 | 10.567 |
|      | 7  | 837.370 | VM | VI | 10.578 | -      |
|      | 8  | 838.395 | RG | VI | 10.581 | 10.541 |
|      | 9  | 839.395 | VM | VI | 10.507 | 10.524 |
|      | 9  | 839.555 | VM | I  | 10.622 | 10.562 |
|      | 11 | 841.385 | VM | VI | 10.675 | 10.554 |
|      | 11 | 841.530 | VM | I  | 10.511 | -      |
|      | 15 | 845.400 | LD | VI | -      | 10.595 |
|      | 21 | 851.340 | RG | VI | 10.525 | -      |
|      | 23 | 853.355 | VM | VI | 10.508 | 10.599 |
|      | 23 | 853.515 | VM | I  | 10.701 | 10.604 |
|      | 29 | 859.335 | LD | VI | 10.637 | 10.733 |
|      | 29 | 859.480 | LD | I  | 10.729 | -      |
|      | 30 | 860.335 | LD | VI | 10.579 | 10.694 |
|      | 30 | 860.480 | LD | I  | 10.695 | -      |
| X    | 6  | 866.320 | VM | VI | 10.632 | 10.565 |
|      | 6  | 866.485 | VM | I  | 10.542 | 10.598 |
|      | 8  | 868.315 | VM | VI | 10.627 | 10.497 |
|      | 8  | 868.480 | VM | I  | 10.549 | 10.746 |
|      | 9  | 869.315 | MD | VI | 10.598 | 10.686 |
|      | 9  | 869.480 | MD | I  | 10.673 | 10.432 |
|      | 11 | 871.475 | MD | I  | 10.641 | 10.830 |
|      | 12 | 872.315 | RG | VI | 10.655 | 10.588 |
|      | 13 | 873.315 | VM | VI | 10.590 | 10.617 |
|      | 13 | 873.465 | VM | I  | 10.695 | 10.659 |
|      | 19 | 879.260 | MD | VI | 10.685 | -      |
|      | 26 | 886.290 | MD | VI | -      | 10.511 |
|      | 26 | 886.425 | MD | I  | 10.618 | 10.583 |
|      | 28 | 888.415 | RG | I  | 10.673 | 10.593 |
|      | 28 | 888.575 | RG | II | 10.529 | 10.513 |
|      | 30 | 890.255 | LD | VI | 10.538 | 10.577 |
|      | 30 | 890.415 | VM | I  | 10.653 | 10.588 |
|      | 30 | 890.575 | VM | II | 10.611 | 10.532 |
|      | 31 | 891.220 | RG | VI | 10.516 | -      |
| XI   | 1  | 892.405 | RG | I  | 10.592 | 10.580 |
|      | 1  | 892.590 | RG | II | -      | 10.512 |
|      | 3  | 894.405 | VM | I  | 10.530 | 10.459 |
|      | 3  | 894.565 | VM | II | 10.577 | 10.584 |
|      | 4  | 895.395 | RG | I  | 10.527 | 10.509 |
|      | 4  | 895.565 | RG | II | 10.481 | 10.403 |
|      | 5  | 896.335 | LD | VI | 10.580 | 10.520 |

## VALUES OF BELGRADE LATITUDE OBTAINED IN THE PERIOD 1969.0-1975.0

|      |    |          |    |     |        |        |
|------|----|----------|----|-----|--------|--------|
| II   | 7  | 898.337  | RG | VI  | 10.500 | 10.487 |
|      | 7  | 898.395  | RG | I   | 10.605 | 10.505 |
|      | 11 | 902.375  | RG | I   | 10.581 | 10.403 |
|      | 12 | 903.365  | MD | I   | 10.551 | 10.732 |
|      | 12 | 903.525  | MD | II  | 10.524 | 10.509 |
|      | 13 | 904.365  | VM | I   | 10.510 | 10.652 |
|      | 19 | 910.355  | MD | I   | 10.482 | 10.578 |
|      | 25 | 916.345  | VM | I   | 10.538 | 10.414 |
|      | 25 | 916.515  | RG | II  | 10.614 | 10.415 |
|      | 29 | 920.335  | VM | I   | 10.447 | 10.547 |
|      | 29 | 920.480  | VM | II  | 10.485 | -      |
| 1971 |    |          |    |     |        |        |
| I    | 19 | 971.340  | RG | II  | 10.166 | -      |
|      | 20 | 972.355  | VM | II  | 10.314 | 10.332 |
|      | 23 | 975.355  | RG | II  | 10.282 | 10.403 |
|      | 23 | 975.515  | RG | III | 10.316 | 10.237 |
|      | 30 | 982.505  | RG | III | 10.446 | 10.350 |
| II   | 10 | 993.510  | RG | III | -      | 10.177 |
|      | 11 | 994.295  | MD | II  | 10.375 | 10.221 |
|      | 11 | 994.485  | MD | III | 10.483 | 10.249 |
|      | 12 | 995.285  | VM | II  | 10.144 | 10.299 |
|      | 12 | 995.475  | VM | III | 10.269 | 10.140 |
|      | 13 | 996.285  | RG | II  | 10.214 | 10.187 |
|      | 13 | 996.470  | RG | III | 10.345 | 10.172 |
|      | 16 | 999.260  | LD | II  | 10.341 | -      |
| III  |    | 2441000+ |    |     |        |        |
|      | 10 | 021.560  | RG | IV  | 10.016 | 10.186 |
|      | 12 | 023.530  | LD | IV  | 10.275 | -      |
|      | 13 | 024.385  | RG | III | 10.423 | 10.049 |
|      | 13 | 024.555  | RG | IV  | 10.093 | 10.211 |
|      | 15 | 026.400  | MD | III | -      | 10.218 |
|      | 18 | 029.365  | MD | III | 10.225 | 10.126 |
|      | 18 | 029.535  | MD | IV  | 10.137 | 10.184 |
|      | 20 | 031.365  | RG | III | 10.132 | 10.012 |
|      | 20 | 031.535  | RG | IV  | 9.970  | 10.172 |
|      | 22 | 033.365  | MD | III | 10.236 | 10.108 |
|      | 24 | 035.525  | LD | IV  | 10.346 | 10.176 |
|      | 25 | 036.380  | MD | III | -      | 10.306 |
|      | 25 | 036.520  | MD | IV  | 10.229 | 10.388 |
|      | 26 | 037.350  | LD | III | 10.321 | 10.194 |
|      | 26 | 037.515  | LD | IV  | 10.104 | 10.197 |
|      | 31 | 042.327  | RG | III | 10.113 | 10.027 |
| IV   | 2  | 044.480  | LD | IV  | 10.350 | -      |
|      | 7  | 049.340  | RG | III | -      | 10.082 |
|      | 8  | 050.315  | MD | III | 10.282 | 10.229 |
|      | 8  | 050.485  | MD | IV  | 10.103 | 10.240 |
|      | 9  | 051.315  | LD | III | 10.053 | 10.048 |
|      | 9  | 051.485  | LD | IV  | 9.972  | 10.268 |
|      | 14 | 056.320  | MD | III | -      | 10.089 |
|      | 14 | 056.465  | MD | IV  | 10.272 | 10.357 |
|      | 15 | 057.465  | VM | IV  | 10.129 | 10.059 |
|      | 16 | 058.465  | LD | IV  | 10.118 | 10.191 |
|      | 18 | 060.455  | MD | IV  | 10.180 | 10.172 |
|      | 20 | 062.310  | LD | III | -      | 10.159 |
|      | 20 | 062.445  | LD | IV  | 10.044 | 10.180 |
|      | 21 | 063.445  | MD | IV  | 10.099 | 10.304 |
|      | 21 | 063.590  | MD | V   | 10.246 | -      |
| V    | 7  | 079.430  | LD | IV  | -      | 10.213 |
|      | 9  | 081.395  | MD | IV  | 10.161 | 10.189 |
|      | 10 | 082.370  | VM | IV  | 10.108 | -      |
|      | 11 | 083.385  | LD | IV  | 10.086 | 10.088 |
|      | 11 | 083.570  | LD | V   | -      | 10.139 |



|      |    |         |    |    |        |        |
|------|----|---------|----|----|--------|--------|
| V    | 12 | 084.36  | VM | IV | 10.201 | -      |
|      | 12 | 084.343 | VI | V  | 10.150 | 10.177 |
|      | 13 | 085.375 | LD | IV | 10.207 | 10.185 |
|      | 13 | 085.335 | MD | V  | 10.154 | 10.137 |
|      | 14 | 086.375 | LD | IV | 10.310 | 10.245 |
|      | 14 | 086.380 | LD | V  | -      | 10.187 |
|      | 17 | 089.335 | MD | V  | 10.225 | 10.225 |
|      | 18 | 090.335 | LD | V  | 10.276 | 10.317 |
|      | 25 | 097.330 | LD | IV | 10.082 | -      |
|      | 3  | 106.500 | MD | V  | 10.334 | 10.335 |
| VI   | 11 | 114.330 | LD | IV | -      | 10.133 |
|      | 11 | 114.475 | LD | V  | 10.367 | 10.384 |
|      | 14 | 117.465 | MD | V  | 10.423 | 10.308 |
|      | 15 | 118.440 | LD | V  | 10.329 | -      |
|      | 24 | 127.420 | MD | V  | 10.234 | -      |
|      | 28 | 131.425 | MD | V  | 10.327 | 10.311 |
|      | 8  | 141.400 | MD | V  | 10.453 | 10.395 |
|      | 9  | 142.395 | LD | V  | 10.359 | 10.307 |
|      | 10 | 143.395 | MD | V  | 10.308 | 10.425 |
|      | 12 | 145.395 | MD | V  | 10.338 | 10.404 |
| VII  | 12 | 145.555 | MD | VI | 10.390 | 10.470 |
|      | 16 | 149.360 | LD | V  | 10.262 | -      |
|      | 17 | 150.520 | VM | VI | 10.298 | -      |
|      | 22 | 155.500 | LD | VI | 10.293 | -      |
|      | 25 | 158.355 | LD | V  | 10.325 | 10.277 |
|      | 27 | 160.345 | LD | V  | 10.488 | 10.391 |
|      | 27 | 160.490 | LD | VI | 10.452 | -      |
|      | 19 | 183.455 | MD | VI | 10.505 | 10.502 |
|      | 20 | 184.285 | VM | V  | 10.487 | 10.493 |
|      | 20 | 184.470 | VM | VI | -      | 10.427 |
| VIII | 21 | 185.445 | MD | VI | 10.525 | 10.492 |
|      | 26 | 190.290 | MD | V  | -      | 10.364 |
|      | 26 | 190.435 | MD | VI | 10.550 | 10.489 |
|      | 28 | 192.400 | VM | VI | 10.384 | -      |
|      | 29 | 193.280 | MD | V  | -      | 10.557 |
|      | 30 | 194.280 | VM | V  | -      | 10.497 |
|      | 30 | 194.425 | VM | VI | 10.506 | 10.501 |
|      | 3  | 198.405 | LD | VI | 10.550 | 10.623 |
|      | 3  | 198.575 | LD | I  | 10.585 | 10.621 |
|      | 4  | 199.405 | MD | VI | 10.564 | 10.599 |
| IX   | 4  | 199.575 | MD | I  | 10.655 | 10.699 |
|      | 9  | 204.420 | MD | VI | -      | 10.559 |
|      | 9  | 204.530 | MD | I  | 10.733 | -      |
|      | 12 | 207.395 | VM | VI | 10.620 | 10.596 |
|      | 21 | 216.360 | LD | VI | 10.737 | 10.589 |
|      | 21 | 216.525 | LD | I  | 10.552 | 10.787 |
|      | 22 | 217.355 | VM | VI | 10.583 | 10.624 |
|      | 22 | 217.525 | VM | I  | 10.540 | 10.702 |
|      | 23 | 218.355 | MD | VI | 10.755 | 10.712 |
|      | 23 | 218.515 | MD | I  | 10.626 | 10.614 |
| X    | 24 | 219.355 | LD | VI | 10.688 | 10.556 |
|      | 24 | 219.515 | LD | I  | 10.612 | 10.703 |
|      | 26 | 221.515 | MD | I  | 10.650 | 10.650 |
|      | 27 | 222.320 | VM | VI | 10.629 | -      |
|      | 27 | 222.505 | VM | I  | 10.547 | 10.692 |
|      | 2  | 227.335 | MD | VI | 10.735 | 10.695 |
|      | 4  | 229.300 | MD | VI | 10.713 | 10.695 |
|      | 5  | 230.300 | LD | VI | 10.628 | -      |
|      | 5  | 230.485 | LD | I  | 10.632 | 10.753 |
|      | 8  | 233.515 | LD | VI | 10.652 | 10.649 |
| XI   | 8  | 233.475 | LD | I  | 10.634 | 10.704 |
|      | 10 | 235.305 | MD | VI | 10.744 | 10.687 |
|      | 10 | 235.475 | MD | I  | 10.735 | 10.777 |

VALUES OF BELGRADE LATITUDE OBTAINED IN THE PERIOD 1969.0-1975.0

|      |    |         |    |     |        |        |
|------|----|---------|----|-----|--------|--------|
|      | 11 | 236.305 | VM | VI  | 10.661 | 10.726 |
|      | 11 | 236.475 | VM | I   | 10.768 | 10.765 |
|      | 12 | 237.305 | LD | VI  | 10.699 | 10.666 |
|      | 12 | 237.465 | LD | I   | 10.654 | 10.675 |
|      | 13 | 238.305 | MD | VI  | 10.531 | 10.610 |
|      | 14 | 239.295 | MD | VI  | 10.700 | 10.634 |
|      | 14 | 239.465 | MD | I   | 10.568 | 10.581 |
|      | 19 | 244.285 | LD | VI  | 10.547 | 10.567 |
|      | 19 | 244.470 | LD | I   | -      | 10.756 |
|      | 20 | 245.285 | VM | VI  | 10.610 | 10.644 |
|      | 20 | 245.445 | VM | I   | 10.664 | 10.587 |
|      | 22 | 247.275 | LD | VI  | 10.661 | 10.505 |
|      | 22 | 247.445 | LD | I   | 10.729 | 10.778 |
|      | 23 | 248.275 | VM | VI  | 10.642 | 10.637 |
|      | 23 | 248.435 | VM | I   | 10.606 | 10.736 |
|      | 24 | 249.275 | MD | VI  | 10.605 | 10.484 |
|      | 24 | 249.435 | MD | I   | 10.615 | 10.654 |
|      | 26 | 251.240 | LD | VI  | 10.568 | -      |
|      | 28 | 253.425 | MD | I   | 10.627 | 10.724 |
|      | 29 | 254.425 | LD | I   | 10.565 | 10.648 |
| XI   | 5  | 261.405 | LD | I   | 10.500 | 10.490 |
|      | 5  | 261.565 | LD | II  | 10.561 | 10.545 |
|      | 6  | 262.400 | VM | I   | 10.560 | 10.553 |
|      | 6  | 262.565 | VM | II  | 10.677 | 10.647 |
|      | 8  | 264.395 | MD | I   | 10.532 | 10.551 |
|      | 8  | 264.580 | MD | II  | -      | 10.624 |
|      | 11 | 267.385 | MD | I   | 10.749 | 10.618 |
|      | 11 | 267.520 | MD | II  | 10.549 | -      |
|      | 15 | 271.680 | MD | III | 10.617 | -      |
|      | 27 | 283.345 | VM | I   | 10.612 | 10.499 |
|      | 27 | 283.505 | VM | II  | 10.437 | 10.559 |
| XII  | 7  | 293.340 | LD | I   | -      | 10.488 |
|      | 7  | 293.500 | LD | II  | -      | 10.574 |
|      | 10 | 296.305 | LD | I   | 10.625 | 10.692 |
|      | 15 | 301.295 | VM | I   | 10.550 | 10.629 |
|      | 15 | 301.455 | VM | II  | 10.625 | 10.592 |
|      | 22 | 308.275 | VM | I   | 10.464 | 10.495 |
|      | 22 | 308.440 | VM | II  | -      | 10.572 |
|      | 23 | 309.275 | MD | I   | 10.448 | 10.466 |
|      | 23 | 309.410 | MD | II  | 10.315 | -      |
| 1972 |    |         |    |     |        |        |
| II   | 2  | 350.350 | RG | II  | -      | 10.476 |
|      | 3  | 351.325 | MD | II  | 10.512 | 10.526 |
|      | 5  | 353.315 | RG | II  | 10.267 | 10.442 |
|      | 17 | 365.285 | MD | II  | 10.444 | 10.449 |
|      | 17 | 365.455 | MD | III | 10.358 | 10.502 |
|      | 18 | 366.280 | LD | II  | 10.438 | 10.382 |
|      | 20 | 368.250 | RG | II  | 10.316 | -      |
|      | 26 | 374.255 | RG | II  | 10.272 | 10.290 |
|      | 26 | 374.410 | RG | III | 10.358 | -      |
| III  | 1  | 378.270 | RG | II  | -      | 10.283 |
|      | 1  | 378.425 | RG | III | 10.356 | 10.281 |
|      | 4  | 381.415 | RG | III | 10.243 | 10.184 |
|      | 13 | 390.385 | LD | III | 10.228 | 10.250 |
|      | 13 | 390.555 | MD | IV  | 10.260 | 10.541 |

|     |    |         |    |     |        |        |
|-----|----|---------|----|-----|--------|--------|
|     | 14 | 391.335 | RG | III | 10.138 | 10.345 |
|     | 14 | 391.555 | RG | IV  | 10.452 | 10.288 |
|     | 15 | 392.375 | MD | III | 10.263 | 10.429 |
|     | 15 | 392.545 | LD | IV  | 10.397 | 10.378 |
|     | 17 | 394.375 | MD | III | 10.299 | 10.326 |
|     | 19 | 396.365 | RG | III | 10.248 | 10.343 |
|     | 20 | 397.330 | LD | III | 10.372 | -      |
|     | 20 | 397.525 | LD | IV  | 10.132 | 10.335 |
|     | 21 | 398.550 | MD | IV  | -      | 10.385 |
|     | 25 | 402.345 | RG | III | 10.215 | 10.210 |
|     | 30 | 407.335 | LD | III | 10.211 | 10.155 |
|     | 31 | 408.310 | MD | III | 10.321 | -      |
| IV  | 2  | 410.470 | RG | IV  | 10.224 | -      |
|     | 3  | 411.325 | LD | III | 10.092 | 10.082 |
|     | 4  | 412.510 | MD | IV  | -      | 10.247 |
|     | 5  | 413.325 | RG | III | 10.291 | 10.114 |
|     | 7  | 415.460 | MD | IV  | 10.175 | -      |
|     | 8  | 416.290 | RG | III | 10.223 | -      |
|     | 8  | 416.480 | RG | IV  | 10.208 | 10.236 |
|     | 10 | 418.305 | LD | III | 10.263 | 10.037 |
|     | 22 | 430.445 | RG | IV  | 10.277 | 10.209 |
|     | 29 | 437.400 | RG | IV  | 10.139 | -      |
| V   | 6  | 444.405 | RG | IV  | 10.199 | 10.148 |
|     | 6  | 444.570 | RG | V   | 10.129 | 10.137 |
|     | 7  | 445.420 | MD | IV  | -      | 10.211 |
|     | 8  | 446.395 | LD | IV  | 10.099 | 10.164 |
|     | 8  | 446.565 | LD | V   | 10.122 | 10.129 |
|     | 17 | 455.350 | RG | IV  | 10.233 | -      |
|     | 22 | 460.365 | LD | IV  | 10.243 | 10.258 |
|     | 22 | 460.535 | LD | V   | 10.225 | 10.296 |
|     | 23 | 461.355 | MD | IV  | 10.164 | 10.392 |
|     | 23 | 461.525 | MD | V   | 10.201 | 10.214 |
|     | 24 | 462.355 | RG | IV  | 10.306 | 10.229 |
|     | 24 | 462.525 | RG | V   | 10.112 | 10.097 |
|     | 25 | 463.320 | LD | IV  | 10.118 | -      |
|     | 26 | 464.320 | MD | IV  | 10.102 | -      |
|     | 29 | 467.360 | LD | IV  | -      | 10.065 |
|     | 29 | 467.530 | LD | V   | -      | 10.074 |
|     | 30 | 468.325 | MD | IV  | 10.244 | 10.218 |
|     | 30 | 468.495 | MD | V   | 10.262 | 10.267 |
|     | 31 | 469.350 | RG | IV  | -      | 10.183 |
|     | 31 | 469.495 | RG | V   | 10.257 | 10.159 |
| VI  | 5  | 474.435 | LD | V   | 10.195 | 10.225 |
|     | 6  | 475.315 | MD | IV  | 10.124 | 10.156 |
|     | 6  | 475.460 | MD | V   | 10.241 | -      |
|     | 7  | 476.315 | RG | IV  | 10.190 | 10.206 |
|     | 7  | 476.485 | RG | V   | 10.163 | 10.080 |
|     | 8  | 477.340 | LD | IV  | -      | 10.153 |
|     | 8  | 477.500 | LD | V   | -      | 10.124 |
|     | 9  | 478.330 | MD | IV  | -      | 10.169 |
|     | 9  | 478.475 | MD | V   | 10.268 | 10.259 |
|     | 15 | 484.480 | LD | V   | -      | 10.132 |
|     | 17 | 486.455 | RG | V   | 10.110 | 10.192 |
|     | 21 | 490.450 | RG | V   | 10.182 | 10.165 |
|     | 25 | 494.435 | RG | V   | 10.175 | 10.177 |
|     | 26 | 495.435 | LD | V   | 10.209 | 10.233 |
|     | 28 | 497.450 | RG | V   | -      | 10.225 |
|     | 28 | 497.570 | RG | VI  | 10.305 | -      |
|     | 29 | 498.425 | LD | V   | 10.158 | 10.050 |
| VII | 2  | 501.415 | RG | V   | 10.311 | 10.267 |
|     | 5  | 504.405 | RG | V   | 10.134 | 10.193 |
|     | 6  | 507.370 | RG | V   | 10.105 | -      |
|     | 10 | 509.395 | RG | V   | 10.249 | 10.329 |

|      |    |         |    |     |        |        |
|------|----|---------|----|-----|--------|--------|
|      | 16 | 515.350 | RG | V   | 10.392 | -      |
|      | 18 | 517.340 | MD | V   | -      | 10.280 |
|      | 18 | 517.510 | MD | VI  | 10.117 | -      |
|      | 19 | 518.340 | RG | V   | 10.193 | -      |
|      | 20 | 519.510 | MD | VI  | 10.130 | -      |
| VIII | 30 | 529.360 | MD | V   | -      | 10.165 |
|      | 9  | 539.315 | MD | V   | 10.173 | 10.259 |
|      | 9  | 539.450 | MD | VI  | 10.276 | -      |
|      | 11 | 541.305 | MD | V   | 10.196 | 10.179 |
|      | 11 | 541.450 | MD | VI  | 10.295 | -      |
|      | 14 | 544.490 | MD | VI  | -      | 10.245 |
|      | 27 | 557.280 | MD | V   | -      | 10.292 |
|      | 27 | 557.400 | MD | VI  | 10.350 | -      |
| IX   | 1  | 562.415 | MD | VI  | 10.338 | 10.290 |
|      | 6  | 567.400 | RG | VI  | 10.430 | 10.415 |
|      | 7  | 568.395 | LD | VI  | 10.508 | 10.537 |
|      | 14 | 575.375 | RG | VI  | 10.471 | 10.399 |
|      | 14 | 575.520 | RG | I   | 10.532 | -      |
|      | 18 | 579.340 | RG | VI  | 10.442 | -      |
|      | 22 | 583.355 | LD | VI  | 10.467 | 10.514 |
|      | 22 | 583.550 | LD | I   | -      | 10.521 |
|      | 25 | 586.355 | RG | VI  | 10.530 | 10.391 |
|      | 28 | 589.345 | RG | VI  | 10.485 | 10.474 |
| X    | 15 | 606.455 | MD | I   | 10.354 | 10.357 |
|      | 17 | 608.310 | MD | VI  | -      | 10.468 |
|      | 24 | 615.460 | MD | I   | -      | 10.436 |
|      | 25 | 616.260 | RG | VI  | 10.453 | 10.455 |
|      | 25 | 616.430 | RG | I   | 10.500 | 10.510 |
|      | 26 | 617.265 | LD | VI  | 10.670 | 10.678 |
|      | 26 | 617.425 | LD | I   | 10.619 | 10.595 |
|      | 27 | 618.260 | MD | VI  | 10.390 | 10.499 |
|      | 27 | 618.425 | MD | I   | 10.592 | 10.363 |
|      | 31 | 622.245 | MD | VI  | 10.455 | 10.376 |
|      | 31 | 622.415 | MD | I   | 10.575 | 10.354 |
| XI   | 1  | 623.245 | RG | VI  | 10.521 | 10.656 |
|      | 1  | 623.415 | RG | I   | 10.534 | 10.467 |
|      | 4  | 626.405 | RG | I   | 10.632 | 10.511 |
|      | 7  | 629.370 | MD | I   | 10.521 | -      |
|      | 8  | 630.395 | RG | I   | 10.695 | 10.651 |
|      | 9  | 631.420 | LD | I   | -      | 10.707 |
|      | 12 | 634.385 | RG | I   | 10.610 | 10.527 |
|      | 28 | 650.360 | MD | I   | -      | 10.476 |
|      | 28 | 650.480 | MD | II  | 10.483 | -      |
| XII  | 3  | 655.325 | RG | I   | 10.568 | 10.606 |
|      | 4  | 656.325 | LD | I   | 10.520 | 10.482 |
|      | 20 | 672.275 | RG | I   | 10.464 | 10.526 |
|      | 20 | 672.445 | RG | II  | 10.514 | 10.633 |
|      | 21 | 673.275 | LD | I   | 10.522 | 10.493 |
|      | 23 | 675.240 | RG | I   | 10.461 | -      |
|      | 28 | 680.255 | RG | I   | 10.562 | 10.514 |
|      | 29 | 681.270 | MD | I   | -      | 10.511 |
| 1973 |    |         |    |     |        |        |
| I    | 13 | 696.240 | RG | I   | -      | 10.431 |
|      | 14 | 697.375 | MD | II  | 10.460 | 10.443 |
|      | 20 | 703.330 | RG | II  | 10.499 | -      |
|      | 25 | 708.370 | LD | II  | -      | 10.545 |
|      | 26 | 709.345 | MD | II  | 10.254 | 10.543 |
| II   | 6  | 720.475 | RG | III | 10.469 | 10.431 |
|      | 8  | 722.450 | LD | III | 10.196 | -      |
|      | 12 | 726.395 | LD | II  | 10.488 | 10.560 |
|      | 12 | 726.465 | RG | III | 10.329 | 10.338 |
|      | 19 | 733.250 | LD | II  | 10.421 | -      |

|      |    |         |    |     |        |        |
|------|----|---------|----|-----|--------|--------|
| III  | 19 | 733.445 | RG | III | 10.467 | 10.292 |
|      | 17 | 759.375 | RG | III | 10.340 | 10.340 |
|      | 17 | 759.540 | RG | IV  | 10.270 | 10.382 |
|      | 22 | 764.355 | LD | III | 10.394 | 10.266 |
|      | 22 | 764.525 | LD | IV  | 10.350 | 10.346 |
|      | 23 | 765.355 | MD | III | 10.392 | 10.186 |
|      | 23 | 765.525 | MD | IV  | 10.229 | 10.254 |
|      | 31 | 773.335 | RG | III | 10.231 | 10.295 |
|      | 31 | 773.505 | RG | IV  | 10.336 | 10.336 |
|      | 2  | 775.325 | LD | III | 10.400 | 10.266 |
| IV   | 2  | 775.490 | LD | IV  | 10.309 | 10.318 |
|      | 7  | 780.315 | RG | III | 10.312 | 10.365 |
|      | 7  | 780.460 | RG | IV  | 10.185 | -      |
|      | 17 | 790.430 | MD | IV  | 10.250 | -      |
|      | 18 | 791.285 | RG | III | 10.298 | 10.254 |
|      | 22 | 795.445 | RG | IV  | 10.180 | 10.194 |
|      | 27 | 800.435 | MD | IV  | 10.202 | 10.314 |
|      | 13 | 816.410 | RG | IV  | -      | 10.192 |
|      | 13 | 816.530 | RG | V   | 10.195 | -      |
|      | 14 | 817.385 | MD | IV  | 10.103 | 10.138 |
| V    | 15 | 818.400 | RG | IV  | -      | 10.257 |
|      | 17 | 820.375 | RG | IV  | 10.112 | 10.215 |
|      | 21 | 824.365 | MD | IV  | 10.084 | 10.162 |
|      | 22 | 825.360 | RG | IV  | 10.208 | 10.135 |
|      | 24 | 827.330 | RG | IV  | 10.130 | -      |
|      | 29 | 832.345 | RG | IV  | 10.098 | 10.286 |
|      | 29 | 832.505 | RG | V   | 10.239 | 10.166 |
|      | 30 | 833.360 | MD | IV  | 10.114 | 10.165 |
|      | 1  | 835.335 | MD | IV  | 9.996  | 10.026 |
|      | 1  | 835.500 | MD | V   | 10.238 | 10.121 |
| VI   | 12 | 846.470 | RG | V   | 10.132 | 10.289 |
|      | 13 | 847.320 | MD | IV  | -      | 10.193 |
|      | 13 | 847.465 | MD | V   | 10.092 | 10.176 |
|      | 16 | 850.440 | RG | V   | 10.155 | -      |
|      | 22 | 856.445 | MD | V   | 10.234 | 10.074 |
|      | 5  | 869.405 | RG | V   | 10.092 | 10.176 |
|      | 6  | 870.405 | MD | V   | 10.020 | 10.156 |
|      | 10 | 874.400 | RG | V   | 10.183 | 10.204 |
|      | 12 | 876.385 | RG | V   | 10.210 | 10.105 |
|      | 16 | 880.375 | RG | V   | 10.200 | 10.184 |
| VII  | 19 | 883.340 | RG | V   | 10.238 | -      |
|      | 21 | 885.365 | RG | V   | 10.106 | 10.185 |
|      | 31 | 895.335 | RG | V   | 10.271 | 10.335 |
|      | 1  | 896.480 | RG | VI  | 10.257 | -      |
|      | 21 | 916.445 | MD | VI  | 10.292 | 10.168 |
|      | 2  | 928.415 | RG | VI  | 10.334 | 10.254 |
|      | 4  | 930.405 | RG | VI  | 10.367 | 10.371 |
|      | 7  | 933.370 | MD | VI  | 10.172 | -      |
|      | 9  | 935.395 | MD | VI  | 10.264 | 10.252 |
|      | 11 | 937.380 | RG | VI  | 10.463 | 10.437 |
| VIII | 12 | 938.350 | MD | VI  | 10.325 | -      |
|      | 15 | 941.340 | RG | VI  | 10.380 | -      |
|      | 16 | 942.365 | MD | VI  | 10.211 | 10.297 |
|      | 20 | 946.365 | RG | VI  | 10.347 | 10.367 |
|      | 20 | 946.550 | RG | I   | -      | 10.331 |
|      | 25 | 951.370 | RG | VI  | -      | 10.212 |
|      | 29 | 955.335 | RG | VI  | 10.306 | 10.278 |
|      | 29 | 955.505 | RG | I   | 10.385 | 10.207 |
|      | 5  | 961.325 | MD | VI  | 10.266 | 10.285 |
|      | 5  | 961.480 | MD | I   | 10.317 | 10.282 |
| IX   | 10 | 966.330 | MD | VI  | -      | 10.377 |
|      | 11 | 967.305 | RG | VI  | 10.249 | 10.249 |
|      | 11 | 967.460 | RG | T   | 10.231 | 10.449 |
|      | 11 | 967.460 | RG |     |        |        |

|      |    |         |    |     |        |        |
|------|----|---------|----|-----|--------|--------|
|      | 19 | 975.470 | MD | I   | -      | 10.286 |
|      | 23 | 979.250 | RG | VI  | 10.353 | -      |
|      | 26 | 982.265 | MD | VI  | 10.438 | 10.445 |
|      | 27 | 983.260 | RG | VI  | 10.314 | 10.371 |
| XI   | 27 | 983.425 | RG | I   | 10.421 | 10.538 |
|      | 1  | 988.415 | RG | I   | 10.400 | 10.522 |
|      | 10 | 997.385 | RG | I   | 10.443 | 10.324 |
|      | 18 | 005.365 | RG | I   | 10.476 | 10.388 |
|      | 19 | 006.365 | MD | I   | 10.317 | 10.430 |
|      | 19 | 006.550 | MD | II  | -      | 10.267 |
|      | 20 | 007.355 | RG | I   | 10.383 | 10.342 |
| XII  | 23 | 010.330 | MD | I   | 10.501 | -      |
|      | 6  | 023.290 | RG | I   | 10.276 | -      |
|      | 10 | 027.305 | MD | I   | 10.470 | 10.420 |
|      | 10 | 027.470 | RG | II  | 10.401 | 10.332 |
|      | 16 | 033.260 | RG | I   | 10.538 | -      |
|      | 20 | 037.250 | RG | I   | 10.438 | -      |
|      | 20 | 037.445 | MD | II  | 10.423 | 10.522 |
|      | 23 | 040.435 | RG | II  | 10.397 | 10.344 |
| 1974 |    |         |    |     |        |        |
| I    | 9  | 057.385 | MD | II  | 10.315 | 10.379 |
|      | 9  | 057.555 | RG | III | 10.303 | 10.356 |
|      | 13 | 061.375 | RG | II  | 10.351 | 10.363 |
|      | 13 | 061.545 | MD | III | 10.455 | 10.222 |
|      | 15 | 063.400 | RG | II  | -      | 10.351 |
|      | 22 | 070.380 | RG | II  | -      | 10.469 |
|      | 22 | 070.500 | MD | III | 10.492 | -      |
|      | 24 | 072.515 | RG | III | 10.385 | 10.199 |
|      | 26 | 074.345 | RG | II  | 10.283 | 10.401 |
|      | 26 | 074.510 | MD | III | 10.325 | 10.375 |
| II   | 29 | 077.335 | RG | II  | 10.392 | 10.327 |
|      | 29 | 077.505 | MD | III | 10.284 | 10.138 |
|      | 5  | 084.315 | MD | II  | 10.430 | 10.412 |
|      | 5  | 084.485 | RG | III | 10.417 | 10.339 |
|      | 10 | 089.300 | RG | II  | 10.366 | 10.426 |
|      | 10 | 089.465 | MD | III | 10.362 | 10.242 |
|      | 12 | 091.320 | MD | II  | -      | 10.292 |
|      | 12 | 091.440 | RG | III | 10.425 | -      |
|      | 16 | 095.285 | RG | II  | 10.410 | 10.421 |
|      | 16 | 095.455 | MD | III | 10.408 | 10.220 |
| III  | 27 | 106.255 | MD | II  | 10.397 | 10.355 |
|      | 27 | 106.425 | RG | III | 10.345 | 10.309 |
|      | 28 | 107.255 | RG | II  | 10.408 | 10.396 |
|      | 28 | 107.400 | MD | III | 10.425 | -      |
|      | 3  | 110.245 | RG | II  | 10.429 | 10.368 |
|      | 3  | 110.415 | MD | III | 10.346 | 10.219 |
|      | 12 | 119.385 | MD | III | 10.284 | 10.147 |
|      | 12 | 119.555 | RG | IV  | 10.268 | 10.384 |
|      | 14 | 121.385 | RG | III | 10.326 | 10.264 |
|      | 14 | 121.530 | MD | IV  | 10.397 | -      |
| IV   | 19 | 125.370 | RG | III | 10.360 | 10.312 |
|      | 19 | 125.535 | MD | IV  | 10.324 | 10.419 |
|      | 21 | 127.365 | RG | III | 10.402 | 10.252 |
|      | 21 | 127.525 | MD | IV  | 10.206 | 10.297 |
|      | 26 | 133.345 | MD | III | 10.373 | 10.322 |
|      | 26 | 133.515 | RG | IV  | 10.248 | 10.361 |
|      | 28 | 135.370 | MD | III | -      | 10.165 |
|      | 28 | 135.515 | RG | IV  | 10.289 | 10.410 |
|      | 3  | 141.325 | MD | III | 10.270 | 10.176 |
|      | 3  | 141.495 | RG | IV  | 10.267 | 10.362 |
|      | 6  | 144.290 | RG | III | 10.375 | -      |



|      |    |         |    |     |        |        |
|------|----|---------|----|-----|--------|--------|
|      | 9  | 147.315 | RG | III | 10.592 | 10.194 |
|      | 9  | 147.480 | RG | IV  | 10.126 | -      |
|      | 10 | 148.280 | MD | III | 10.357 | -      |
|      | 20 | 158.420 | RG | IV  | 10.309 | -      |
| V    | 29 | 167.430 | RG | IV  | -      | 10.335 |
|      | 11 | 179.395 | RG | IV  | 10.181 | 10.214 |
|      | 11 | 179.555 | RG | V   | 10.309 | 10.238 |
|      | 19 | 187.365 | RG | IV  | 10.290 | 10.357 |
|      | 19 | 187.535 | RG | V   | 10.235 | 10.306 |
|      | 26 | 194.345 | RG | IV  | 10.274 | 10.229 |
|      | 26 | 194.515 | MD | V   | 10.153 | 10.190 |
|      | 30 | 198.340 | RG | IV  | 10.224 | 10.259 |
|      | 30 | 198.505 | MD | V   | 10.239 | 10.268 |
| VI   | 4  | 203.350 | MD | IV  | -      | 10.266 |
|      | 4  | 203.495 | RG | V   | 10.199 | 10.240 |
|      | 5  | 204.325 | MD | IV  | 10.225 | 10.250 |
|      | 5  | 204.490 | RG | V   | 10.126 | 10.221 |
|      | 17 | 216.310 | RG | IV  | -      | 10.240 |
|      | 17 | 216.430 | MD | V   | 10.212 | -      |
|      | 20 | 219.310 | RG | IV  | -      | 10.121 |
|      | 20 | 219.445 | MD | V   | 10.127 | 10.104 |
|      | 25 | 224.435 | RG | V   | 10.275 | 10.196 |
| VII  | 27 | 226.430 | RG | V   | 10.237 | 10.225 |
|      | 3  | 232.415 | RG | V   | 10.142 | 10.220 |
|      | 10 | 239.395 | RG | V   | 10.265 | 10.263 |
|      | 10 | 239.555 | RG | VI  | 10.382 | 10.323 |
|      | 13 | 242.385 | RG | V   | 10.133 | 10.116 |
|      | 13 | 242.555 | RG | VI  | 10.231 | 10.174 |
|      | 16 | 245.375 | RG | V   | 10.208 | 10.212 |
|      | 16 | 245.545 | RG | VI  | 10.311 | 10.267 |
|      | 24 | 253.355 | RG | V   | 10.178 | 10.167 |
|      | 24 | 253.525 | RG | VI  | 10.279 | 10.248 |
|      | 28 | 257.320 | RG | V   | 10.225 | -      |
|      | 28 | 257.510 | RG | VI  | 10.200 | 10.188 |
| VIII | 1  | 261.360 | RG | V   | -      | 10.342 |
|      | 1  | 261.480 | RG | VI  | 10.357 | -      |
|      | 7  | 267.315 | MD | V   | 10.291 | 10.363 |
|      | 7  | 267.485 | MD | VI  | 10.324 | 10.270 |
|      | 14 | 274.320 | MD | V   | -      | 10.345 |
| IX   | 14 | 274.440 | MD | VI  | 10.336 | -      |
|      | 6  | 299.395 | MD | VI  | 10.177 | 10.308 |
|      | 12 | 303.385 | RG | VI  | 10.298 | 10.301 |
|      | 13 | 304.385 | MD | VI  | 10.313 | 10.324 |
|      | 17 | 308.375 | RG | VI  | 10.368 | 10.392 |
|      | 17 | 308.535 | MD | I   | 10.260 | 10.257 |
|      | 28 | 319.340 | RG | VI  | 10.184 | 10.304 |
|      | 28 | 319.530 | MD | I   | -      | 10.260 |
| X    | 10 | 331.330 | RG | VI  | -      | 10.258 |
|      | 10 | 331.475 | RG | I   | 10.286 | 10.280 |
|      | 11 | 332.330 | MD | VI  | -      | 10.241 |
|      | 17 | 338.455 | RG | I   | 10.288 | 10.333 |
|      | 27 | 348.265 | MD | VI  | 10.273 | 10.367 |
|      | 27 | 348.425 | RG | I   | 10.354 | 10.274 |
|      | 2  | 354.230 | RG | VI  | 10.243 | -      |
| XI   | 11 | 363.220 | RG | VI  | 10.391 | 10.368 |
|      | 12 | 364.190 | MD | VI  | 10.358 | -      |
|      | 12 | 364.385 | RG | I   | 10.359 | 10.260 |
|      | 14 | 366.215 | RG | VI  | 10.276 | 10.310 |
|      | 14 | 366.375 | MD | I   | 10.296 | 10.259 |
|      | 20 | 372.205 | MD | VI  | 10.264 | 10.254 |
|      | 20 | 372.365 | RG | I   | 10.319 | 10.267 |
|      | 30 | 382.360 | MD | I   | -      | 10.200 |

VALUES OF BELGRADE LATITUDE OBTAINED IN THE PERIOD 1969.0-1975.0

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|     |    |         |    |    |        |        |
|-----|----|---------|----|----|--------|--------|
| XII | 21 | 403.275 | RG | I  | 10.255 | 10.256 |
|     | 21 | 403.440 | RG | II | 10.238 | 10.242 |
|     | 22 | 404.275 | MD | I  | 10.327 | 10.319 |
|     | 22 | 404.435 | MD | II | 10.366 | 10.283 |
|     | 28 | 410.230 | RG | I  | 10.308 | -      |

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